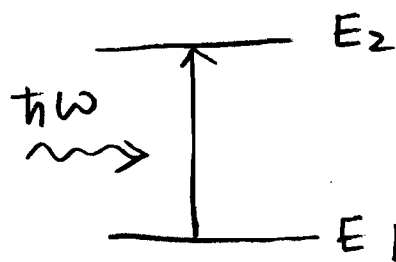


Discrete 2-level system in non-monochromatic electromagnetic field



$$R_{12} = \frac{1}{V} \sum_{\mathbf{k}} \frac{2\pi}{\hbar} |H'_{12}|^2 \delta(E_2 - E_1 - \hbar\omega_{\mathbf{k}}) \cdot \underset{\substack{\text{polarization} \\ \downarrow}}{2} n_{\text{ph}} \quad \left(\frac{1}{\text{s} \cdot \text{cm}^3}\right)$$

↑ Photon wave vector

$$n_{\text{ph}} = \frac{1}{e^{\hbar\omega_{\mathbf{k}}/k_B T} - 1} \quad \text{number of photons per state (Bose-Einstein statistics)}$$

Density of states for photons.

$$e^{i\vec{k} \cdot \vec{r}}$$

Periodic boundary cond.

$$\begin{cases} k_x = \frac{2\pi}{L} \cdot l \\ k_y = \frac{2\pi}{L} \cdot m \\ k_z = \frac{2\pi}{L} \cdot n \end{cases}$$

$$\omega_{\mathbf{k}} = \frac{kc}{n_r}$$

n_r : refractive index.

Number of states with photon energy E_{21}
 per unit volume, per energy interval $(\frac{1}{\text{cm}^3 \cdot \text{eV}})$

$$N(E_{21}) = \frac{2}{V} \int \frac{4\pi k^2 dk}{\left(\frac{2\pi}{L}\right)^3} \cdot \delta(E_2 - E_1 - \hbar\omega_k)$$

$$\hbar\omega_k = \frac{\hbar kc}{n_r} = E_{21}$$

$$k = \frac{n_r}{\hbar c} E_{21}$$

$$dk = \frac{n_r}{\hbar c} dE_k$$

$$N(E_{21}) = \frac{8\pi}{(2\pi)^3} \cdot \left(\frac{n_r}{\hbar c}\right)^2 E_{21}^2 \cdot \left(\frac{n_r}{\hbar c}\right) = \frac{8\pi n_r^3 \cdot E_{21}^2}{h^3 c^3}$$