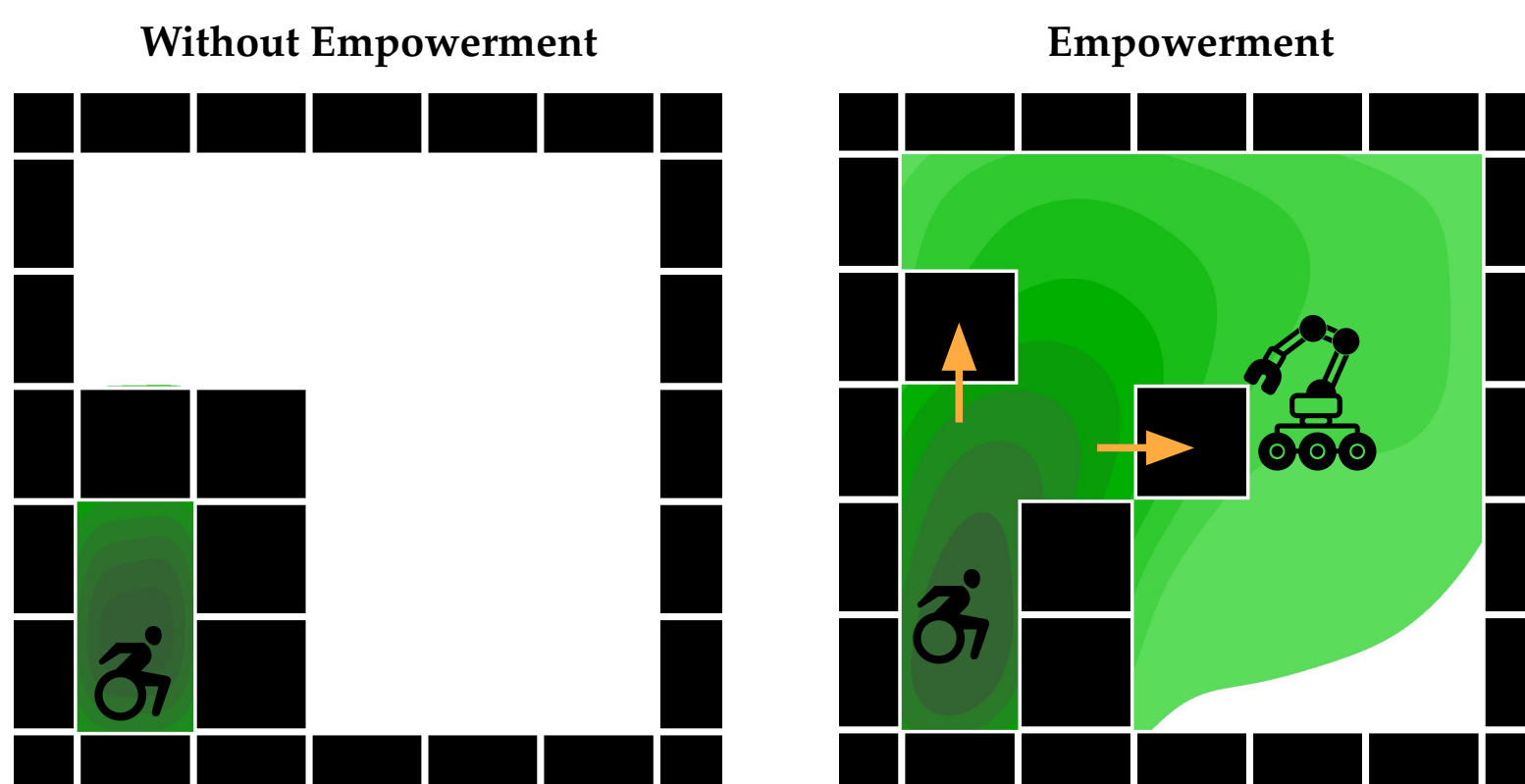


Motivation

- Assistive agents typically assume humans are optimizing a reward (e.g., CIRL [1] setup)
 - Learning rewards is hard
 - Misspecified rewards can be very harmful
 - Human objectives often not well-modeled by rewards
- How can we create aligned agents without learning and maximizing a human reward?
- Key Idea:** maximize an **empowerment objective** [2,3,4,5,6] to help the human have maximal control over the world
 - We show how a **scalable contrastive algorithm can estimate and maximize human empowerment**



Objective: Empowering Humans

- For policies π_H and π_R we define the **human empowerment** objective:

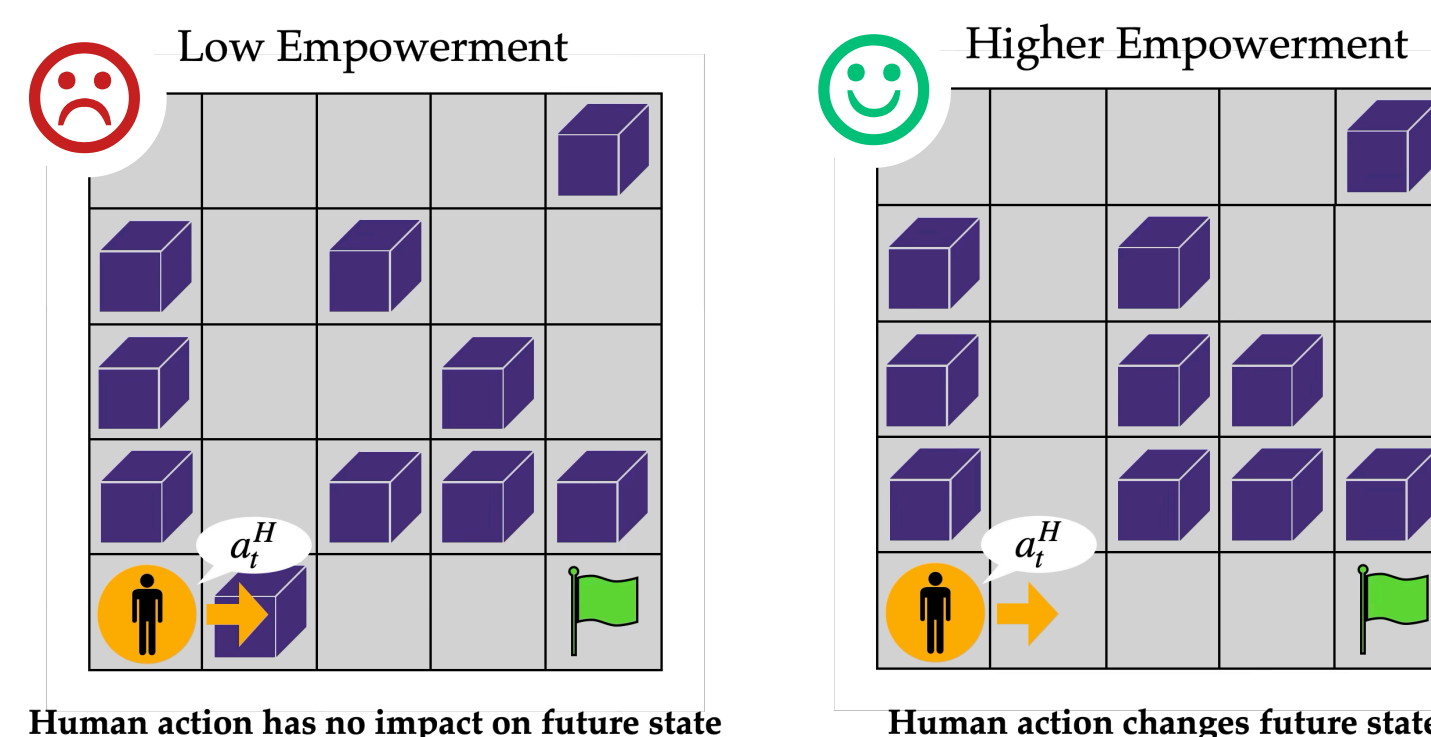
$$\mathcal{E}(\pi_H, \pi_R) = \mathbb{E} \left[\sum_{t=0}^{\infty} \gamma^t I(a_t^H; \mathfrak{s}^+ | \mathfrak{s}_t) \right]$$

↑ Empowerment ↑ Sum over future steps ↑ Mutual Informations between human action and the future state

- The mutual information term becomes:

$$I(a_t^H; \mathfrak{s}^+ | \mathfrak{s}_t) \triangleq \mathbb{E}_{\mathfrak{s}_t, \mathfrak{s}_{t+k}, a_t^H, a_t^R} \left[\log \frac{p(\mathfrak{s}_{t+k} = \mathfrak{s}_{t+k} | \mathfrak{s}_t = \mathfrak{s}_t, a_t^H = a_t)}{p(\mathfrak{s}_{t+k} = \mathfrak{s}_{t+k} | \mathfrak{s}_t = \mathfrak{s}_t)} \right]$$

When $\mathcal{E}(\pi_H, \pi_R)$ is large, the human's actions have high influence on the (γ -discounted) future state



Analysis

What does empowerment do when the human is optimizing a scalar reward?

Theorem 3.1. Under Assumption 3.1 and Assumption 3.2, for sufficiently large γ and any $\beta > 0$,

$$\mathcal{E}_\gamma(\pi_H, \pi_R)^{1/2} \leq (\beta/e) \mathcal{J}_{\pi_R}^\gamma(\pi_H).$$

Robot empowerment objective

Discounted return under human's objective

Assumption 3.1 (Skill Coverage). The rewards $R \sim \mathcal{R}$ are uniformly distributed over the scaled $|\mathcal{S}|$ -simplex $\Delta^{|\mathcal{S}|}$ such that:

$$(R + \frac{1}{|\mathcal{S}|}) (\frac{1}{1-\gamma}) \sim \text{Unif}(\Delta^{|\mathcal{S}|}) = \text{Dirichlet}(\underbrace{1, 1, \dots, 1}_{|\mathcal{S}| \text{ times}}).$$

Assumption 3.2 (Ergodicity). For some π_H, π_R , we have

$$P^{\pi_H, \pi_R}(\mathfrak{s}^+ = s | s_0) > 0 \quad \text{for all } s \in \mathcal{S}, \gamma \in (0, 1).$$

- Increasing human empowerment optimizes a **lower bound** on the **average-case reward**

References

- [1] Hadfield-Menell, D. et al., 2016. "Cooperative Inverse Reinforcement Learning." *NeurIPS*
- [2] Du, Y. et al., 2020. "AvE: Assistance via Empowerment." *NeurIPS*
- [3] Salge, C. et al., 2014. "Empowerment—an Introduction." *Guided Self Organization Inception*
- [4] Choi, J. et al., 2021. "Variational Empowerment as Representation Learning for Goal-Conditioned Reinforcement Learning." *ICML*
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Learning Empowerment

- We use a **time-contrastive objective** [7,8] to estimate empowerment:

$$\mathcal{L}_c(\{x_i\}, \{y_j\}) \triangleq \sum_{i=1}^N \left[\log \left(\frac{e^{x_i^T y_i}}{\sum_{j=1}^N e^{x_i^T y_j}} \right) + \log \left(\frac{e^{x_i^T y_i}}{\sum_{j=1}^N e^{x_j^T y_i}} \right) \right]$$

predict future from present predict past from future
 conditioned on human action unconditional classification

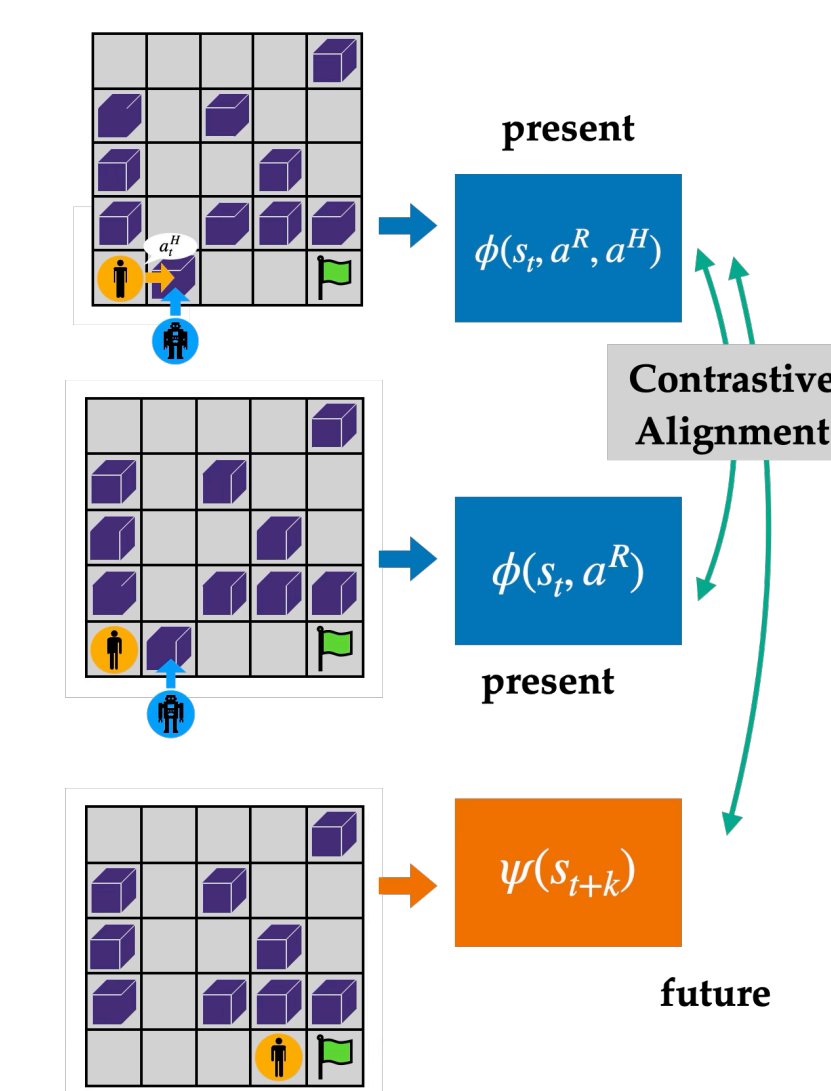
$$\max_{\phi, \phi', \psi} \mathbb{E}_{\{(s_i, a_i, s'_i) \sim P(s_t, a_t^H, s_{t+k})\}_{i=1}^N} [\mathcal{L}_c(\{\phi(s_i, a_i)\}, \{\psi(s'_i)\}) + \mathcal{L}_c(\{\phi'(s_i)\}, \{\psi(s'_i)\})]$$

- Get probability ratios both conditioned and unconditioned on the human action a^H ... which lets us approximate empowerment:

$$\mathcal{E}(\pi_H, \pi_R) \approx \mathbb{E}_{\pi_H, \pi_R} \left[\sum_{t=0}^{\infty} \gamma^t (\phi(s_t, a^R, a^H) - \phi(s_t, a^R))^T \psi(g) - \log \frac{C_2}{C_1} \right].$$

- Use this estimate as the **proxy reward** for training the robot with RL:

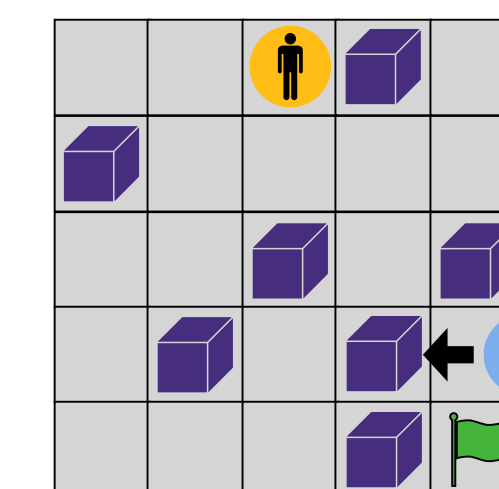
$$r(s, a^R) = (\phi(s_t, a^R, a^H) - \phi(s_t, a^R))^T \psi(g).$$



Experiments

Train our approach with a human model and no knowledge of the true human objective

Assistive Gridworld [2]



Overcooked [9]

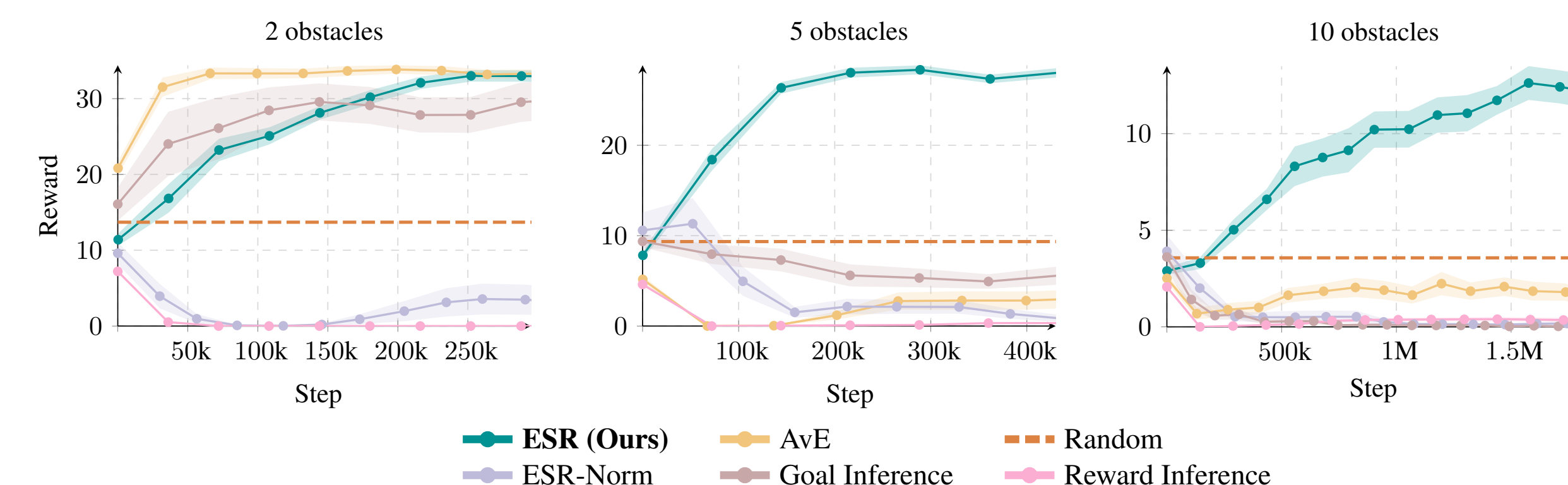
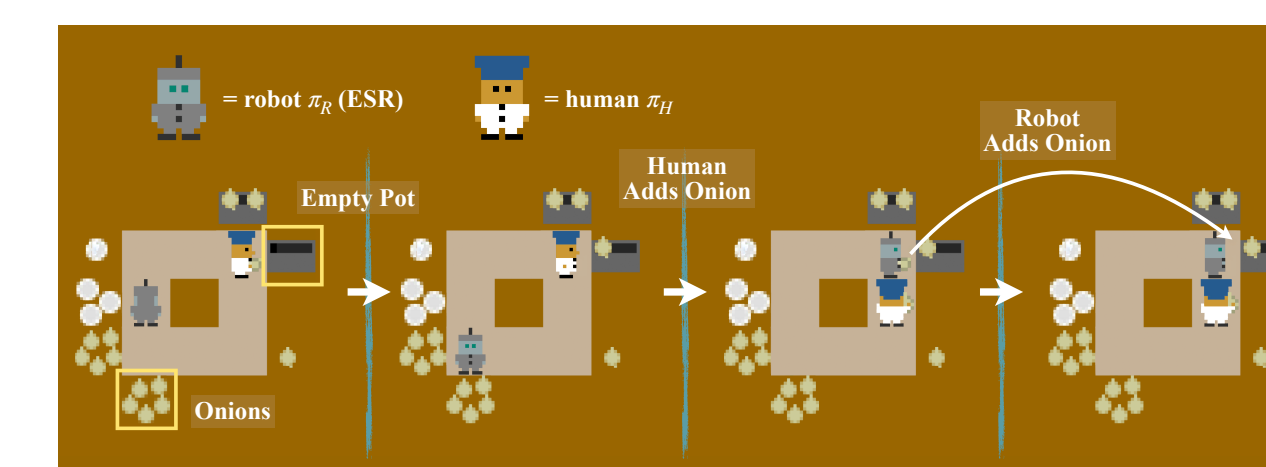


Table 1: Overcooked Results

Layout	ESR (Ours)	Reward Inference	AvE	Random
Asymmetric Advantages	72.00 ± 5.37	60.33 ± 0.26	36.71 ± 1.71	59.36
Coordination Ring	8.40 ± 0.69	5.96 ± 0.20	5.69 ± 0.93	6.02
Cramped Room	91.33 ± 4.08	39.24 ± 0.35	5.13 ± 1.31	69.26

Notation

- Two agents interact in an MDP

$$M = (\mathcal{S}, \mathcal{A}_H, \mathcal{A}_R, R, P, \gamma)$$
 - Human H
 - Assistive agent ("robot") R
- Two policies $a_t^R \sim \pi_R(\cdot | \mathfrak{s}_t)$ and $a_t^H \sim \pi_H(\cdot | \mathfrak{s}_t)$
- Dynamics $P(s' | s, a^H, a^R)$
 - random variables \mathfrak{s}_t represent state at time t
 - future state \mathfrak{s}^+ is a random \mathfrak{s}_K with $K \sim \text{Geom}(1 - \gamma)$