

Energy Efficient Routing with Delay Guarantee for Sensor Networks

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January 3, 2006

Abstract

The paper presents a routing algorithm that maximizes the lifetime of a sensor network in which all data packets are destined to a single collection node. Lifetime is maximized by adjusting the number of packets traversing each node. The adjustment is carried out by transmitting over alternative routes. First part of the paper assumes that the worst case delay resulting from energy efficient routing is less than the maximum tolerable value. Ignoring the delay constraint of the network, the routes are selected as the solution to a linear programming (LP) problem in which the objective is to maximize the minimum lifetime of each node. The solution is first implemented in a centralized algorithm. The LP solution is then approximated by an iterative algorithm based on least cost path routing, in which each step is implemented efficiently in a distributed manner. Second part of the paper incorporates delay guarantee into energy efficient routing by limiting the length of the routing paths from each sensor node to the collection node. Simulations reveal that the lifetime of the network increases significantly by optimal routing and there is not always a tradeoff between the delay guarantee and the battery lifetime of the sensor network. The delay of the network keeps increasing as the maximum allowed delay value increases although the optimal lifetime and the connectivity of all the nodes to the collection node is achieved so including delay constraint in energy efficient routing improves the network performance.

1 Introduction

A wireless sensor network consists of a group of nodes, each comprising one or more sensors, a processor, a radio and a battery. Such sensor networks are expected to find widespread use in such applications as traffic monitoring on freeways or urban street intersections, seismic and medical data-gathering because of their low cost, small size and wireless data transfer [1].

A key concern in wireless sensor networks is energy efficiency. The nodes in a sensor network may not be charged once their energy is drained so the lifetime of the network depends critically on energy conservation mechanism. As shown in [2], most of the battery energy is consumed by the radio. A Time Division Multiple Access (TDMA) scheme at the medium access control layer (MAC) achieves to decrease this energy consumption by avoiding overhearing other nodes' packets, idle listening and collisions. However, when MAC protocol power savings are not combined with power efficient routing, there will be high variations in energy spent in transmission and reception of packets for different nodes due to the different number of packets that each node needs to forward. This will cause some nodes to die earlier, which will decrease the efficiency of the network. Throughout the rest of the paper, we assume that MAC protocol can completely eliminate overhearing, idle listening and collision problems and we focus on adjusting the number of packets forwarded by each node through the choice of different paths in the network. It is straightforward to make changes in the formulations based on different MAC protocol capabilities.

A wireless sensor network is a special class of ad hoc network, in which every packet is destined for the same collection node. Numerous routing protocols have been developed for general ad hoc wireless networks to provide correct and efficient route establishment between the nodes in the network so that messages can be delivered in a timely manner during mobility and changing topology [4]. Shortest hop routing is the most common metric used in table-driven protocols such as DSDV (Destination-Sequenced Distance-Vector) and WRP (Wireless Routing Protocol), and source-initiated protocols such as AODV (Ad Hoc On-Demand Distance Vector) and DSR (Dynamic Source Routing). Routing based on shortest hop, however, is not suitable for sensor networks where there are many flows towards one access point and the elimination of a node may disconnect a large number of nodes from the access point.

Various power-aware metrics have been discussed in [5] to find the traffic distribution that balances the energy consumption optimally. These metrics include maximizing the time to network partition, minimizing the variance in node power levels, minimizing cost per packet and minimizing maximum node cost. The metric of maximizing the time during which all nodes are alive is formulated as a Linear Programming (LP) problem in [6, 7]. None of these schemes, however, propose a routing protocol that makes use of this formulation. The effect of the metric of minimizing the cost per packet is investigated for different cost functions in [5, 6, 8, 9, 10]. The cost depends on the ratio of the initial battery energy to remaining battery energy in [5, 6, 10] or on the ratio of the rate of energy consumption to the remaining energy of the node in [8, 9]. The relation of maximizing the minimum lifetime of the nodes to minimizing the cost per packet has been previously investigated in [6]. We take this relation one step further to provide a delay guarantee on the arrival of the packets to their destination while maximizing the network lifetime.

The first part of this paper formulates the lifetime maximization problem as a linear programming (LP) problem, and proposes a routing protocol for centralized implementation of LP problem. The centralized protocol is based on decomposing the LP solution into multiple routing trees.

A distributed routing protocol is then proposed to implement this decomposition by a sequence of least cost path problems, where the cost of a path is the sum or the maximum of the cost of the nodes on that path and the cost of each node is a function of its initial and remaining battery energy. This distributed implementation provides a platform for simultaneously achieving energy efficient routing and delay guarantee since delay guarantee cannot be introduced into LP formulation before decomposition.

The second part of the paper extends the energy efficient routing to provide a guarantee on the maximum delay each packet experiences. Minimizing energy consumption subject to a deadline or delay constraint has been introduced in [11]. [11] proposes an algorithm for the scheduling of the packet transmissions over a wireless link based on the observation that in many channel coding schemes the energy required to transmit a packet can be significantly reduced by transmitting the packet over a longer period of time. In this paper, we generalize this problem for a multi-hop network. We assume that the transmission rate is fixed and limit the number of hops each packet experiences in the network to provide a guarantee on the worst case delay. To the best of our knowledge, this is the first work that considers energy efficient routing with delay guarantee in multi-hop networks.

The rest of the paper is organized as follows: Section 2 presents the assumptions necessary for formulating the problem. Section 3 gives the LP formulation of maximizing the network lifetime and introduces a routing algorithm based on the LP solution. Section 4 describes a distributed algorithm based on least cost path routing that aims to achieve optimal lifetime. Section 5 proposes routing protocols that incorporate delay into the energy efficient routing with the goal of providing a delay guarantee. Section 6 analyzes the memory and CPU requirements at the sensor nodes for the implementation of these algorithms. Simulation results are in Section 7. In Section 8, some concluding remarks are made.

2 Assumptions

The following assumptions underly this study.

1. Consider a wireless ad hoc network that consists of one access point (AP) and several sensor nodes that generate data for transfer to the AP.
2. The transmission power of all the sensor nodes are the same across the network. Each node is supported by an omnidirectional antenna. Consequently, links are bidirectional: If two nodes i and j transmit at the same power, then if node i can hear node j , node j can also hear node i . Bidirectional links are needed for the proper functioning of some network protocols such as distributed Bellman-Ford algorithms [12].
3. The topology information of the sensor network is represented by a graph $G = (V, E)$, in which V is the set of nodes, including the AP as node 1. The edges $E \subset V \times V$ are such that $(i, j) \in E$ if nodes i and j can transmit to each other. N and $|V|$ are used interchangeably to denote the number of nodes in the network including AP.
4. The nodes in the network are assumed to generate data at a specific rate, which may be different for each node. The LP formulation in Section 3 requires the estimation of these rates at the beginning whereas they can be learnt iteratively for the iterative routing algorithms in Section 4.
5. Data generated at a node is independent of the transmission structure. The data aggregation models where the amount of data supplied at nodes does depend on the routing paths [13] is a much harder problem and beyond the scope of this paper.
6. The power consuming parts in a sensor node are radio, sensor and microprocessor. We assume that MAC protocol operate the radios in sleep mode when the sensor nodes are not transmitting or receiving a packet.
7. The operational lifetime of the sensor network is defined to be the time until the first node dies since sensor network monitoring can be impaired by the early death of some nodes and the possible disconnectedness of some other nodes from AP as a result. The relation of this lifetime estimate to the time duration

until different fractions of the nodes die is given in Section 7.

3 Centralized Energy Efficient Routing

The objective of the routing algorithm is to determine the optimal path from each sensor node to the AP based on the topology of the network and the packet generation rates at the sensor nodes. Optimizing the routing paths will assign packet flow rate f_{ij} from node i to node j for $i, j \in V$. As long as these optimal flow rates are non-zero for at least two flows outgoing from a node in the network, choosing the same routing path all the time will not be optimal. In this case, the next hop for node $i \in V$ has to alternate among nodes $j \in V$ for which $f_{ij} \neq 0$. Notice that this is not multiple path routing since at any given time, there is still a single path from each sensor node to the AP, but this path may change over time.

Section 3.1 describes the LP formulation for determining optimal flow rates. Section 3.2 proposes a routing protocol based on the centralized calculation of these optimal values through the LP formulation.

3.1 Linear Programming Formulation

The optimization problem is given in Figure 1. The variables of the problem are the packet flow rates f_{ij} , which is the average time spent for the transmission of the packets from node i to node j in unit time, and the network lifetime t .

The goal of the problem is to maximize the time duration during which all nodes are alive.

The first constraint represents the non-negativity constraint of flows, whereas the second constraint eliminates the possibility of flows between the nodes without a communication link. The third constraint represents the requirement that the net flow out of each node i be the time required to transmit the packets generated in that node $g_i t t$, where $t t$ is the transmission time of one packet and g_i is the packet generation rate at node i , except AP. The fourth constraint represents the requirement that the to-

$$\begin{aligned}
& \text{Maximize } t \\
& \text{Subject to: } f_{ij} \geq 0 \text{ for } i, j \in [1, N] \\
& f_{ij} = 0 \text{ for } (i, j) \notin E \\
& \sum_j f_{ij} - \sum_j f_{ji} = g_i \text{ for } i \in [2, N] \\
& t(\sum_j p_{tx} f_{ij} + \sum_j p_{rx} f_{ji} + p_s g_i + (1 - \sum_j f_{ij} - \sum_j f_{ji}) p_l) \leq e_i \text{ for } i \in [2, N]
\end{aligned}$$

Figure 1: Linear Programming model for determining optimal flows along each link

tal energy consumed by node i during the network lifetime, which is given by the product of the network lifetime t and the energy consumed per unit time, be less than its total energy e_i . The total energy consumed in unit time includes the energy spent in transmission and reception of packets, listening to the channel and sensing. The energy spent in transmission and reception are $\sum_j p_{tx} f_{ij}$ and $\sum_j p_{rx} f_{ji}$ respectively, where p_{tx} is the energy spent for the transmission of a packet in unit time and p_{rx} is the energy spent for the reception of a packet in unit time. The energy spent in listening to the channel is then $(1 - \sum_j f_{ij} - \sum_j f_{ji}) p_l$, where p_l is the energy spent per unit time by the radio in sleep mode since the radio is assumed to sleep by MAC protocol if there is no transmission or reception of packets. Finally, the energy spent in sensing is $p_s g_i$, where p_s is the energy spent in obtaining the samples in one packet.

This problem is LP problem since all the constraints are linear in the variables when we replace variables f_{ij} by $t f_{ij}$.

In order to use this algorithm in a practical framework, a routing protocol is needed to decompose the network with optimal flow rates $f_{ij}, i, j \in V$ into multiple routing trees. Then the nodes in the network will be scheduled by a TDMA protocol at the MAC layer such that all packets reach the AP by a deadline. Since any routing tree may result from this decomposition, the deadline should be achieved for all possible such trees.

Let us assume that the time is divided into time slots. Each time slot is long enough to carry one packet. The TDMA scheduling algorithm guarantees the transmission

of at least one packet in each time slot. Then the necessary and sufficient condition for the network to meet the delay constraint $delay_{max}$ for all possible routing trees is $tt(|V| \sum_{i \in V} g_i) \leq delay_{max}$. This is equivalent to sending all packets generated in the network on the path containing maximum possible number of hops, which is $|V|$. This assumption is not stated for the similar formulation described in [6] but is an implicit assumption for the LP formulation described above. Putting capacity constraints on the nodes such as $\sum_j f_{ij} + \sum_j f_{ji} \leq delay_{max}$ is not enough since it takes time for the flows to be transferred across the network. The problem of adjusting the energy efficient routing paths to provide a delay guarantee in the network is examined in Section 5.

3.2 Routing Protocol

The linear programming approach provides optimal flow rates based on the complete topology information and packet generation rate at each node. We now provide a routing algorithm that generates a single path from any sensor node to the AP at each time and attains the optimal flow rates at each link at the end.

We first prove that a directed acyclic graph ¹ attains the maximum lifetime while satisfying all constraints in LP formulation in Figure 1. We then give an algorithm to obtain such a directed acyclic graph solution and then to decompose it into directed-in-trees ². The optimal solution can then be attained by routing the packets over each of these directed-in-trees for the proportion of the battery lifetime of the network equal to its weight.

Theorem 1 *Consider the set of directed graphs consisting of arcs from node i to node j if and only if value of f_{ij} optimal for LP problem in Figure 1 is positive. The set includes a directed acyclic graph.*

Proof We prove this theorem by providing an algorithm that takes a possibly cyclic graph and at each iteration

¹ A directed acyclic graph is a directed graph where no path starts and ends at the same vertex.

² A directed-in-tree rooted at node s is a tree where there is a unique directed path from any node to the node s . Every node in the directed-in-tree (except node s) has outdegree 1.

eliminates one cycle in the graph by subtracting the minimum flow rate in the cycle from all the flow rates of the cycle without decreasing the lifetime of the network while satisfying the constraints. \square

After obtaining the solution to the LP problem, the directed simple cycles in the graph can be found by using an extension of Depth-First Search (DFS) algorithm [14]. Then the cycles can be eliminated by the method given in the proof of Theorem 1 to obtain a directed acyclic graph solution for the LP problem in Figure 1. This solution can then be expressed as a superposition of multiple directed-in-trees due to its acyclic property. We now prove that we can find such directed-in-trees that satisfy the constraints of the problem in Figure 1. We first need the following lemmas.

Lemma 1 *An undirected graph $G = (V, T)$ is a tree if it has $|V| - 1$ edges and is acyclic.*

Proof See [14] for the proof. \square

Lemma 2 *Let $G^v = (V, E^v)$ be a directed acyclic graph such that $outdeg(i) = 1$ for $i \in \{2, 3, \dots, |V|\}$ and $outdeg(1) = 0$. Then G^v is a directed-in-tree rooted at node 1.*

Proof Let $G_u^v = (V, E_u^v)$ be an undirected graph such that $(i, j) \in E_u^v$ only if $(i, j) \in E^v$. G_u^v does not contain any cycle since otherwise the outdegree of at least one node in the cycle must be 2 in G^v in order not to form a directed cycle. Besides, G_u^v has $|V| - 1$ edges. Thus, it is a tree by Lemma 1. If G^v is a directed-in-tree, the root must be node 1 since $outdeg(1) = 0$. Let us choose node 1 as the root of G_u^v . We can then prove that the head of each arc in G^v is closer to the node 1 than its tail by contradiction. \square

For the directed acyclic graph solution to the LP problem shown in Figure 1, let $f_{ij}, i, j \in V$ be the optimal flow rate from node i to node j , $E^+ = \{(i, j) | f_{ij} > 0\}$, $G = (V, E^+)$. Denote optimal lifetime by t_o . G is decomposed into multiple routing trees as follows:

1. Choose one outgoing link from each node $i \in V$ such that $f_{ij} > 0$ and use the single path from each sensor node to the AP on the resulting directed-in-tree rooted at the AP as the routing path.
2. If the packet flow up to now along at least one link $(i, j) \in E^+$ on the tree is greater than $f_{ij}t_o$, set $f_{ij} = 0$.
3. If $\sum_{i,j} f_{ij} = 0$, stop. Else, go back to step 1.

Choosing one outgoing link at each node in step 1 guarantees that the resulting graph is a directed-in-tree by Lemma 2.

The routing protocol is then given as follows. Assume that the AP has enough processing energy whereas the sensor nodes are energy limited. At the beginning, the sensor nodes determine their parent in the shortest path tree (SPT), i.e. tree that contains minimum-hop path from each sensor node to the AP, in order to send their topology information to the AP. This can be performed by flooding a packet from the AP to the sensor nodes, which then choose their parent to be the node sending the packet over least number of hops. During this flooding, the sensor nodes also determine the identity of their neighbors, nodes with which direct communication can be established. They then send their neighbor information to the AP over SPT (See [2] for a detailed topology discovery protocol). AP runs the LP problem, and sends the optimal flow rates of the directed acyclic graph and the optimal lifetime to all the nodes in the network. A sensor node i then chooses one of the outgoing links at each time to forward the packets in the network as long as the total packet flow at each link (i, j) is less than $f_{ij}t_o$.

4 Distributed Energy Efficient Routing

In the previous section, we used LP programming in order to determine optimal routing paths from each node in the network to the AP to maximize the system lifetime. Solving LP problem, however, requires the whole network topology, packet generation rate at each node and too many computations to be implemented at a sensor node. In this section, we provide an algorithm that approximates the LP solution through successive more efficiently solved optimization problems, minimum cost path problems. This approximation will also be useful in in-

corporating delay constraint into the routing protocol in Section 5.

The goal of the distributed energy efficient routing is to get as close as possible to the optimal LP lifetime while periodically executing a distributed routing algorithm based on the remaining and initial energy of each node. We present two distributed routing algorithms, namely *least sum-cost path algorithm* and *least max-cost path algorithm*, to be implemented for each period. These algorithms aim at minimizing the cost of the routing paths from each sensor node to the AP, where the cost of the path is defined as the sum or maximum of the costs of the links on that path. They are closely related to previous work on minimizing the cost per packet in [5, 6, 8, 9, 10].

Recall that the topology of the network is represented by the graph $G = (V, E)$ where $(i, j) \in E$ if nodes i and j can communicate with each other. Let us define the directed graph equivalent of G by $G_d = (V, E_d)$ where $\langle i, j \rangle \in E_d$ and $\langle j, i \rangle \in E_d$ for each $(i, j) \in E$. The iterative algorithm consists of obtaining a directed graph with a cost C_{ij} assigned to every link $\langle i, j \rangle \in E_d$ and then finding the shortest path tree from AP to all the nodes in that graph at the beginning of each time frame to be used for routing until the end of that frame.

Since the cost of the links are used in finding the shortest path from AP to the sensor nodes, the cost of directed link $\langle j, i \rangle$, C_{ji} , is equal to the cost of including the node i on the path. A one-to-one node cost function for node i at p -th iteration is defined to be the ratio of the total energy consumed up to period p over the total battery energy:

$$C_i = \frac{\text{total consumed energy}}{\text{total battery energy}} \quad (1)$$

$$= p * \frac{\sum_j p_{tx} f_{ij} + \sum_j p_{rx} f_{ji} + p_s g_i + (1 - \sum_j f_{ij} - \sum_j f_{ji}) p_l}{e_i} \quad (2)$$

where f_{ij} is the average resulting flow rate on link $\langle i, j \rangle$. The above node cost function increases from value 0 to value 1 as network evolves. The link cost function can be any monotonically increasing function of C_i over interval (0,1) for some d such that $C_{ji} = d(C_i)$. For instance, the cost function used in [6] is defined to be the ratio of total battery energy to the remaining energy, which represents the case for which $d(x) = \frac{1}{1-x}$.

The next step is to calculate the shortest path from node 1 (AP) to all other nodes in the network where the cost of the path P from node i to node j is defined as the sum and maximum of the costs of the links in P for least sum-cost path algorithm and least max-cost path algorithm respectively. Bellman-Ford algorithm can be used to calculate this tree for both of these algorithms while requiring a slight change for least max-cost path algorithms, which is changing the action at each pulse from $\forall \langle i, j \rangle \in E_d$, if $ct(j) > ct(i) + C_{ij}$, $ct(j) = ct(i) + C_{ij}$ and $pred(j) = i$ to $\forall \langle i, j \rangle \in E_d$, if $ct(j) > \max(ct(i), C_{ij})$, $ct(j) = \max(ct(i), C_{ij})$ and $pred(j) = i$, in which $ct(i)$ is the cost of node i . The proof of the correctness of this algorithm is analogous to that of Bellman-Ford algorithm and the complexity remains the same. The stopping condition is the death of a node $i, i \in V - \{1\}$.

The routing protocol is then given as follows. The time is divided into time frames. At the beginning of a time frame, each sensor node $i \in V$ calculates its *node cost* C_i as described in Equation 1 to be used in the calculation of C_{ji} , and initializes its *cost* $ct(i)$ to ∞ (The cost of the AP $ct(1)$ is initialized to 0). The AP floods the network with a tree construction packet. This packet contains the *node cost* and *cost* of the transmitting node in the routing tree. Upon reception of a tree construction packet, the sensor node checks whether the transmitting node is the next hop on a path of smaller cost than previously learned paths. This is achieved by checking the condition $ct(j) > ct(i) + C_{ij}$ ($ct(j) > \max(ct(i), C_{ij})$) in least sum-cost (max-cost) path algorithm, in which j is the receiving node and i is the transmitting node. If the condition holds, the receiving node updates this *cost* by $ct(j) = ct(i) + C_{ij}$ ($ct(j) = \max(ct(i), C_{ij})$) in least sum-cost (max-cost) path algorithm, and rebroadcasts the packet. At the end of the flooding, each sensor node chooses its parent node to be the next hop neighbor on the least cost path to the AP, and use this next hop until the end of the time frame.

Simulation results in Section 7 show the effect of different cost functions for least sum-cost path algorithms and their comparison to least max-cost path algorithm and LP solution.

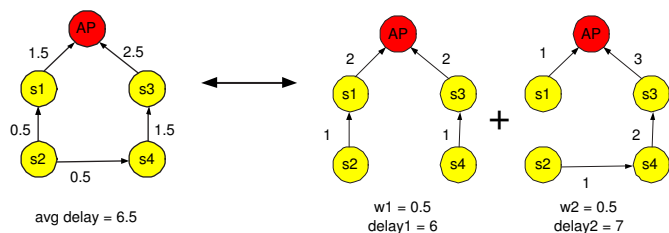


Figure 2: Delay performance of the routing trees resulting from the decomposition of the optimal flow graph.

5 Energy Efficient Routing with Delay Guarantee

Energy efficient routing may choose paths much longer than the shortest paths to the AP while avoiding nodes with small residual energy. Longer paths may prevent the system from achieving delay guarantee. This section aims to give a delay guarantee on the arrival of packets to the AP while generating energy efficient paths.

One way to introduce delay constraint in the optimization problem formulated in Figure 1 is to upper bound the total flow rate by the delay constraint $delay_{max}$:

$$\sum_i \sum_j f_{ij} \leq delay_{max} \quad (3)$$

To understand whether the flow rates optimal for the optimization problem satisfy the delay constraint, we have to understand the routing algorithm in a practical framework. The network with optimal flow rates f_{ij} assigned to each link $(i, j) \in E$ needs to be decomposed into multiple routing trees. At each time, the network will use one of these trees so a single path from each sensor node to the AP. However, guaranteeing the average delay does not tell anything about the delay at a specific time. Figure 2 illustrates this problem. The optimal flow rates are shown on the left whereas the decomposition is shown on the right. If all the nodes interfere with each other, then the delay is 7 time slots half of the total network lifetime although the average delay satisfies the delay constraint of 6.5 time slots.

We now introduce delay constraint on the decomposed network based on the distributed implementation described in Section 4. We assume that the transmission rate is fixed and limit the number of hops each packet experiences in the network to provide a guarantee on the worst case delay.

In order to give a guarantee of the maximum delay on the arrival of the packets to the AP, MAC protocol should be based on TDMA such as PEDAMACS [2] instead of random access. In [3], it is shown that the problem of minimizing the length of a schedule, which is the maximum delay of the packets to reach the AP, based on the connectivity and conflict graph is NP-complete. The problem of finding the routes from each sensor node to the AP such that the MAC layer guarantees a maximum length of the schedule is even much harder than the problem of finding minimum length schedule given the routing paths in the network. Therefore, we aim to guarantee the worst case delay while generating energy efficient routes.

We assume that MAC protocol is TDMA and guarantees the movement of at least one packet in each time slot. We first generate a distributed algorithm based on an upper bound on the worst case delay. Then we show how to improve the performance in terms of energy efficiency and connectivity by using a centralized controller to help the nodes choose one of the paths available at each node based on the worst case delay.

5.1 Level Restricted Energy Efficient Routing (LR-ENR)

Distributed Bellman-Ford algorithm is used to provide a guarantee on the delay by limiting the number of iterations. Bellman-Ford algorithm is known to find the minimum cost path of length at most i at iteration i [14]. The number of iterations is found by an upper bound on the worst case delay.

The worst case delay in the network is $tt \sum_{i \in V} l_i g_i$ where l_i is the length of the path from node i to the AP, g_i is the packet generation rate at node i and tt is the length of a time slot that includes the transmission time of a packet and a guard interval ($l_1 = 0$ since node 1 is AP). This de-

lay is upper bounded by $d * g * tt$ where d is the maximum of the lengths of the routing paths from each sensor node to the AP and g is the total number of packets generated in the network.

Given a delay requirement $delay_{max}$, we therefore calculate the maximum path length d_{max} as follows:

$$d_{max} = \operatorname{argmax}_d d * g * tt \leq delay_{max} \quad (4)$$

A modified version of Bellman-Ford algorithm can then be executed to find minimum cost paths of length at most d_{max} from each node to the AP. Instead of running each iteration of Bellman-Ford pulse for $|V|$ times and just keeping the parent in the routing tree, the modified version runs each pulse for d_{max} times and keeps the minimum cost path from each node to the AP.

The routing protocol is therefore the same as the distributed implementation described in Section 4 except the inclusion of a counter and the complete routing path in the tree construction packet. The time is divided into time frames. At the beginning of the frame, the AP floods the network with a tree construction packet. The tree construction packet keeps a *counter* c and the nodes on the routing path it followed starting at the AP in addition to the *node cost* and *cost* of the transmitting node in the routing tree. c is initialized to 0 at the AP and increased by 1 at each transmission. Upon reception of a tree construction packet, the sensor node checks whether the transmitting node is the next hop on a path of smaller cost than previously learned paths only if this counter c is less than d_{max} and ignore the packet otherwise. If $c < d_{max}$ and a smaller cost path is found, the sensor node updates the *cost* in the packet, increases the *counter* c by 1, adds its ID to the routing path the packet followed, and rebroadcasts the packet. At the end of the flooding, each sensor node chooses the minimum cost routing path, and use this path until the end of the time frame.

5.2 Hop Restricted Energy Efficient Routing (HR-ENR)

We can achieve higher lifetime and connectivity for a certain delay constraint by using a centralized controller

Minimize $\sum_{i=2}^N \sum_{j=1}^N A_{ij} x_{ij}$
 Subject to: $x_{ij} \geq 0$ for $i \in [2, N], j \in [1, N], x_{ij}$
 integer
 $\sum_{j=1}^N x_{ij} = 1$ for $i \in [2, N]$
 $tt \sum_{i=2}^N \sum_{j=1}^N j g_i x_{ij} \leq delay_{max}$

Figure 3: Integer Programming model of path length optimization

based on the exact worst case delay instead of an upper bound on this delay as in Section 5.1. This is achieved by running the Bellman-Ford iterations $|V|$ times and then optimizing the path lengths based on the cost of the paths at each iteration.

If the vector containing the length of the routing paths, $l = [l_1, \dots, l_{|V|}]$, was given, the minimum cost paths would be found by running Bellman-Ford algorithm for the number of times equal to l_j for node $j \in V$. In this problem, on the other hand, the delay requirement $delay_{max}$ is given. This restricts the lengths of the paths such that $tt \sum_{i \in V} l_i g_i \leq delay_{max}$. The problem is then to find the optimal vector $l = [l_1, \dots, l_{|V|}]$ that minimizes the total cost while satisfying $tt \sum_{i \in V} l_i g_i \leq delay_{max}$.

Figure 3 gives the IP formulation for choosing the optimal length of the paths based on the costs determined by Bellman-Ford algorithm. The variables of the problem are x_{ij} , which is 1 if the length of the path chosen by node i is j and is zero otherwise. The input to the problem is the cost of the paths A_{ij} and the packet generation rates g_i , in which A_{ij} represents the cost of the minimum cost path of length at most j from node i to the AP and g_i represents the packet generation rate at node $i \in V$.

The goal of the problem is to minimize the total cost of the paths. The first constraint represents the non-negativity constraint of x_{ij} whereas the second constraint represents the requirement that only one of the paths be chosen by each node $i \in V$. The third constraint rewrites the delay constraint requirement $tt \sum_{i \in V} l_i g_i \leq delay_{max}$ in terms of the variables x_{ij} .

The routing protocol is then given as follows. The time is

divided into time frames. At the beginning of the frame, the AP floods the network with a tree construction packet, which contains the counter, its routing path, node cost and the cost of the transmitting node in the routing tree. The first part of the algorithm is similar to the one described in Section 5.1. The only difference is that each node $i \in V$ keeps the minimum cost path of length at most l for all $1 \leq l \leq |V|$. Upon reception of a tree construction packet, the sensor node checks whether the cost of the path is smaller than that of previously learned paths of the same length. If so, it updates its minimum cost path for that length, and rebroadcasts the packet. At the end of the flooding, each sensor node knows about the minimum cost path of each length. They then send only the cost of the paths corresponding to each length $1 \leq l \leq |V|$, not the paths themselves, to the AP. The AP finds the optimal path length for each node based on the formulation in Figure 3 and sends it back to the sensor nodes in the network. The sensor nodes then use the routing path of the optimal length until the end of the frame.

6 Complexity Analysis

Since each individual wireless sensor node is usually a small device with limited memory space and computational capability, it is important to understand the memory and CPU requirements of the implementation of these algorithms at the sensor nodes.

For the centralized algorithm in Section 3.2, the per node memory requirement is $O(deg_{max})$ whereas the CPU requirement is $O(deg_{max}|V|)$, where deg_{max} is the maximum degree of the nodes in G . Each node has to keep the ID of its neighbors, the optimal rates of the links to these neighbors and the optimal lifetime in the memory, which is of complexity $O(deg_{max})$. At the beginning, the nodes send and receive packets to find the shortest path to the AP and discover their neighbors. The maximum number of iterations is $|V|$. In each iteration, each node sends at most one packet and receives at most deg_{max} packets. Each packet contains the ID and cost of the transmitting node. The sensor nodes then send their own topology information and forward their children's topology informa-

tion to the AP. The maximum number of packets that is forwarded is $|V|$ whereas each packet contains the ID of each node's neighbors. Finally, the optimal flow rates on the links to all neighbors of the sensor nodes and optimal lifetime are sent back to the nodes. Each of these steps require $O(deg_{max}|V|)$ packets to send and receive, resulting in $O(deg_{max}|V|)$ CPU requirement.

For the distributed algorithm described in Section 4, the per node memory requirement is $O(1)$ whereas the CPU requirement is $O(deg_{max}|V|)$. Each node just needs to keep the parent in the minimum cost path to the AP and its cost in the memory, resulting in complexity of $O(1)$. The nodes send and receive packets to find the shortest path to the AP. Each packet contains the ID and cost of the transmitting node. Therefore, the CPU complexity is $O(deg_{max}|V|)$.

For the level restricted energy efficient routing algorithm described in Section 5.1, the per node memory requirement is $O(|V|)$ whereas the CPU requirement is $O(deg_{max}|V|^2)$. Each node needs to keep the cost of the minimum cost path and all the nodes on that path. The maximum path length is $|V|$ so the memory complexity is $O(|V|)$. The nodes send and receive packets to find the shortest path to the AP. Each packet contains the ID and cost of the transmitting node, the nodes on the path followed by the packet and the counter. The maximum number of nodes on a path is d_{max} . Therefore, the CPU complexity is $O(deg_{max}d_{max}^2|V|^2)$, which is at maximum $O(deg_{max}|V|^2)$.

For the hop restricted energy efficient routing algorithm described in Section 5.2, the per node memory requirement is $O(|V|^2)$ whereas the CPU requirement is $O(deg_{max}|V|^2)$. Each node needs to keep the minimum cost path corresponding to each length l for $1 \leq l \leq |V|$. The maximum path length is $|V|$, which results in memory complexity of $O(|V|^2)$. The nodes send and receive tree construction packets to find the shortest path to the AP. The complexity of this step is $O(deg_{max}|V|^2)$. The sensor nodes then send their costs and forward their children's cost information to the AP. The maximum number of packets that is forwarded is $|V|$ whereas each packet contains the cost of $|V|$ paths, resulting in a complexity of $O(|V|^2)$. Finally, the optimal path lengths are sent back

algorithm	memory	CPU
centralized	$O(deg_{max})$	$O(deg_{max} V)$
distributed	$O(1)$	$O(deg_{max} V)$
LR-ENR	$O(V)$	$O(deg_{max} V ^2)$
HR-ENR	$O(V ^2)$	$O(deg_{max} V ^2)$

Table 1: Memory and CPU requirements of the sensor nodes for algorithm implementations.

to the nodes, resulting in a complexity of $O(|V|)$.

These complexity results are summarized in Table 1.

7 Simulation

The purpose of our simulation is to observe the amount of increase in network battery lifetime as a result of route optimization and to examine the effect of different link cost functions and delay constraints on the network lifetime.

In the simulations, the nodes are randomly distributed in a circular area of radius 100 units unless otherwise stated. The transmission range is chosen to be slightly larger than the threshold necessary for connectivity of the network [15]. The graph $G = (V, E)$ is obtained by placing edges between the nodes closer than this transmission range. The results discussed below are averages of the performance of ten different random configurations.

The energy consumed in transmission and reception of packets, listening to the channel and sampling are derived from the power consumption figures for the Berkeley mica nodes, which is given in Table 2. The transmission rate is 50 kbps. The packet generation rate g_i at each node i is 1/30 per second, which is a typical value for traffic light applications [3]. The battery power level e_i is chosen to be that of a pair of AA batteries, which can supply 2200mAh at 3V, for all nodes $i, i \in V - \{1\}$. The sampling rate is 128Hz at each node.

Figure 4 compares the lifetime of the network using the routing determined by the linear programming formulation in Figure 1 with that using minimum hop routing. The optimization of the paths increases the network life-

operation	power consumption
transmitting one packet	0.92mJ
receiving one packet	0.69mJ
listening to channel	29.71mJ/sec
operating radio in sleep mode	15 μ J/sec
sampling sensor	1.5 μ J/sample

Table 2: Power consumption of basic operations in Berkeley mica nodes.

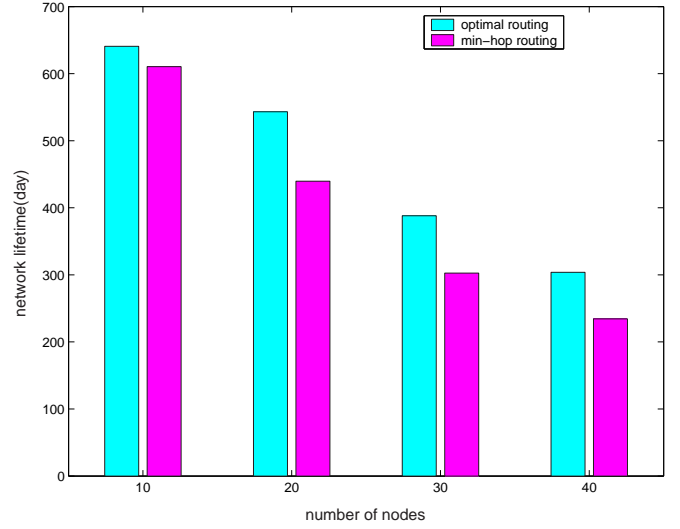


Figure 4: Comparison of the lifetime for optimal and minimum hop routing.

time by 50-150 days. The energy spent for sampling sensor is also included in lifetime calculations to get more realistic estimates. Ignoring [6] or decreasing the energy consumed in sensor will further increase the effect of routing algorithm in the final lifetime estimates.

The goal of the iterative algorithm is to approximate the solution of LP formulation by dividing the complexity into multiple steps of minimum cost path problems. The parameters of the algorithm that affect the battery lifetime of the network are *the type of least cost path algorithm*, *step interval* and *cost function*. *Step interval* is defined to be the length of the time frame during which the same routing paths are used. *Cost function* is important in terms of emphasizing different battery levels at different inten-

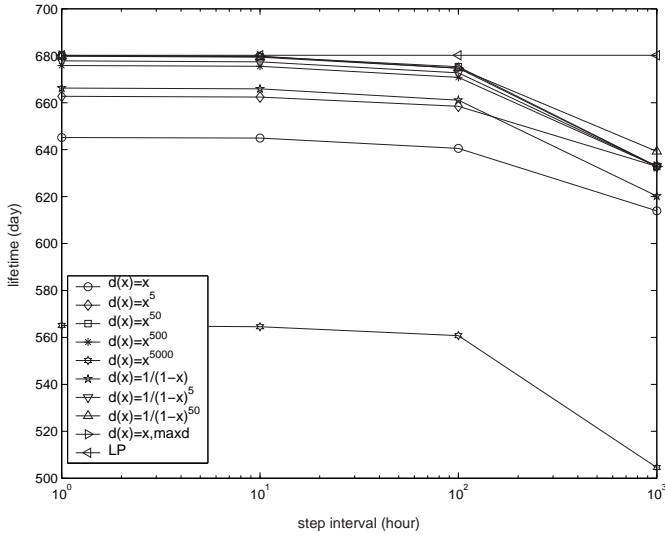


Figure 5: Average battery lifetime of the random configurations of 20 nodes for different cost functions and step intervals.

sities in least sum-cost path algorithm and is defined as $d(x)$ in Section 4.

Figure 5 gives the network lifetime for iterative algorithm. As the step interval increases, the lifetime of the network decreases due to the decreasing number of iterations. For small enough step intervals, the lifetime is almost equal to the optimal lifetime for least max-cost path algorithm whereas it is very close to this optimal value for cost functions $d(x) = x^{50}$ and $d(x) = 1/(1-x)^{50}$ for least sum-cost path algorithm. This suggests that for cost function $d(x) = x^n$ in least sum-cost path algorithm, n should not be chosen too small since the cost function becomes almost linear and it may be hard to differentiate between a path containing one node with small residual energy and a lot of nodes with high residual energy, and a path containing a lot of nodes of medium residual energy. Also, n should not be chosen too large because it is hard to differentiate between different $d(x) = x^n$ values unless x is very close to 1. On the other hand, as n gets larger in cost function $d(x) = 1/(1-x)^n$ for least sum-cost path algorithm, it gets closer to the optimal value since the cost of the path gets closer to taking the maximum of the costs on the path in that case.

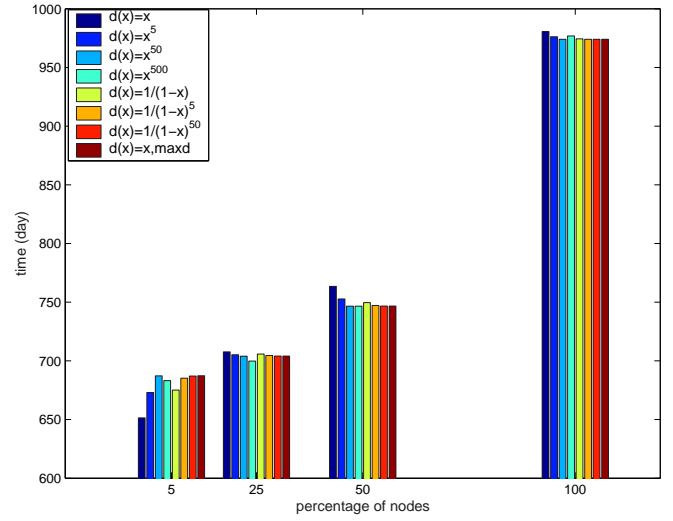


Figure 6: The time at which a specific percentage of the nodes are either dead or disconnected from the AP.

Figure 6 shows the effect of different cost functions on the number of nodes connected to the AP over time. The figure justifies estimating the network lifetime by the time duration until the first node dies since the time duration from the disconnectedness of 5% of the nodes to that of 50% of the nodes is very small. The least max-cost path algorithm and least sum-cost path algorithm with cost function $d(x) = 1/(1-x)^n$ for large n gives the best lifetime estimate in terms of the disconnectedness of a small percentage of the nodes. However, they perform worse than the least sum-cost path algorithms with cost function $d(x) = x^n$ for small n in terms of achieving a large lifetime until a higher percentage of the nodes become disconnected. The reason is that the latter case considers all the nodes on the path whereas the first case considers only the critical nodes with less remaining energy. In the long run, considering only the critical nodes creates cycles in the resulting flow rates causing more energy to be spent in non-critical nodes, which causes the energy of the remaining nodes to deplete earlier than other algorithms.

The simulation for the energy efficient routing with delay guarantee is performed to understand the tradeoff between providing delay guarantee and achieving a high lifetime. In all plots below, ‘max number of levels’ and ‘maximum delay (slot)’ denote d_{max} and $delay_{max}$ re-

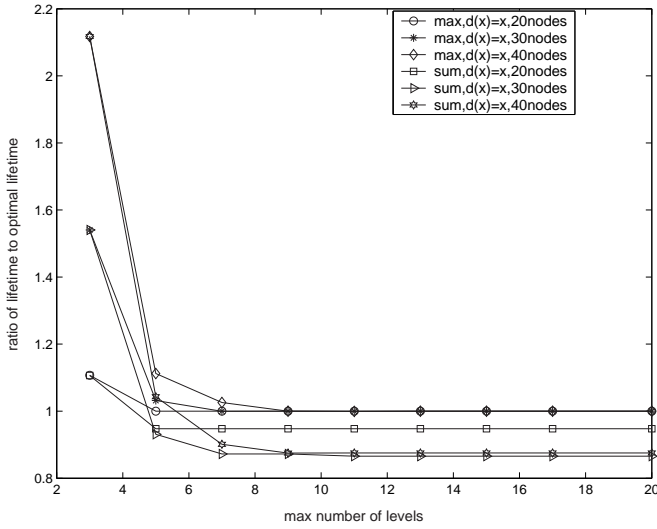


Figure 7: Average battery lifetime of the random configurations of different number of nodes as a function of maximum allowed path length.

spectively, which are defined in Section 5.

Figure 7 shows that the increase in the maximum allowed length of the routing paths beyond the value required for connectivity does not affect the network lifetime for LR-ENR for both least-sum and least-max cost path algorithms for random configurations of different number of nodes. The first decrease in lifetime results from the increase in connectivity of the network. The maximum level used in the network however keeps increasing as the maximum allowed length increases for the same lifetime as shown in Figure 8. This suggests that increasing the delay of the network does not necessarily increase the network lifetime.

Although the maximum level used in routing is higher in least-max cost path algorithms than least-sum cost path algorithms, least-max cost path algorithms achieve a higher lifetime in terms of the death of the first node. Therefore, the following simulations that compare the performance of LR-ENR and HR-ENR in terms of achieving optimal lifetime is performed for least-max cost path algorithms.

Figure 9 shows the lifetime of the network for LR-ENR and HR-ENR and random configurations of different number of nodes. For the maximum allowed delay where

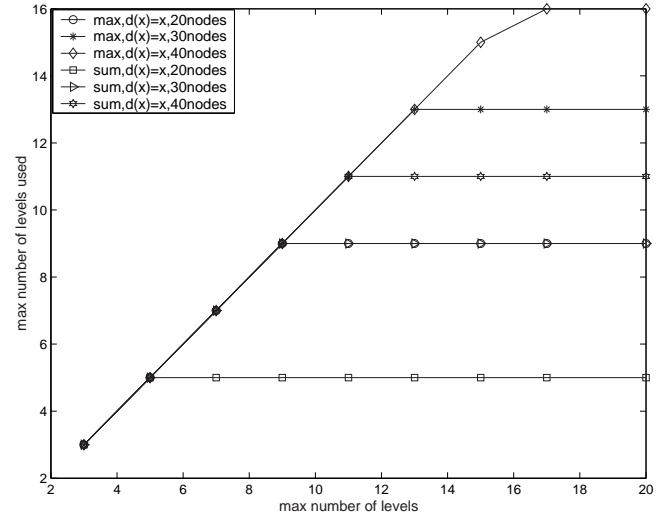


Figure 8: Maximum number of levels used in the routing of the random configurations of different number of nodes as a function of maximum allowed path length.

LR-ENR cannot provide connectivity, HR-ENR provides connectivity of all the nodes and achieves optimal lifetime. At the delay value where the connectivity of all the nodes is achieved, the lifetime is equal to optimal lifetime. This means that the uniform distribution of packets in a uniform topology causes the connectivity and optimal lifetime of the network be achieved simultaneously.

Figure 10 shows the lifetime of the network for the grid configuration of 49 nodes for LR-ENR and HR-ENR. ‘same’ refers to the case where all the nodes generate packets at the same rate whereas ‘diff’ refers to the case where the packet generation rate at one side of the grid is twice that of the other side. For LR-ENR, once the connectivity of the nodes are achieved, the optimal lifetime is also achieved as in the uniform configuration of the nodes. For HR-ENR, although the lifetime is close to the optimal lifetime once all the nodes are connected for the ‘same’, the lifetime increases from 80% to 100% as the maximum allowed delay increases for the ‘diff’ case. This suggests that the non-uniform distribution of the packets in a uniform distribution of the nodes results in achieving connectivity before achieving the optimal lifetime.

Figure 11 shows the lifetime of the network for the ring configuration of 50 nodes for LR-ENR and HR-ENR.

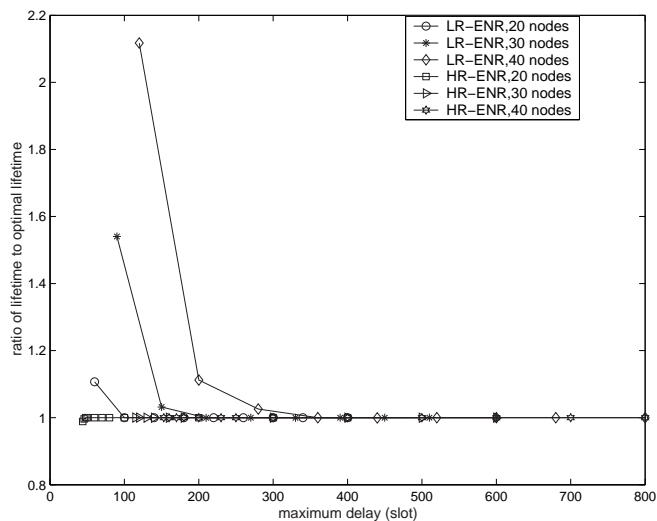


Figure 9: Average battery lifetime of the random configurations of different number of nodes as a function of maximum allowed delay.

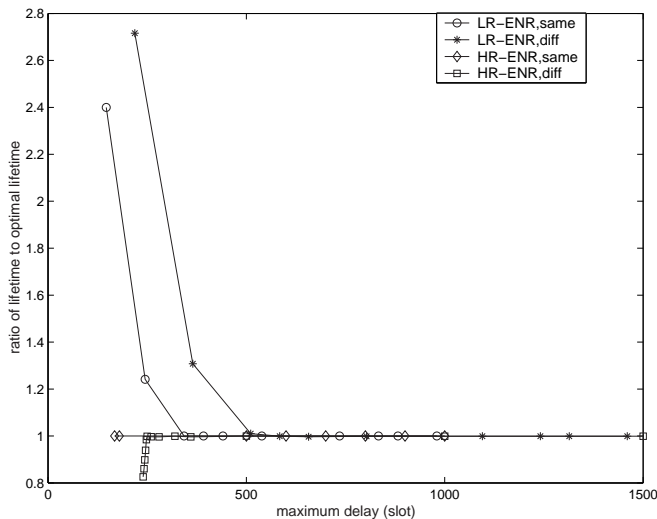


Figure 10: Average battery lifetime of the grid configuration of 49 nodes as a function of maximum allowed delay.

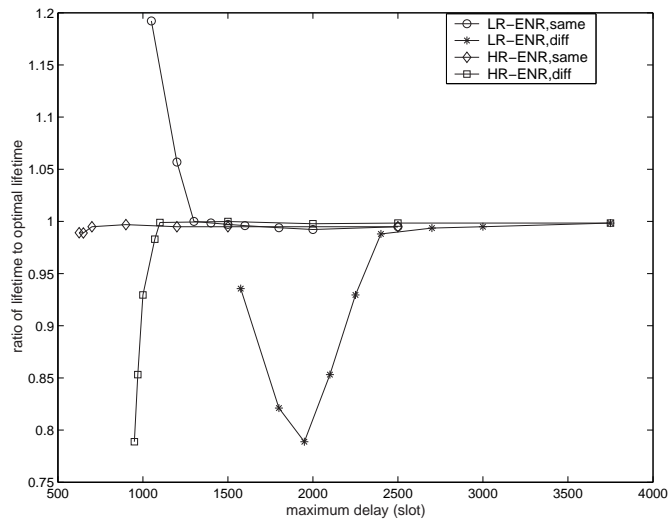


Figure 11: Average battery lifetime of the ring configuration of 50 nodes as a function of maximum allowed delay.

‘same’ refers to the case where all the nodes generate packets at the same rate whereas ‘diff’ refers to the case where the nodes on one side of the ring generate twice as many packets as those on the other side of the ring. In the ‘diff’ case, the lifetime increases from 77% to 100% after the connectivity of the nodes is achieved for both LR-ENR and HR-ENR. There is even a slight increase in the lifetime of ‘HR-ENR, same’ case after the connectivity is achieved. The main feature of ring network is that there are only two path options for each node, which may be of very different lengths for some nodes. The non-uniform distribution of the nodes therefore is another factor for the network lifetime to be below the optimal lifetime despite network connectivity.

When the maximum allowed delay increases, the network delay keeps increasing although the connectivity of all the nodes and optimal lifetime is achieved. To understand the decrease in network performance by not putting any constraint on the network delay, Table 3 compares the minimum and maximum value of the path length and delay values that achieve optimal lifetime and connectivity for LR-ENR and HR-ENR respectively. ‘LR-ENR min’ and ‘LR-ENR max’ correspond to minimum and maximum path length, whereas ‘HR-ENR min’ and ‘HR-ENR max’

correspond to minimum and maximum delay. For random configurations, the difference between them increases as the number of nodes increases for both LR-ENR and HR-ENR. For 40-50 nodes, for random, ring and grid configurations and same or different packet generation rates, the ratio of maximum delay to minimum delay increases up to 2. This ratio is expected to increase as the number of nodes increases.

8 Conclusion

In this paper, we present a routing protocol for sensor networks with the goal of maximizing the time duration until the first node dies. We show that the lifetime can be estimated by the minimum lifetime of the nodes over the network since the time from the disconnectedness of 5% to 50% of the nodes from AP is very small and the quality of data at the AP decreases as a result of the death of the nodes.

We first focus on single path routing. We formulate the path optimization as a Linear Programming (LP) problem in which the objective is to maximize the lifetime of the network. We then give a centralized routing algorithm based on this LP solution. This optimal routing is shown to increase the network lifetime by 50-150 days over the minimum hop routing. We also describe a distributed algorithm based on iterative least cost path routing where the cost of each path is either the sum or the maximum of the cost of the nodes on that path. We show that the least cost path routing for the later achieves optimal lifetime when the cost of each node is given by the ratio of its total consumed energy to its initial energy.

We also modify the energy efficient routing to provide a delay guarantee by limiting the length of the routing paths from each sensor node to the AP. The decrease in battery lifetime as a result of decreasing the maximum allowed delay is shown to be considerable for non-uniform distribution of the nodes and uneven packet generation patterns across the network. We also show that when the maximum allowed delay increases, the network delay keeps increasing although the connectivity of all the nodes and optimal lifetime is achieved. This favors limiting the max-

imum delay at a certain level once the optimal lifetime and connectivity is achieved.

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configuration	LR-ENR min	LR-ENR max	HR-ENR min	HR-ENR max
random, 20 nodes	5	9	48	68
random, 30 nodes	9	13	115	152
random, 40 nodes	9	16	153	264
ring, 50 nodes - same	26	49	625	1177
ring, 50 nodes - diff	32	49	1100	2054
grid, 50 nodes - same	7	7	168	168
grid, 50 nodes - diff	7	17	250	479

Table 3: Minimum and maximum path lengths and delays used for LR-ENR and HR-ENR respectively to achieve optimal lifetime and network connectivity.

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