

EECS140 Midterm 2  
Spring 2017

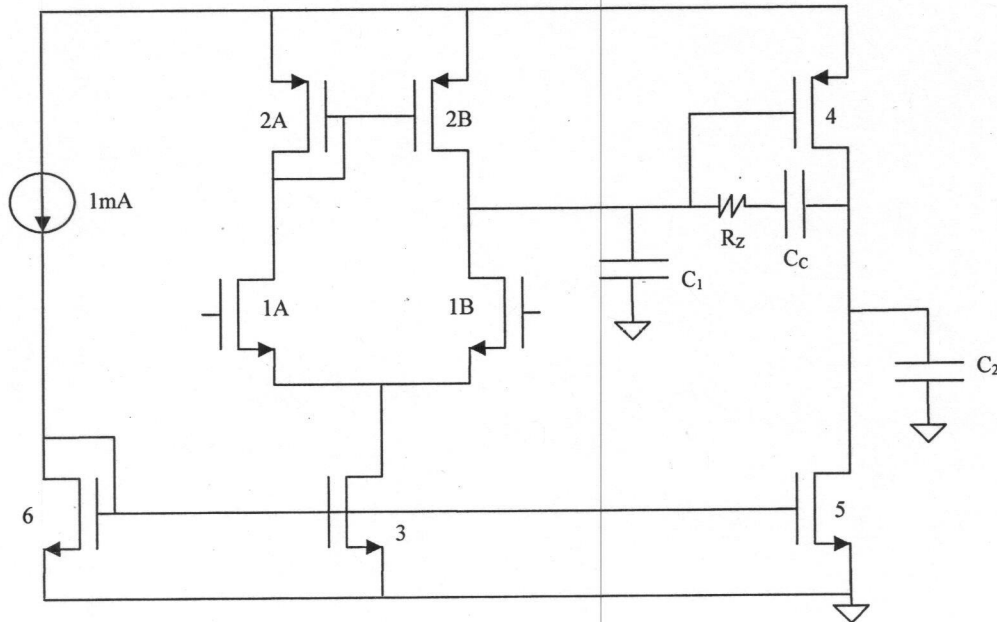
Name Key

SID \_\_\_\_\_

Prob.	Score
1a-e	/10
1f-1	/25
2, 3	/30
4	/15
Total	/80

1) Unless otherwise indicated, you may make the following assumptions:

- All transistors are biased in saturation with  $V_{ov}=0.2V$
- $V_{DD}=3V$ ,  $V_{tn}=1V$ ,  $V_{tp}=-1V$
- M3, and M6 are identical, M5 is 10 times wider
- All capacitors are assumed to be zero except  $C_C$ ,  $C_1$ , and  $C_2$ .



a. What is the common mode input range (min and max)?

$$+1 \text{ min} = 1.4V \quad \text{max} = 2.8V +1$$

b. What is the output swing (min and max)?

$$+1 \text{ min} = 0.2V \quad \text{max} = 2.8V +1$$

c. If  $C_1=0$ ,  $C_2=1 \text{ pF}$ , and  $C_c=1 \text{ pF}$ , what is the positive slew rate?

$$\frac{I_{D3} +1}{C_c} = 10^9 \text{ V/s} +1$$

d. If  $C_1=0$ ,  $C_2=2 \text{ pF}$ , and  $C_c=1 \text{ pF}$ , what is the negative slew rate?

$$\frac{I_{D3} +1}{C_c} = 10^9 \text{ V/s} +1$$

e. If  $C_1=0$ ,  $C_2=1,000 \text{ pF}$ , and  $C_c=1 \text{ pF}$ , what is the negative slew rate?

$$+1 \frac{I_{D5}}{C_2} = \frac{10^{-2}A}{10^{-9}F} = 10^7 \text{ V/s} +1$$

A different amplifier with the same topology has the following parameters. You may ignore the pole/zero doublet from the mirror.

$g_{m1,2}$	$R_{o1}$	$g_{m4}$	$R_{o2}$	$C_1$	$C_C$	$C_2$
1mS	1M	1mS	100k	10p	1p	100p

- f. If  $C_C=0$  (magically we will assume no  $C_{gd4}$  for this part only), what are the uncompensated poles?

$\omega_{p1,u} = 10^5 \frac{\text{rad}}{\text{s}}$	$\omega_{p2,u} = 10^5 \frac{\text{rad}}{\text{s}}$
--	--

On the following pages,

- g. what is the location of the RHZ zero?

$\omega_z = 10^9 \frac{\text{rad}}{\text{s}}$
---

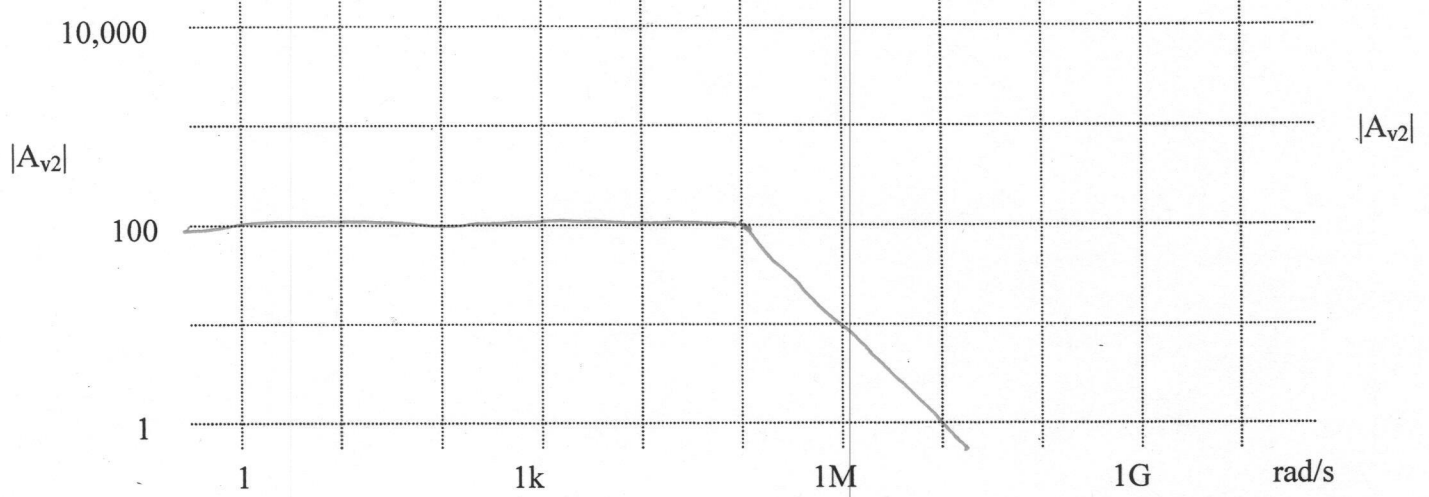
- h. plot the magnitude of the second stage gain  
 i. plot the overall impedance seen at the first stage output (including  $R_{o1}$ ,  $C_1$ ,  $C_C$ , and any effects of Miller multiplication),  
 j. plot the magnitude of the first stage gain,  
 k. plot the magnitude and phase of the overall gain. **Label any poles and zeros clearly.**  
 l. Estimate the phase margin for this value of  $C_C$ .

PM = 0
--------

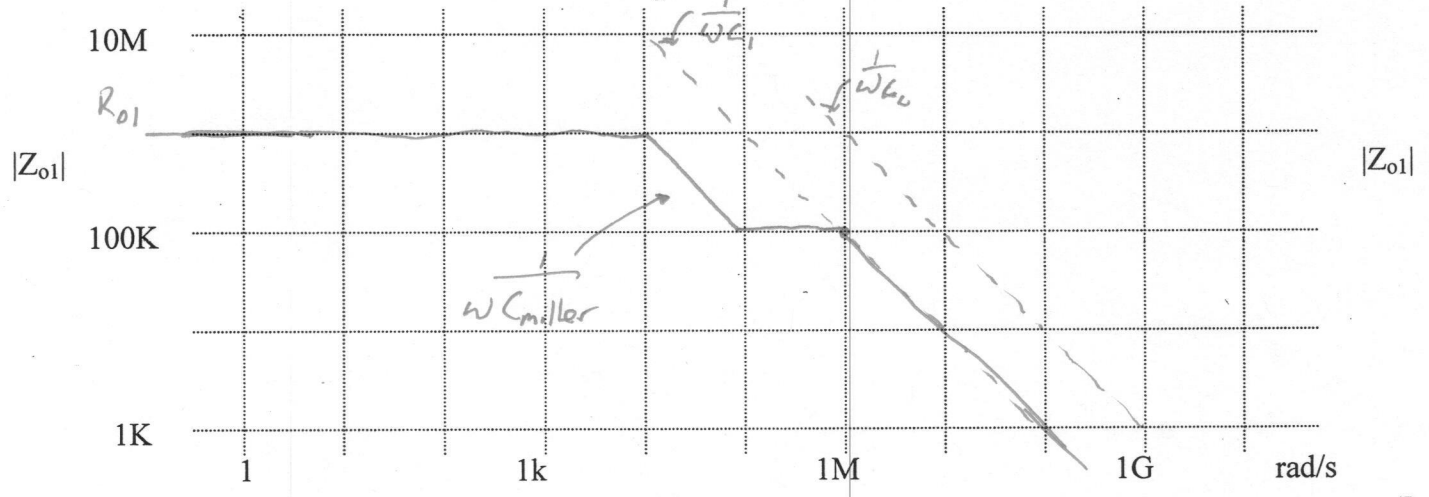
- m. What is the maximum feedback factor and closed loop gain for which the amplifier has a 45 degree phase margin?

$f = 10^{-3}$	$A_{cl} = 10^3$
---------------	-----------------

1h) Second stage gain -  $|A_{v2,0}|$  2

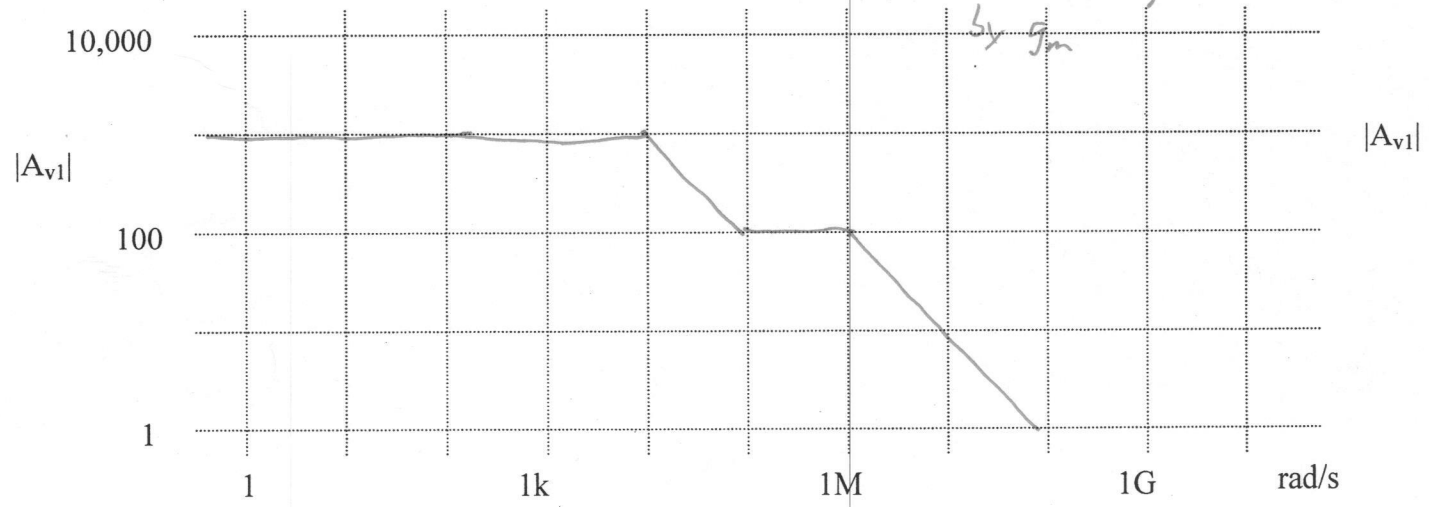


1i) Impedance at first stage output,  $|Z_{o1}|$  4

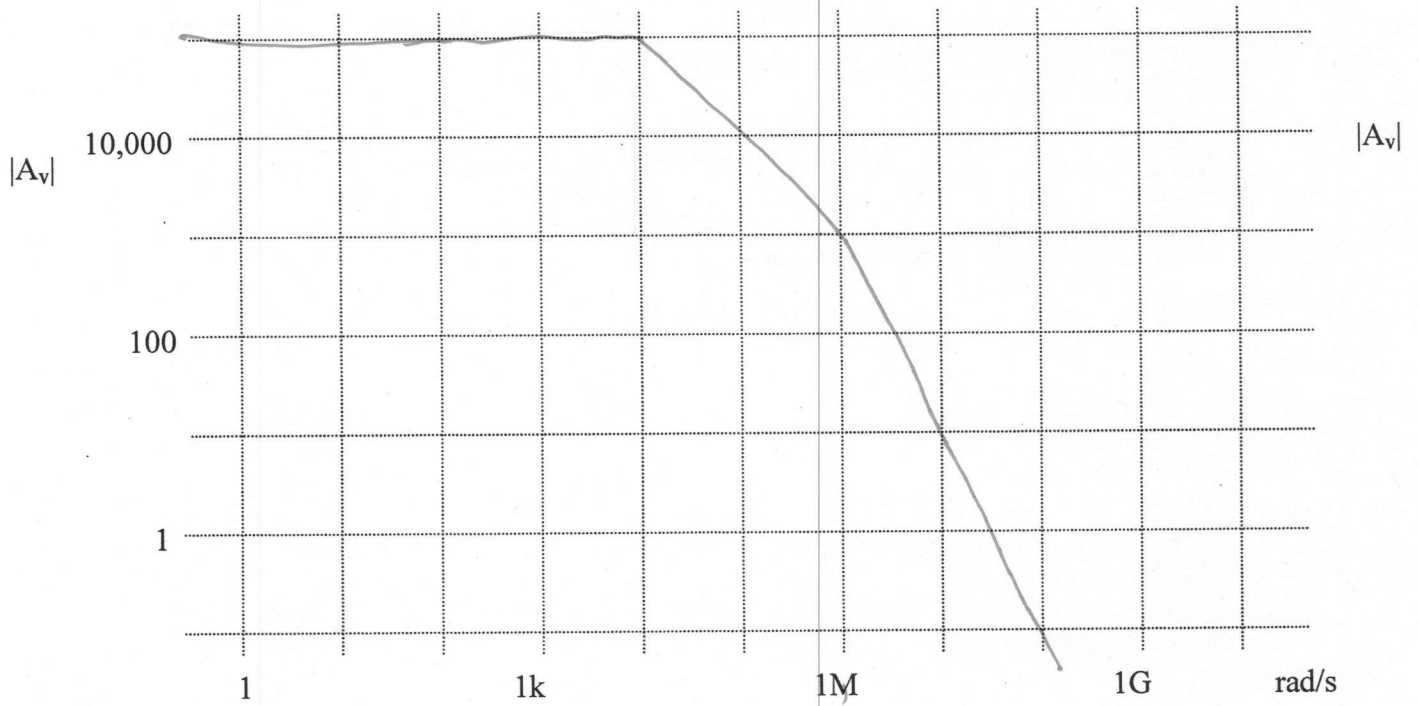


1j) First stage gain,  $|A_{v1}|$

2 pts for multiply whichever is up here by  $g_m$



1kl) op amp Bode plot 5 total

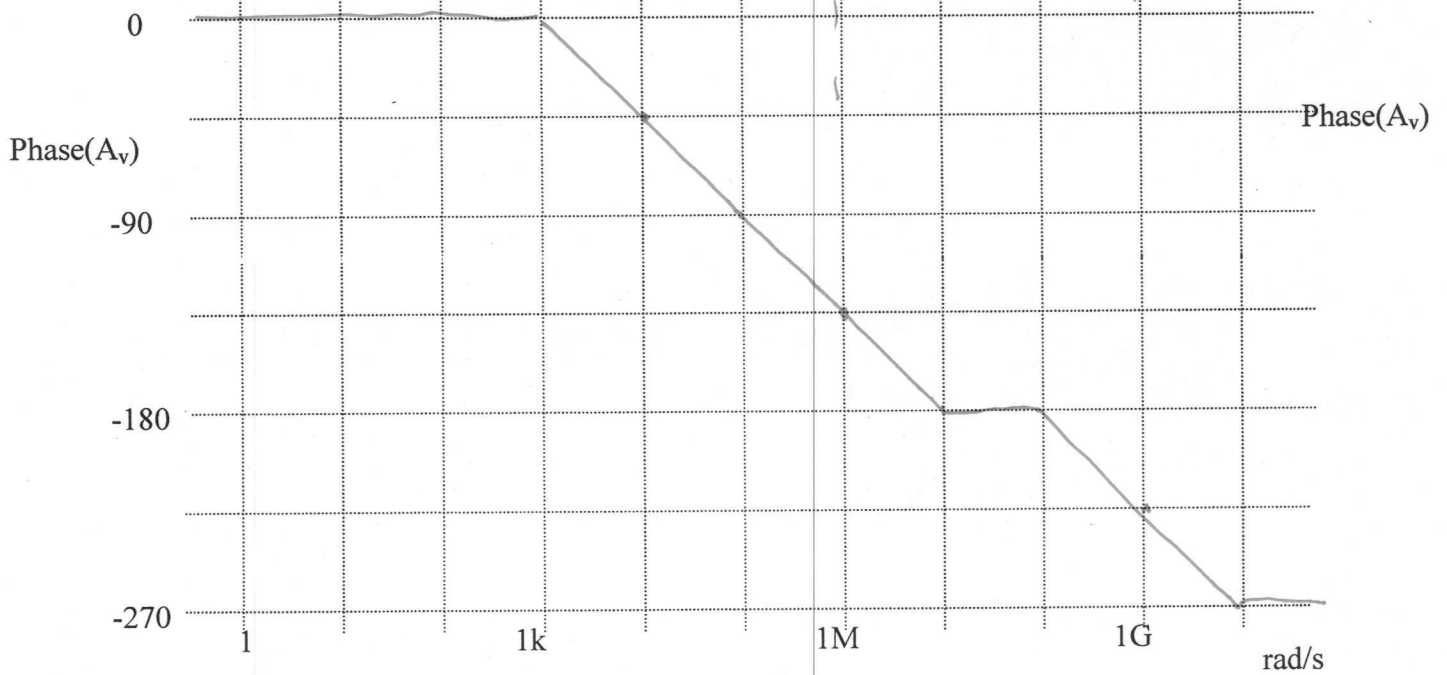


Label any poles and zeros clearly!

$\omega_{p1, z}$

$\omega_{p2, z}$

$\omega_{zRHP}$



2) [8] A single-pole amplifier has a gain of 1,000 and a pole at 1MHz. It is used in feedback with a feedback factor  $f=0.01$ .

a. What is the approximate closed-loop gain,

$$A_{cl} \approx \frac{1}{f} = 100 \text{ V/V}$$

b. percent gain error,

$$\frac{1}{A_{cl}} \times 100\% = -10\%$$

c. closed-loop pole location,

$$f_{cl} = \frac{GBW}{A_{cl}} = 10 \text{ MHz}$$

d. and time constant of the step response?

$$\tau = \frac{1}{\omega_{cl}} = \frac{1}{2\pi \cdot 10^7} \text{ s}$$

3) [22] A particular diode D1 has a saturation current of 1pA, and at 1mA current at room temperature the diode voltage has a temperature coefficient of -2mV/K. You are using copies of this diode to make a bandgap reference as in Lab 4, with D2 composed of seven copies of D1. You can use the approximation that  $\ln(7) \approx 2$ . Assuming that the current in both diodes is maintained at 1mA at room temperature

a. What is the voltage on D1 at room temperature?

$$(9 \text{ decades})(60 \text{ mV/decade}) = 0.54 \text{ V}$$

b. What is the voltage on D2 at room temperature?

$$\ln(7) V_{th} \text{ smaller} \approx 0.49 \text{ V}$$

c. What is the different between the two diode voltages at 200K, 300K, and 400K?

$$300K \approx 52 \text{ mV} \quad 400K \approx 70 \text{ mV}$$

$$200K \approx 35 \text{ mV}$$

d. What is the temperature coefficient of the voltage on D2?

$$-2 \frac{\text{mV}}{\text{K}} - \frac{52 \text{ mV}}{300 \text{ K}} \approx -2.17$$

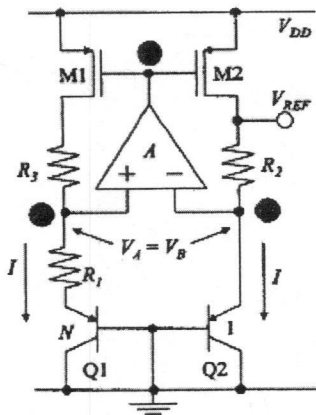
e. Roughly what is the right value for R1?

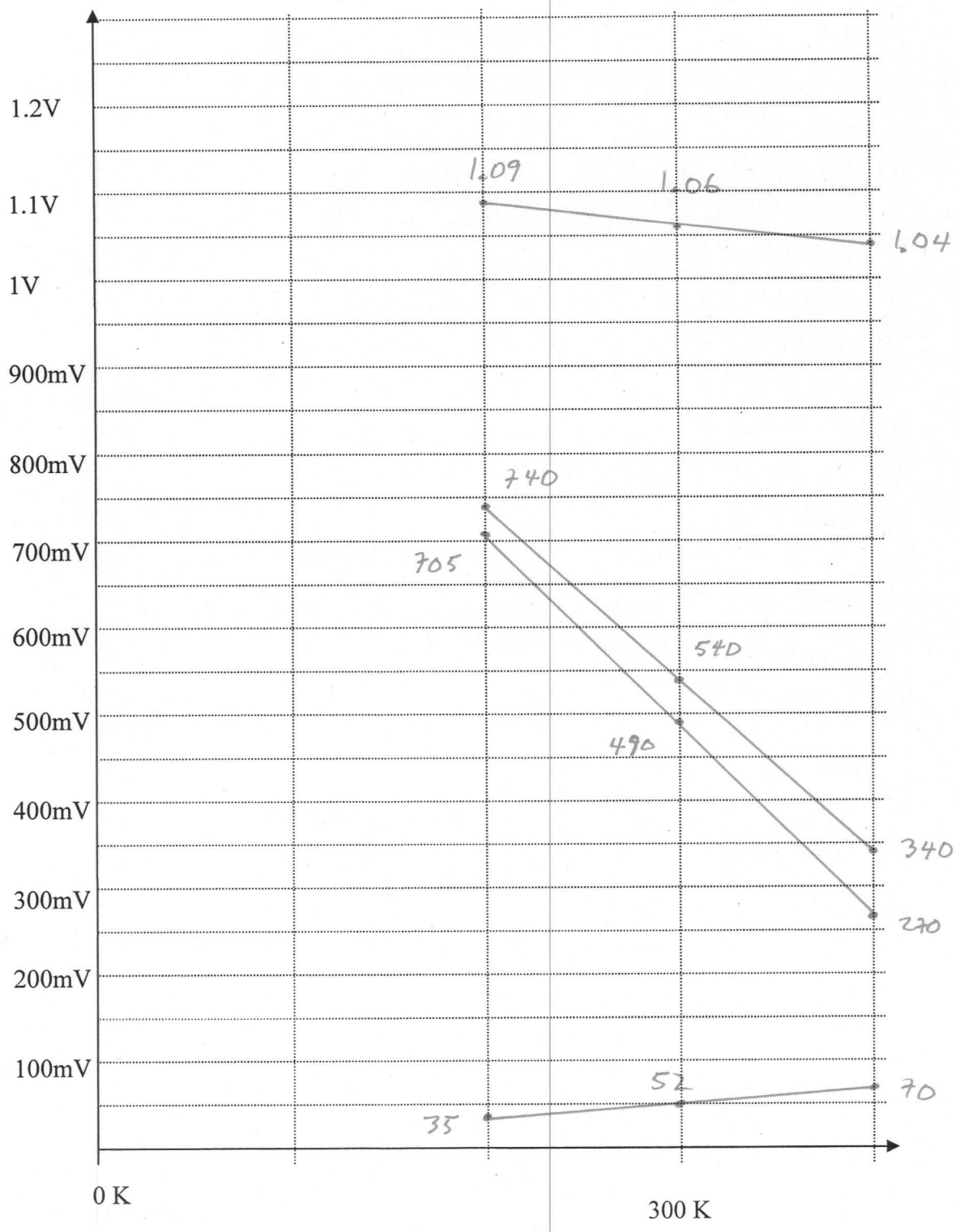
$$\frac{52 \text{ mV}}{1 \text{ mA}} = 52 \Omega$$

f. On the following page, carefully sketch by hand the voltage on D1, the voltage on D2, and the difference between them as a function of temperature from 200K to 400K.

g. On the same plot, if  $R_3=R_2=10 R_1$ , sketch  $V_{ref}$  vs. temperature from 200K to 400K.

} 2 pts  
for each  
line





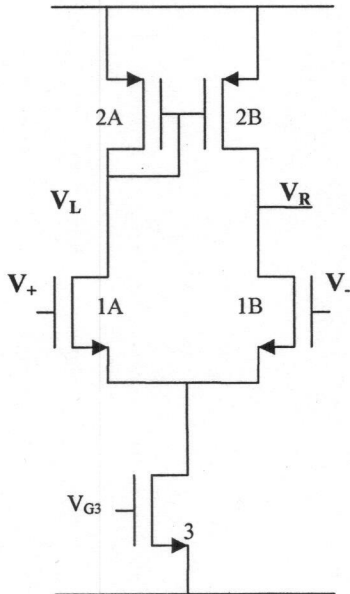
It will help your grade if you draw carefully and label the voltage values of any dots that you draw.

$$10(70) + 340 = 1,040$$

$$10(52) + 540 = 1,060$$

$$10(35) + 740 = 1,090$$

- 4) [15] For the differential amplifier in the figure below, estimate the change in  $V_{TAIL}$ ,  $I_{TAIL}$ ,  $V_L$ , and  $V_R$  due to
- An increase of  $\Delta V$  in both  $V_+$  and  $V_-$
  - An increase of  $\Delta V$  in just  $V_+$
  - An increase of  $\Delta V$  in just  $V_-$
- Give your answers in terms of  $g_{mi}$ ,  $r_{oj}$ , and assume that  $g_m * r_o \gg 1$  for all  $i,j$  combinations.



	$V_{TAIL}$	$I_{TAIL}$	$V_L$	$V_R$
$\Delta V$ in both $V_+$ and $V_-$	$\Delta V$	$\frac{\Delta V}{r_{o3}}$	$\frac{-\Delta V}{2r_{o3}g_{m2}}$	$\frac{-\Delta V}{2r_{o3}g_{m2}}$
$\Delta V$ in just $V_+$	$\Delta V/2$	$\frac{\Delta V}{2r_{o3}}$	$-\frac{\Delta V g_{m1}}{2} \cdot \frac{1}{g_{m2}}$	$\Delta V g_{m1} r_{o1} // r_{o2}$
$\Delta V$ in just $V_-$	$\Delta V/2$	$\frac{\Delta V}{2r_{o3}}$	$\frac{\Delta V g_{m1}}{2} \cdot \frac{1}{g_{m2}}$	$-\Delta V g_{m1} r_{o1} // r_{o2}$

+1 each box

+1 for correct signs in each row