CS61C - Machine Structures  
Lecture 19 - Virtual Memory  

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Review (1/2)  
° Caches are NOT mandatory:  
  • Processor performs arithmetic  
  • Memory stores data  
  • Caches simply make things go faster  
° Each level of memory hierarchy is just a subset of next higher level  
° Caches speed up due to temporal locality: store data used recently  
° Block size > 1 word speeds up due to spatial locality: store words adjacent to the ones used recently  

Review (2/2)  
° Cache design choices:  
  • size of cache: speed v. capacity  
  • direct-mapped v. associative  
  • for N-way set assoc: choice of N  
  • block replacement policy  
  • 2nd level cache?  
  • Write through v. write back?  
° Use performance model to pick between choices, depending on programs, technology, budget, ...

Another View of the Memory Hierarchy  

Virtual Memory  
° If Principle of Locality allows caches to offer (usually) speed of cache memory with size of DRAM memory, then recursively why not use at next level to give speed of DRAM memory, size of Disk memory?  
° Called "Virtual Memory"  
  • Also allows OS to share memory, protect programs from each other  
  • Today, more important for protection vs. just another level of memory hierarchy  
  • Historically, it predates caches

Virtual to Physical Addr. Translation  
° Each program operates in its own virtual address space; only program running  
° Each is protected from the other  
° OS can decide where each goes in memory  
° Hardware (HW) provides virtual -> physical mapping
Simple Example: Base and Bound Reg

User A

$base

User B

$base+ $bound

User C

$base+

Want discontinuous mapping

Process size >> mem

Addition not enough!

=> use Indirection!

Enough space for User D, but discontinuous
("fragmentation problem")

Mapping Virtual Memory to Physical Memory

* Divide into equal sized chunks (about 4KB)
* Any chunk of Virtual Memory assigned to any chunk of Physical Memory ("page")

Paging Organization (assume 1 KB pages)

Physical Address

<table>
<thead>
<tr>
<th>Virtual Address</th>
<th>Page is unit of mapping</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>page 0</td>
</tr>
<tr>
<td>1024</td>
<td>page 1</td>
</tr>
<tr>
<td>...</td>
<td>...</td>
</tr>
<tr>
<td>7168</td>
<td>page 7</td>
</tr>
</tbody>
</table>

Virtual Memory Mapping Function

* Cannot have simple function to predict arbitrary mapping
* Use table lookup of mappings

Virtual Memory Mapping Function

<table>
<thead>
<tr>
<th>Page Number</th>
<th>Offset</th>
</tr>
</thead>
</table>

Address Mapping: Page Table

Virtual Address:

Page Table Base Reg

Index into page table

Page Table located in physical memory

Address Mapping: Page Table

Page Table

Physical Memory Address

Page Table

V, A.R., P.P.A., Val, Access, Physical Address

State of process is PC, all registers, plus page table

OS changes page tables by changing contents of Page Table Base Register

Page Table

A page table is an operating system structure which contains the mapping of virtual addresses to physical locations

Each process running in the operating system has its own page table

"State" of process is PC, all registers, plus page table

OS changes page tables by changing contents of Page Table Base Register
Page Table Entry (PTE) Format
° Contains either Physical Page Number or indication not in Main Memory
° OS maps to disk if Not Valid (V = 0)

Page Table

Val | Access Rights | Physical Page Number
V   | A.R.          | P.P.N.

° If valid, also check if have permission to use page: Access Rights (A.R.) may be Read Only, Read/Write, Executable

Analogy
° Book title like virtual address
° Library of Congress call number like physical address
° Card catalogue like page table, mapping from book title to call number
° On card for book, in local library vs. in another branch like valid bit indicating in main memory vs. on disk
° On card, available for 2-hour in library use (vs. 2-week checkout) like access rights

Address Map, Mathematically Speaking
V = {0, 1, ..., n - 1} virtual address space (n > m)
M = {0, 1, ..., m - 1} physical address space
MAP: V --> M \{0\} address mapping function
MAP(a) = a' if data at virtual address a is present in physical address a' and a' in M = e if data at virtual address a is not present in M

Comparing the 2 levels of hierarchy
° Cache Version Virtual Memory vers.
° Block or Line Page
° Miss Page Fault
° Block Size: 32-64B Page Size: 4K-8KB
° Placement: Direct Mapped, N-way Set Associative
° Replacement: Least Recently Used LRU or Random (LRU)
° Write Thru or Back Write Back

Administrivia
° Project 5 due Saturday midnight
° TA help Friday, not Saturday
° Homework 8 (next week)
° Want to fill in page tables to learn material, so easiest way is to turn in paper; no electronic submission
° Grading scale (same as Spring 99, Fall 99)
  95% A+, 90% A, 85% A-, 80% B+, 75% B, 70% B-, 65% C+, 60% C, 55% C-, 45% D

% perfect or -1 point per question
1. Pliable Data 28% 75%
2. Parts of a Computer 89% 98%
3. Starting a Program 86% 100%
4. Networks 36% 51%
5. Pointers (p's and q's) 3% 20%
6. Floating Point 55% 77%
7. MIPS (self mod. Code) 27% 32%
8. Pointers in C and MIPS 51% 57%
Notes on Page Table
- Solves Fragmentation problem: all chunks same size, so all holes can be used
- OS must reserve "Swap Space" on disk for each process
- To grow a process, ask Operating System
  - If unused pages, OS uses them first
  - If not, OS swaps some old pages to disk
  - (Least Recently Used to pick pages to swap)
- Each process has own Page Table
- Will add details, but Page Table is essence of Virtual Memory

Virtual Memory Problem #1
- Not enough physical memory!
  - Only, say, 64 MB of physical memory
  - N processes, each 4GB of virtual memory!
  - Could have 1K virtual pages/physical page!
- Spatial Locality to the rescue
  - Each page is 4 KB, lots of nearby references
  - No matter how big program is, at any time only accessing a few pages
  - "Working Set": recently used pages

Virtual Address and a Cache
- Cache typically operates on physical addresses
  - Page Table access is another memory access for each program memory access!
  - Need to fix this!

Virtual Memory Problem #2
- Map every address $\Rightarrow$ 1 extra memory access for every memory access
- Observation: since locality in pages of data, must be locality in virtual addresses of those pages
- Why not use a cache of virtual to physical address translations to make translation fast? (small is fast)
- For historical reasons, cache is called a Translation Lookaside Buffer, or TLB

Typical TLB Format
- TLB just a cache on the page table mappings
- TLB access time comparable to cache (much less than main memory access time)
  - Dirty: since use write back, need to know whether or not to write page to disk when replaced

What if not in TLB?
- Option 1: Hardware checks page table and loads new Page Table Entry into TLB
- Option 2: Hardware traps to OS, up to OS to decide what to do
- MIPS follows Option 2: Hardware knows nothing about page table format
TLB Miss (simplified format)

- If the address is not in the TLB, MIPS traps to the operating system
  - When in the operating system, we don’t do translation (turn off virtual memory)
- The operating system knows which program caused the TLB fault, page fault, and knows what the virtual address desired was requested
  - So we look the data up in the page table

<table>
<thead>
<tr>
<th>valid</th>
<th>virtual</th>
<th>physical</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>2</td>
<td>9</td>
</tr>
</tbody>
</table>

If the data is in memory

- We simply add the entry to the TLB, evicting an old entry from the TLB

<table>
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</table>

What if the data is on disk?

- We load the page off the disk into a free block of memory, using a DMA transfer
  - Meantime we switch to some other process waiting to be run
- When the DMA is complete, we get an interrupt and update the process’s page table
  - So when we switch back to the task, the desired data will be in memory

What if we don’t have enough memory?

- We chose some other page belonging to a program and transfer it onto the disk if it is dirty
  - If clean (other copy is up-to-date), just overwrite that data in memory
  - We chose the page to evict based on replacement policy (e.g., LRU)
  - And update that program’s page table to reflect the fact that its memory moved somewhere else

Translation Look-Aside Buffers

- TLBs usually small, typically 128 - 256 entries
- Like any other cache, the TLB can be fully associative, set associative, or direct mapped

Virtual Memory Problem #3

- Page Table too big!
  - 4GB Virtual Memory ÷ 4 KB page ⇒ ~ 1 million Page Table Entries ⇒ 4 MB just for Page Table for 1 process, 25 processes ⇒ 100 MB for Page Tables!
- Variety of solutions to tradeoff memory size of mapping function for slower when miss TLB
  - Make TLB large enough, highly associative so rarely miss on address translation
  - CS 162 will go over more options and in greater depth
2-level Page Table

- Physical Memory: 64 MB
- Virtual Memory: ∞
- Code
- Static
- Heap
- Stack
- 0

Page Table Shrink:

- Single Page Table
  - Page Number
  - Offset
  - 20 bits
  - 12 bits

- Multilevel Page Table
  - Super Page No.
  - Page Number
  - Offset
  - 10 bits
  - 10 bits
  - 12 bits

- Only have second level page table for valid entries of super level page table

Space Savings for Multi-Level Page Table

- If only 10% of entries of Super Page Table have valid entries, then total mapping size is roughly 1/10-th of single level page table
- Exercise 7.35 explores exact size

Note: Actual MIPS Process Memory Allocation

- Address
- I/O Regs
- OS code/data space
- OS restricts I/O Registers, Exception Handlers to OS
- User code/data space
- Exception Handlers
- Stack
- Heap
- Static
- Code
- $sp
- $gp

Things to Remember 1/2

- Apply Principle of Locality Recursively
- Reduce Miss Penalty? Add a (L2) cache
- Manage memory to disk? Treat as cache
  - Included protection as bonus, now critical
  - Use Page Table of mappings vs. tag/data in cache
- Virtual memory to Physical Memory Translation too slow?
  - Add a cache of Virtual to Physical Address Translations, called a TLB

Things to Remember 2/2

- Virtual Memory allows protected sharing of memory between processes with less swapping to disk, less fragmentation than always swap or base/bound
- Spatial Locality means Working Set of Pages is all that must be in memory for process to run fairly well
- TLB to reduce performance cost of VM
- Need more compact representation to reduce memory size cost of simple 1-level page table (especially 32- → 64-bit address)
- Next: Introduction to processors design