

# DOUBLE LAYER FORMATION IN A TWO REGION ELECTRONEGATIVE DISCHARGE

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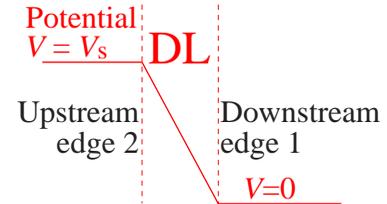
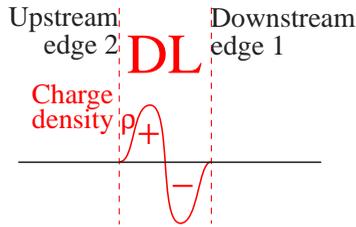
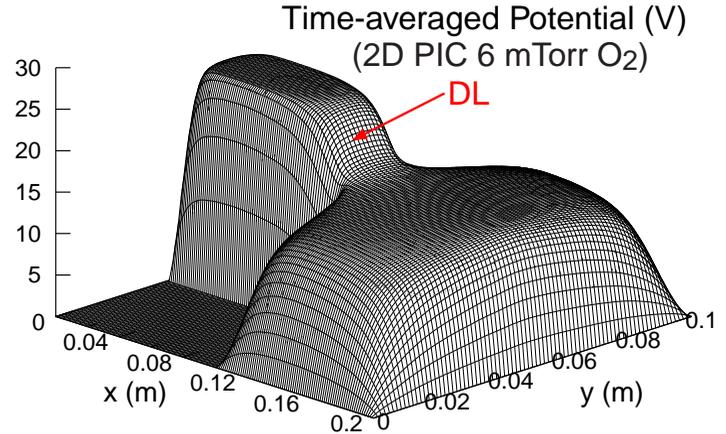
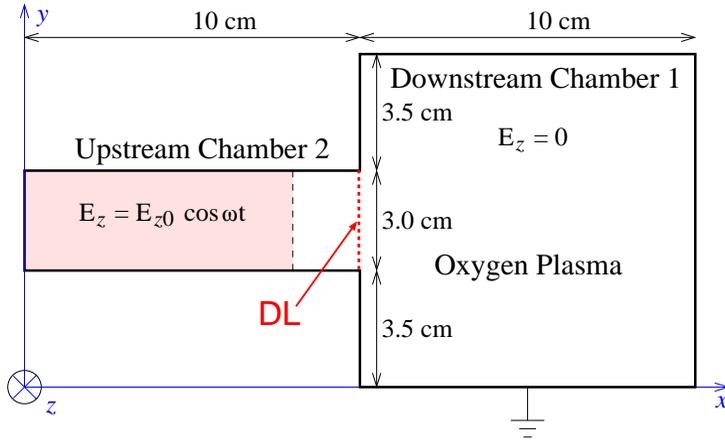
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# OUTLINE

- Introduction
- “Experiments”
  - 2D particle-in-cell (PIC) simulations with rescaled oxygen cross sections
- Theory
  - 1D collisionless model of double layer (DL)
  - Global (volume-averaged) model of upstream and downstream particle and energy balances
- Comparisons
  - Reasonable agreement but also some differences
- Slow and fast wave instabilities
  - The DL has time-varying structure

# INTRODUCTION



- Why does a DL form at low pressures?
  - The particle loss rate is greater upstream than downstream due to the smaller upstream radius
  - A higher ionization rate (and  $T_e$ ) is needed upstream than downstream
  - A DL both “insulates” the low downstream  $T_e$  from the high upstream  $T_e$ , and it accelerates electrons upstream to increase the ionization rate there

# “EXPERIMENTS”

# PIC SIMULATION METHOD

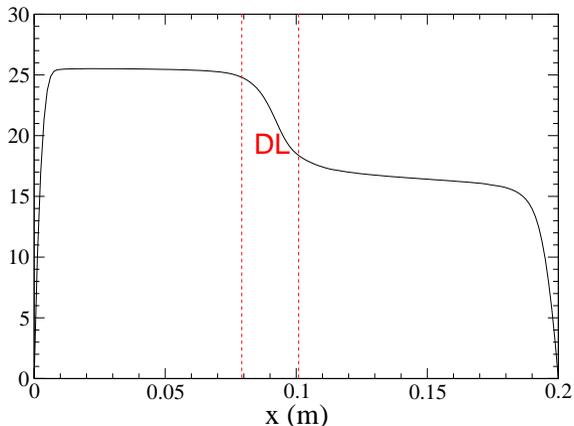
- Self-consistent results from first principles with no assumptions about electron and ion velocity distributions
- Upstream heating at 13.56 MHz  $\perp$  to the plane of the simulation
- RF field adjusted to keep number of upstream electrons constant
- Stability, speed and accuracy require small plasma reactors with low densities and large Debye lengths:

$$n_e \approx 4 \times 10^{14} \text{ m}^{-3}, \lambda_D \approx 0.8 \text{ mm}$$

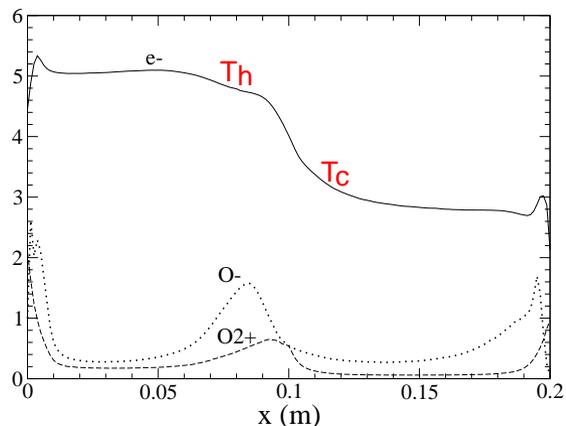
- Due to low densities, rescaled oxygen cross sections were used:  
Positive-negative ion recombination  $\uparrow \times 20$   
Dissociative attachment  $\uparrow \times 5$
- A typical simulation takes 1–2 weeks
- The pressure range explored is 0.5–24 mTorr
- No DL was observed at 0.5 mTorr

# PIC RESULTS FOR 6 mTorr O<sub>2</sub> DISCHARGE

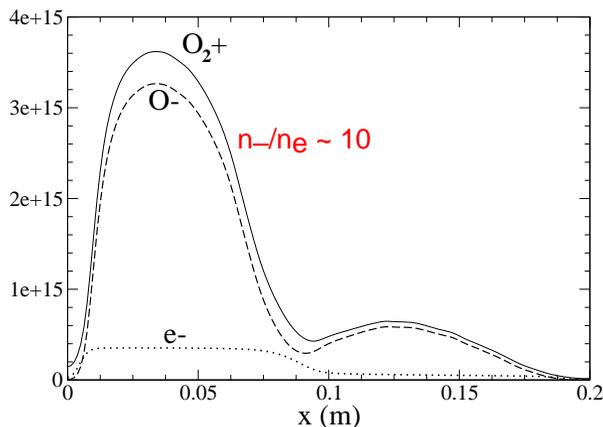
Axial Potential (V)



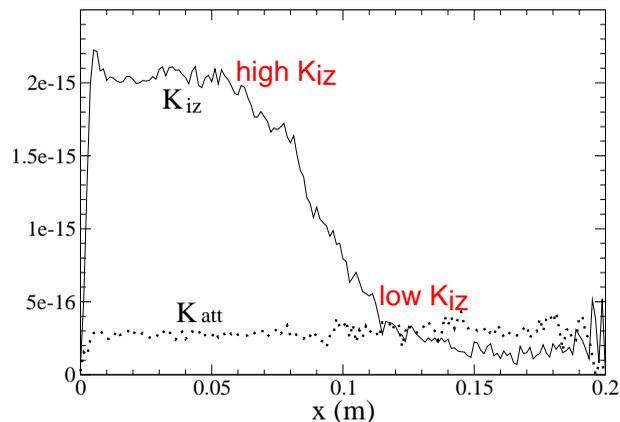
Radially averaged T (V)



Axial Density (m<sup>-3</sup>)

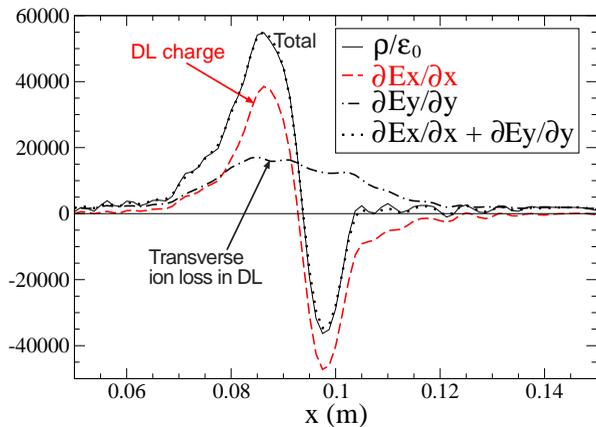


Axial Collision Rates (m<sup>3</sup>/s)

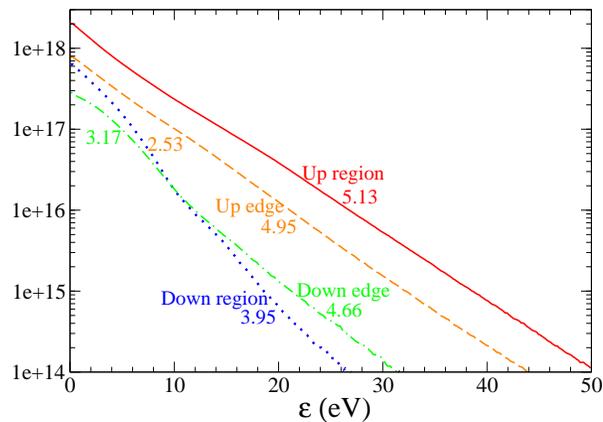


# RESULTS FOR 6 mTorr O<sub>2</sub> DISCHARGE (CONT'D)

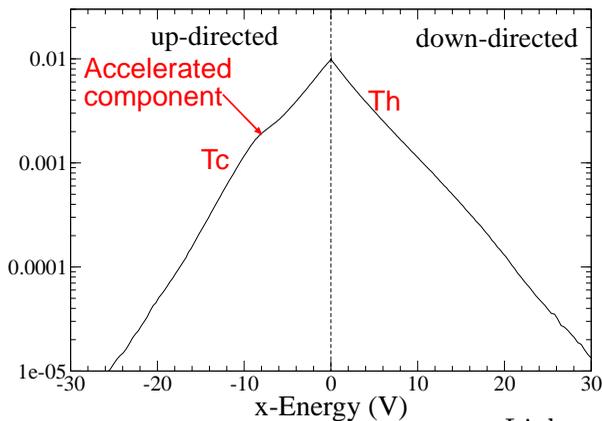
Charge Density Components in DL (V/m<sup>2</sup>)



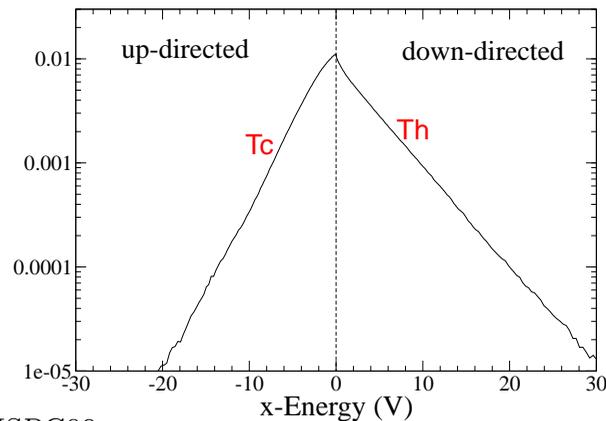
EEDF (a.u.)



Up edge x-component EEDF (a.u.)



Down-edge x-component EEDF (a.u.)



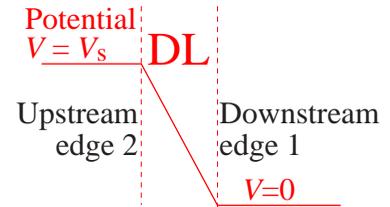
# THEORY

# DL MODEL

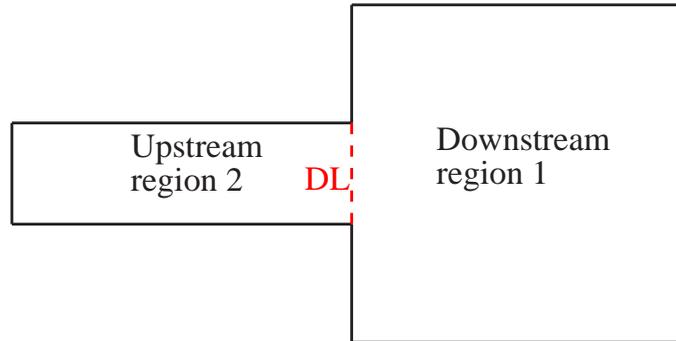
- Charge density  $\rho$  and potential  $V$  within the DL are found by solving Poisson's equation
- Six types of particles contribute to  $\rho$ :
  - thermal positive ions, negative ions, and electrons
  - accelerated positive ions, negative ions, and electrons
- The particle motions are 1D and collisionless
- The boundary conditions are that  $\rho$  and  $d\rho/dV$  vanish at the DL edges
- An additional condition is that the sum of positive and negative charge in the double layer must vanish; equivalently, the total force acting on the double layer must vanish

$$\int_0^{V_s} \rho(V) dV = 0$$

- A final condition that upstream and downstream-directed electron fluxes nearly balance determines the equilibrium value of  $V_s/T_h$ .



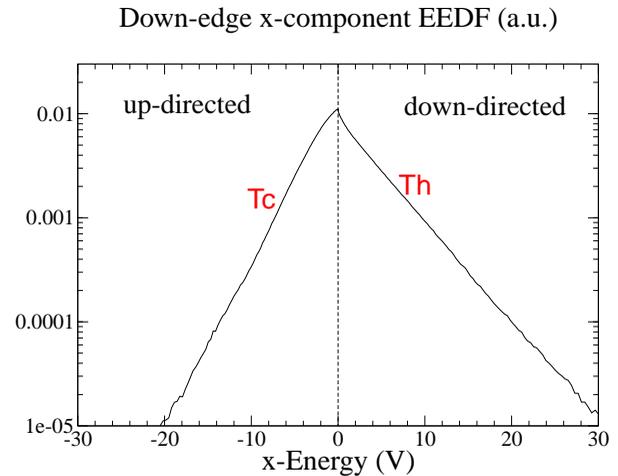
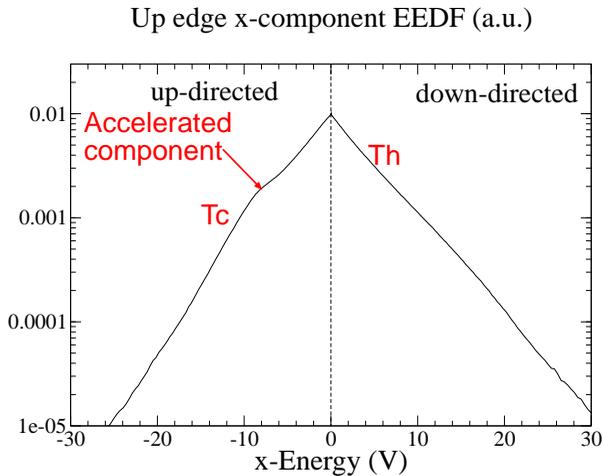
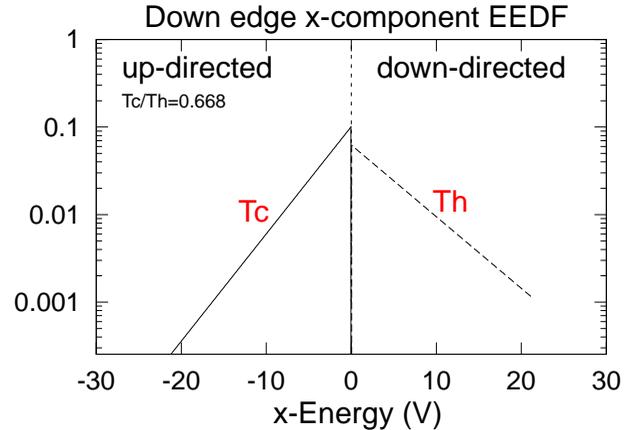
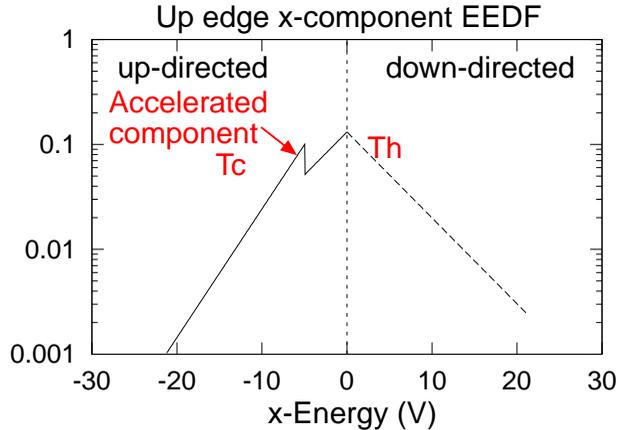
# PARTICLE AND ENERGY BALANCES



- We use a 2D rectangular geometry
- To determine the equilibrium quantities we use
  - global particle balance upstream
  - global particle balance downstream
  - global energy balance downstream
- Upstream energy balance (which determines the upstream electron density) depends on the input power, and is beyond the scope of this study

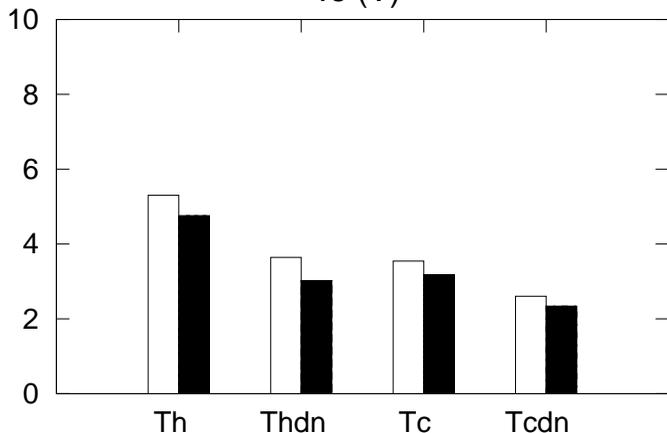
# COMPARISONS

# MODEL (TOP) and PIC (BOTTOM) EEDF'S (6 mTorr O<sub>2</sub>)

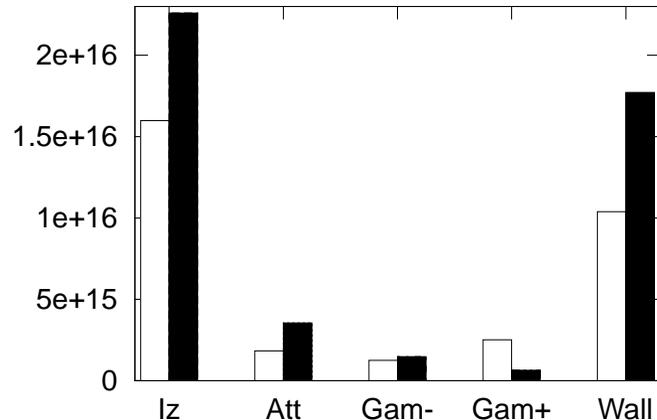


# MODEL (WHITE) AND PIC (BLACK) FOR 6 mTorr O<sub>2</sub>

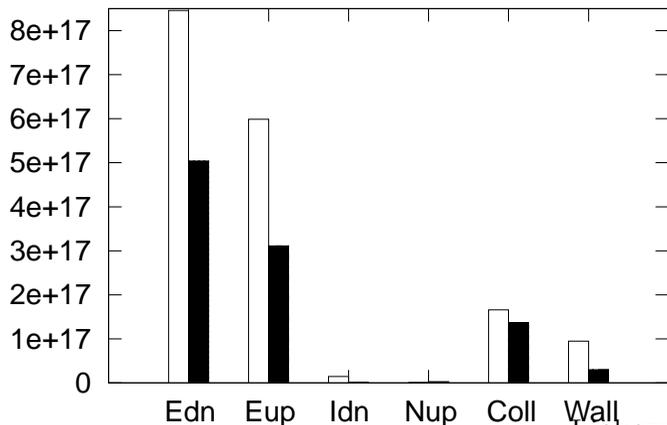
Te (V)



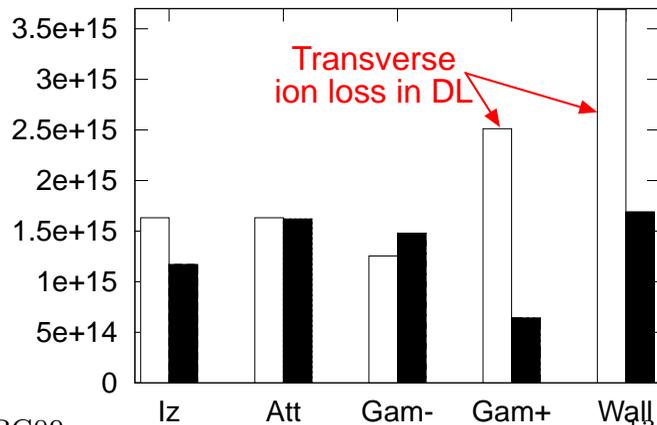
Up elec bal (#/s)



Down energy bal (eV/s)

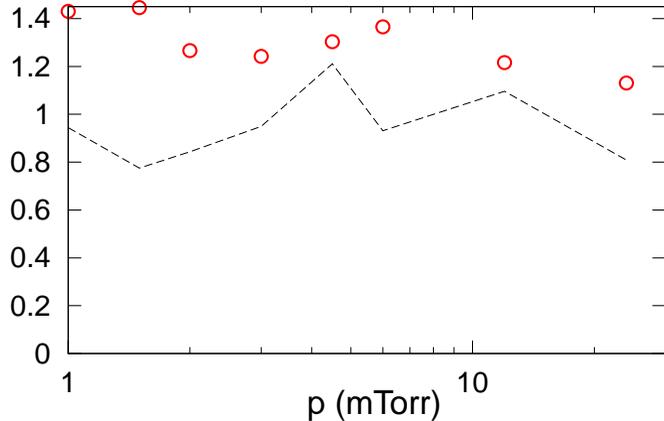


Down elec balance (#/s)

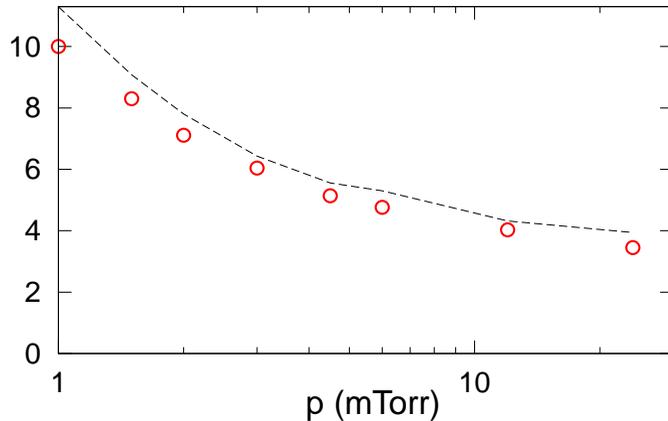


# MODEL (DASH) AND PIC (CIRCLES) VS PRESSURE

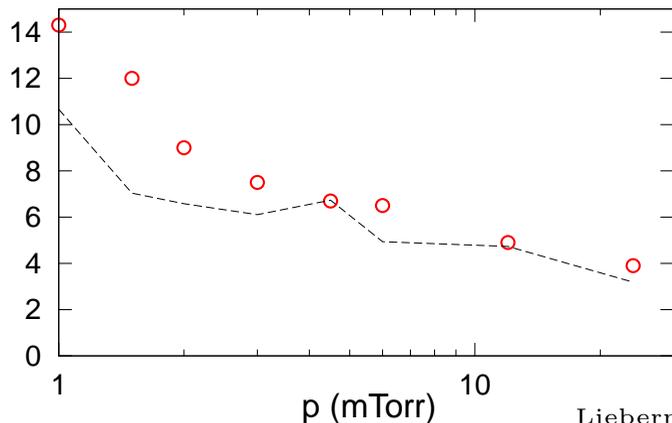
Vs/Th



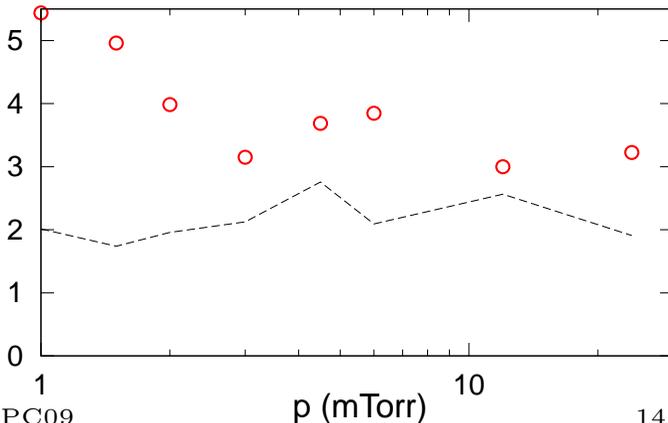
Th (V)



Vs (V)



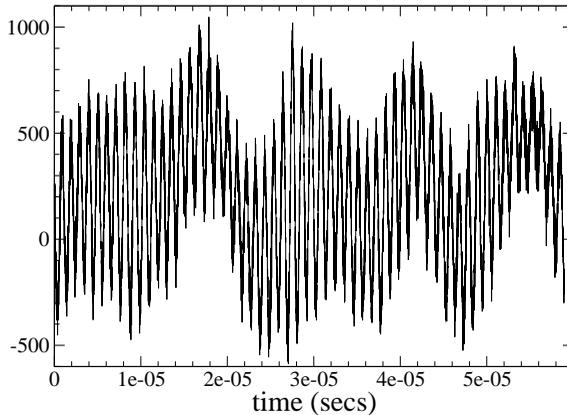
ne2/ne1



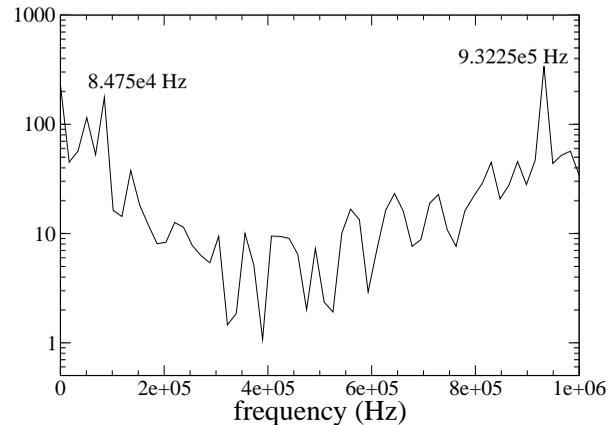
# TIME-VARYING PHENOMENA

# SLOW AND FAST WAVE INSTABILITIES (6 mTorr O<sub>2</sub>)

Ex(t) at x=10 cm (dn DL edge)  
time interval = 59 microseconds



FFT of Ex(t) at x = 10 cm (dn DL edge)

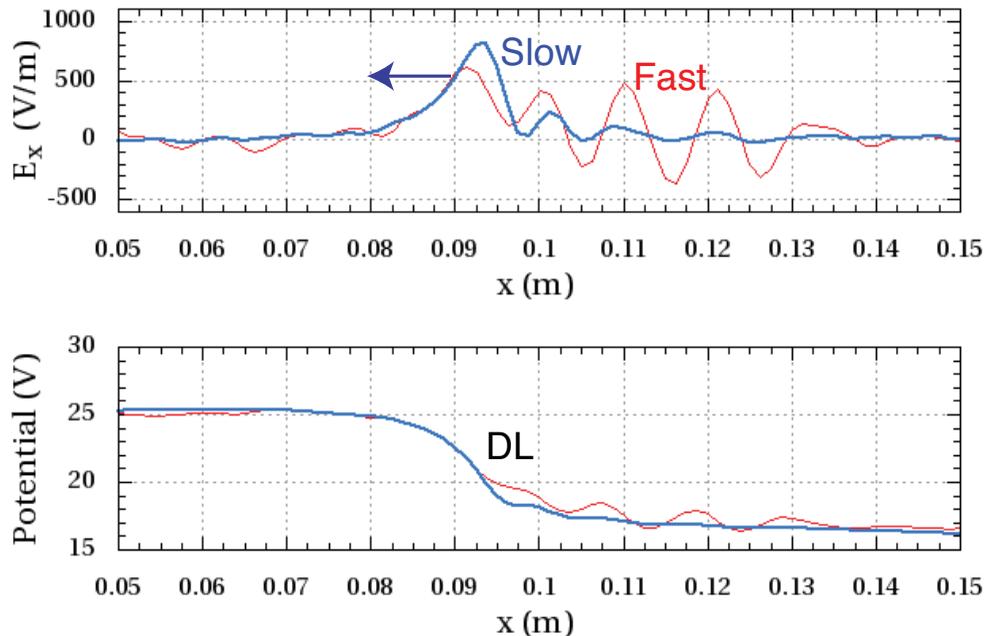


- At 2–12 mTorr, the DL coexists with an unstable slow wave that originates downstream and propagates upstream as it grows
- The wave frequency is 50–100 kHz with a wavelength of order 1 cm
- The wave produces  $\sim 20\%$  oscillations in the double layer potential and  $\sim 0.5$  cm oscillations in the DL position
- We believe the wave is driven by counter-streaming flows of positive and negative ions (Tuszewski and Gary, 2003)
- There is an additional unstable fast wave at higher pressures having frequency of order 1 MHz and a wavelength of order 1 cm

# MOVIE SHOWING SLOW AND FAST WAVES

Red solid line: fast waves averaged over  $0.1475 \mu\text{s}$  intervals  
Blue solid line: slow waves averaged over  $1.18 \mu\text{s}$  intervals

160. Waves in 6 mTorr DL region (23.6 microseconds)



# CONCLUSIONS

- 2D PIC simulations can be powerful tools to study the physics of double layer formation
- The simulations provide diagnostics **at the edges and inside the DL**, which would be very difficult to do in a laboratory experiment
- The simulations show upstream edge Maxwellian electrons **along with an accelerated component**, and a downstream edge bi-Maxwellian with a hotter tail tied to the upstream temperature
- The simulations show that the DL can coexist with unstable slow and fast wave-driven oscillations
- A 1D analytical DL model coupled with global models of the upstream and downstream particle and energy balance captures the essential physics of DL formation in this two-region system

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