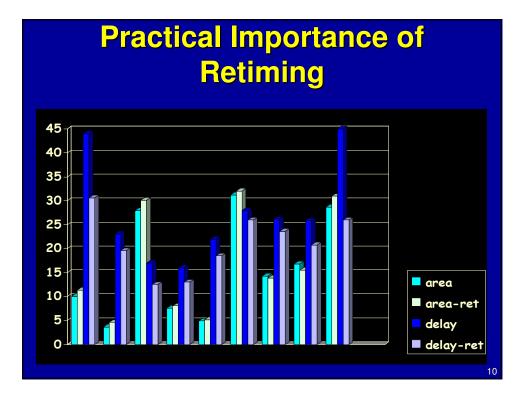
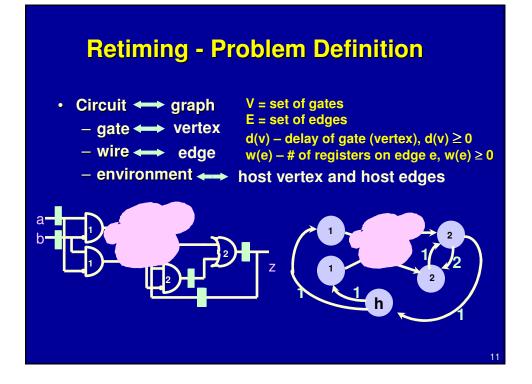
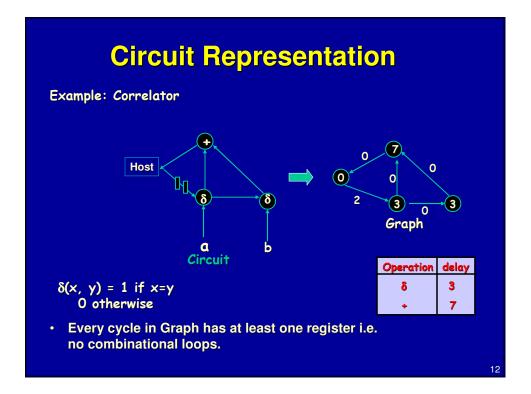


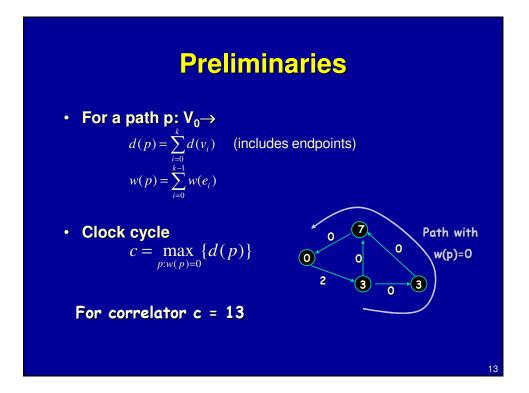
Importance of Retiming

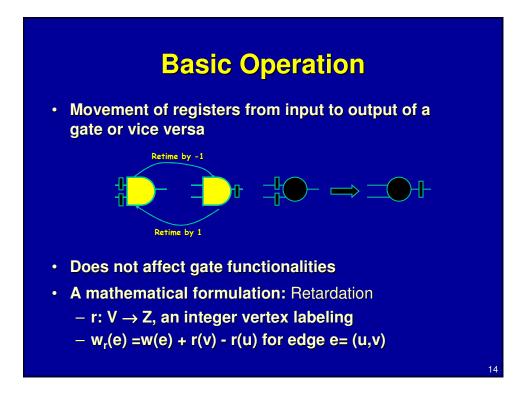
- Practical sequential optimization
- Global optimality for clock period and register positioning
- Must for HDL synthesis
 - lowers dependency on user description
- Low power strategy
 - decrease #registers with no loss in performance

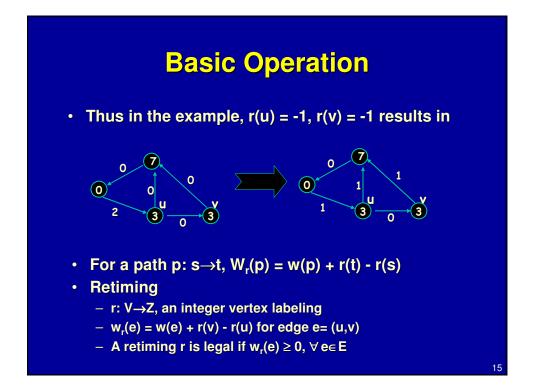


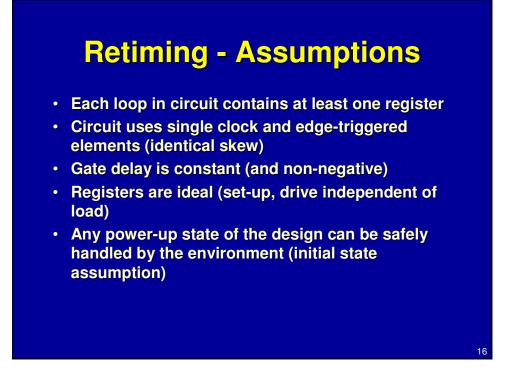


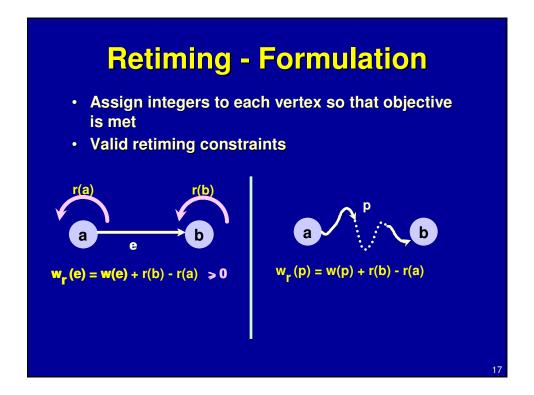










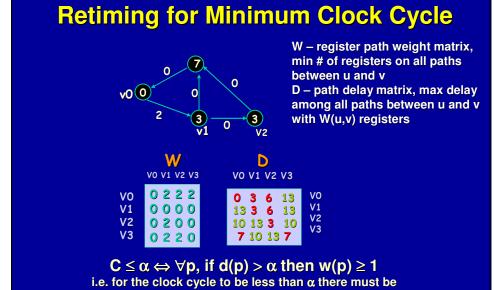


Retiming for Minimum Clock Cycle - Problem Statement: (Minimum cycle time) - Given G(V, E, d, w), find a Legal retiming r so that $c = \max_{p:Wr(p)=0} \{d(p)\}$ (A) is minimized - 2 important matrices · Register weight matrix $W(u,v) = \min\{w(p): u \xrightarrow{p} v, w(p) = W(u,v)\}$

$$D(u,v) > c \Rightarrow W(u,v) \ge 1$$

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(B)



a latch in the path

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Conditions for Retiming

- Suppose we need to check if a retiming exists for a clock cycle α
- Legal retiming: $w_r(e) \geq 0$ for all e. Hence $w_r(e) = w(e) + r(v) r(u) \geq 0 \text{ or}$

• For all paths p: $u \rightarrow v$ such that $d(p) \ge \alpha$, we require $w_r(p) \ge 1$ - Thus

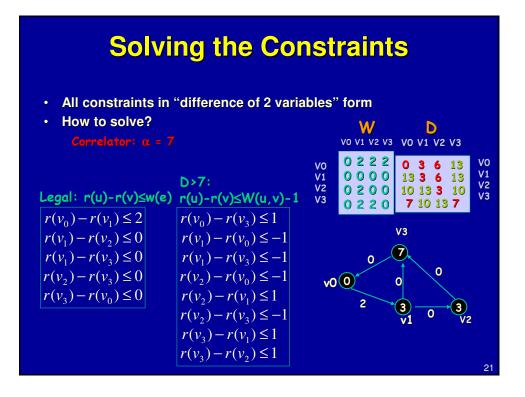
$$1 \le w_r(p) = \sum_{i=0}^{k-1} w_r(e_i)$$

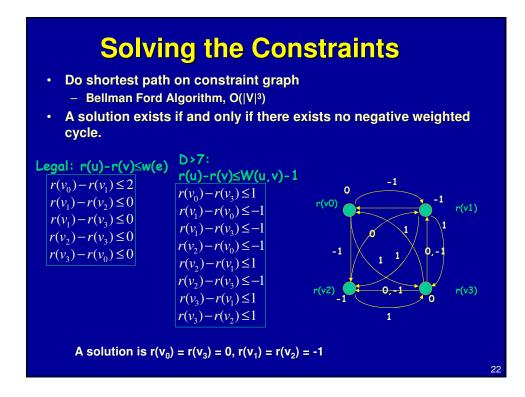
= $\sum_{i=0}^{k-1} [w(e_i) + r(v_{i+1}) - r(v_i)]$
= $w(p) + r(v_k) - r(v_0)$
= $w(p) + r(v) - r(u)$

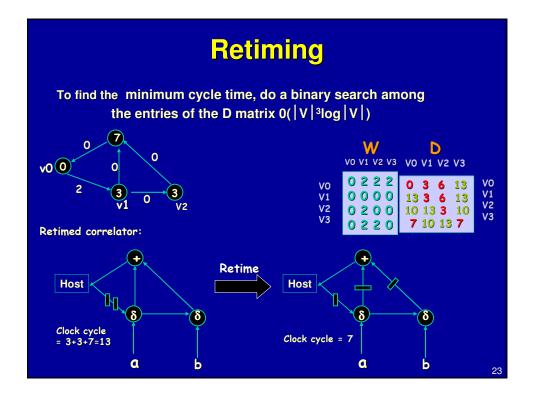
Or take the least w(p) (tightest constraint) $r(u)-r(v) \le W(u,v)-1$

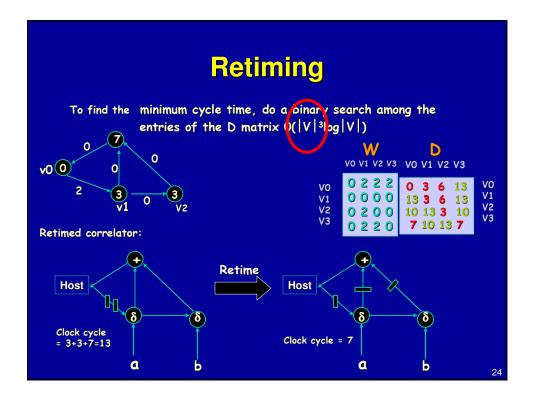
i.e. there are many paths *p*, choose the *p* that gives tightest constraint Note: we just need to apply it to (u, v) such that $D(u,v) > \alpha$

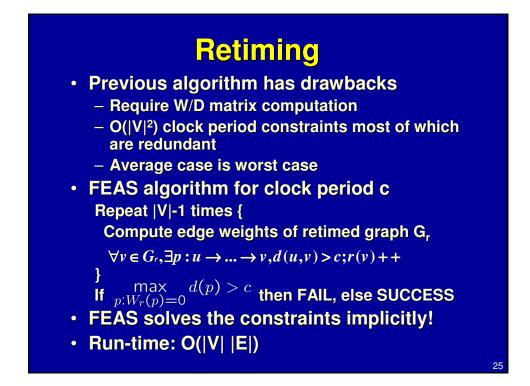
20

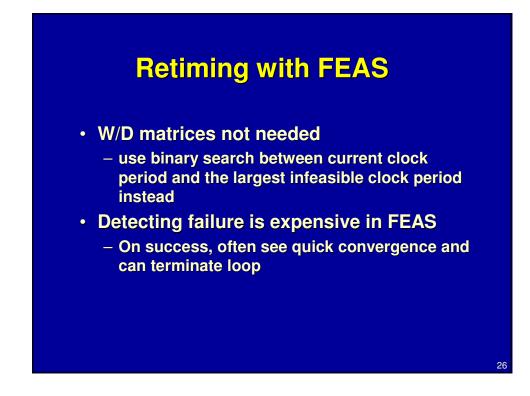


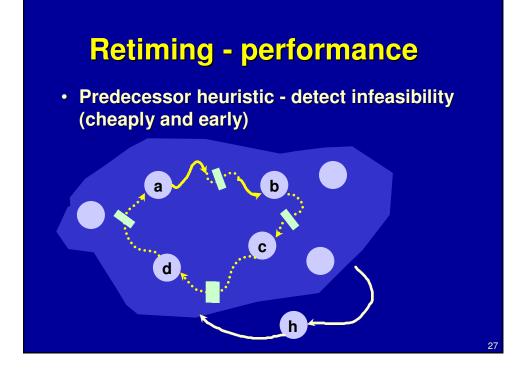


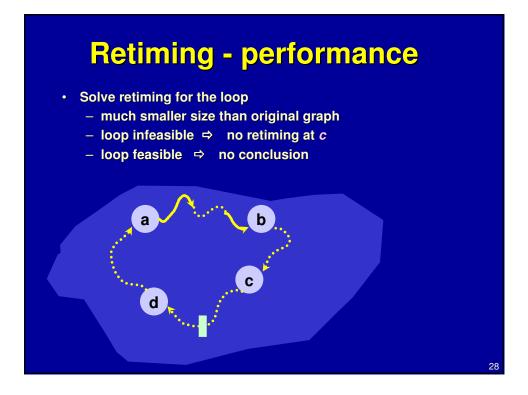








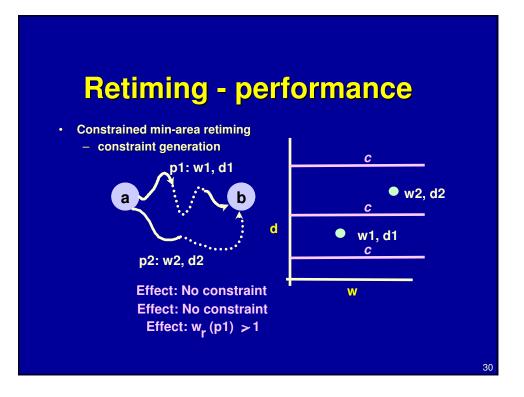






Goal: minimize number of registers used $\min N_{r} = \sum_{e \in E} w_{r}(e)$ $= \sum_{e:u \to v} (w(e) + r(v) - r(u))$ $= \sum_{e \in E} w(e) + \sum_{e:u \to v} (r(v) - r(u))$ $= N + \sum_{u \to v} (r(v) - r(u))$ $= N + \sum_{v \in V} [r(v)(\# fanin(v) - \# fanout(v)]]$ $= N + \sum_{v \in V} a_{v}r(v)$ Other constraints where a_{v} is a constant. Same as before Solved by solving the dual linear program

• A minimum cost circulation problem

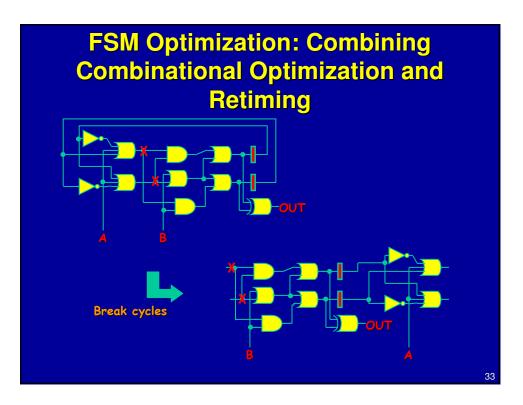


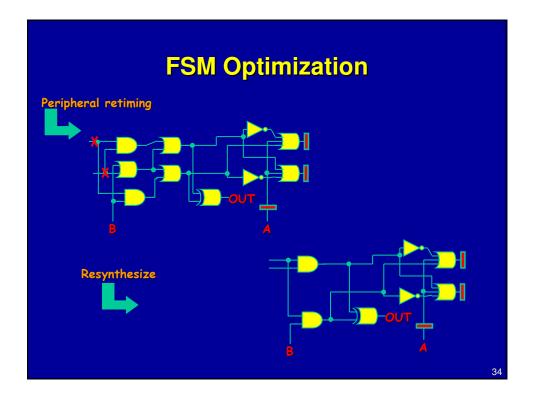
Retiming For Minimum Area

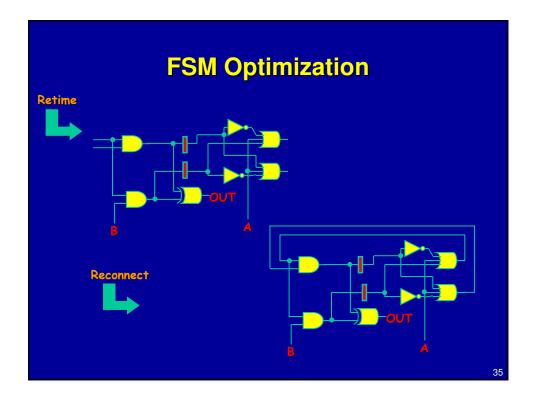
In practice

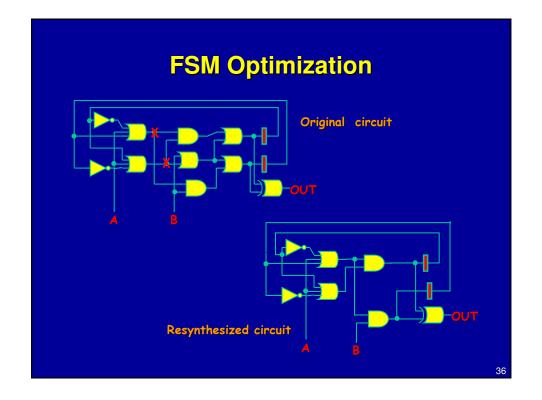
- We need W & D matrices to add clock period edges
 - Compute row of matrix at a time and avoid redundant edges
- Use minimum cost scaling to solve circulation problem
 - Numeric precision needs big integers!

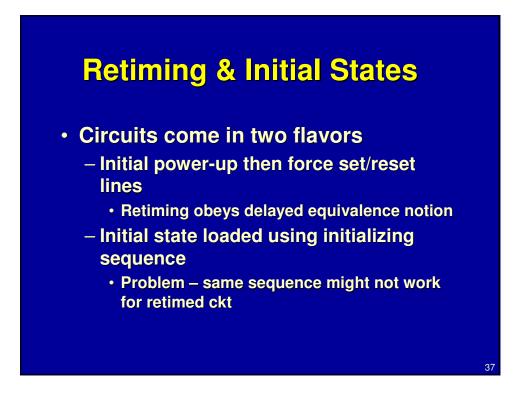
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Retiming in practice today

- Mostly used in pipelined datapath
- Verification technology needs to be improved for greater acceptance

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