

CS-184: Computer Graphics

Lecture #16: Global Illumination

Prof. James O'Brien
University of California, Berkeley

10/24/12

Today

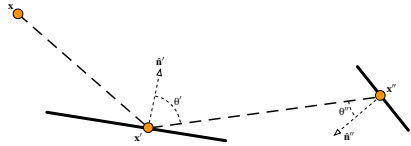
- The Rendering Equation
- Radiosity Method
- Photon Mapping
- Ambient Occlusion

2

The Rendering Equation

$$L_s(\mathbf{x}, \mathbf{x}') = \delta(\mathbf{x}, \mathbf{x}') \left[E(\mathbf{x}, \mathbf{x}') + \int_S \rho_{\mathbf{x}'}(\mathbf{x}, \mathbf{x}'') L_s(\mathbf{x}', \mathbf{x}'') \frac{\cos(\theta') \cos(\theta'')}{\|\mathbf{x}' - \mathbf{x}''\|^2} d\mathbf{x}'' \right]$$

sum over every bit of surface in the scene
 scaled by distance from \mathbf{x} to \mathbf{x}''
 light energy hitting \mathbf{x} from \mathbf{x}''
 orientation (form factor)



5

Radiosity

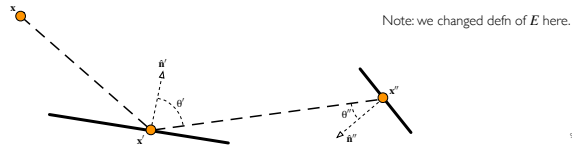
- Assume all materials are perfectly Lambertian (diffuse only, no specularities)
 - Removes all dependence on directions
 - Reduces dimensionality of lightfield
 - Allows a FEM solution (break up into chunks)
- Can also relax assumption slightly...

6

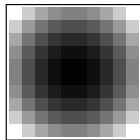
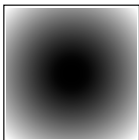
Rewrite in Terms of Radiosity

$$L_s(\mathbf{x}, \mathbf{x}') = \delta(\mathbf{x}, \mathbf{x}') \left[E_{x'} + \int_S \rho_{x'} L_s(\mathbf{x}', \mathbf{x}'') \frac{\cos(\theta') \cos(\theta'')}{\|\mathbf{x}' - \mathbf{x}''\|^2} d\mathbf{x}'' \right]$$

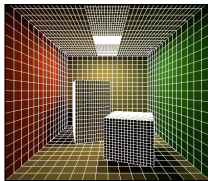
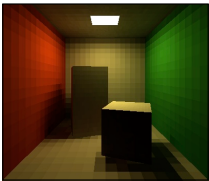
$$H_{x'} = E_{x'} + \rho_{x'} \int_S \delta(\mathbf{x}', \mathbf{x}'') \frac{H_{x''} \cos(\theta') \cos(\theta'')}{2\pi \|\mathbf{x}' - \mathbf{x}''\|^2} d\mathbf{x}''$$



Discretize into Patches



Piece-wise
constant patches



Example mesh for Cornell Box
by Mark Schreierbach

10

Discretize into Patches



The Candlestick Theater.
Mark Mack Architects.

11

Discretize into Patches



The Candlestick Theater.
Mark Mack Architects.

12

Radiosity Method

- Given the light emitted and surface properties
- First compute F_{ij} , form factors between patches
- Then **solve a linear system to balance energy between all patches**
- Comments:
 - The system is very large
 - It is also sparse (why?)
 - Should be solved with an iterative method
 - e.g.: Jacobi or Gauss-Seidel
 - **Solution is view independent**

15

Progressive Radiosity

- If magnitude of eigenvalues of $\mathbf{A} < 1$
$$(\mathbf{I} - \mathbf{A})^{-1} = \mathbf{I} + \mathbf{A} + \mathbf{A}^2 + \mathbf{A}^3 + \dots$$

- True for form-factor matrices

- Use Gauss-Seidel-like iteration but reorder by priority

$$\mathbf{h}^{k+1} = \mathbf{h}^k + \mathbf{u}^{k+1}$$

$$\mathbf{u}^{k+1} = \mathbf{A} \mathbf{u}^k$$

$$\mathbf{h}^0 = 0 \quad \mathbf{u}^0 = \mathbf{e}$$

Idea: let important sources
of light energy emit first, maybe
don't even bother with dark things

Southwell Relaxation

16

Progressive Radiosity

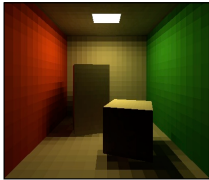


From dissertation "Efficient and predictive realistic image synthesis"
by Karol Myszkowski

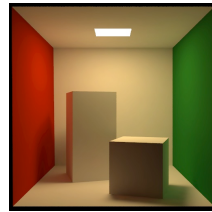
17

Touchup

- Each patch will have a constant color
- Smooth solution (e.g. average to vertices)



Example mesh for Cornell Box
by Mark Schmelzerbach



Does not match but you get the idea...

18

Other Things

- Each patch will have a constant color
 - Smooth solution (e.g. average to vertices)
- No specular reflection
 - Add Phong specular term or raytraced specular reflection
- Grid artifacts
 - Be clever with grid...

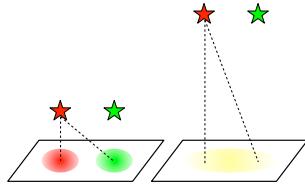
19



White Light by Paul Cookesedge

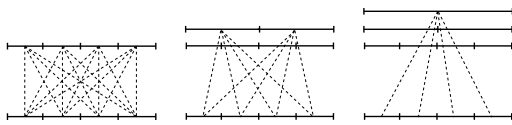
Hierarchical Radiosity

- Light smoothes with distance
 - Compare $1/h^2$ with $1/(h^2 + d^2)$ as h gets large



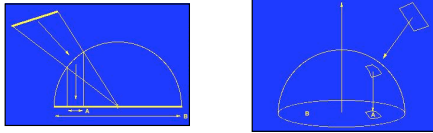
Hierarchical Radiosity

- Light smoothes with distance
 - Compare $1/h^2$ with $1/(h^2 + d^2)$ as h gets large
- Group patches into hierarchy
 - Far interactions use lower-res form factors



Computing Form Factors

- Form factors have a geometric meaning

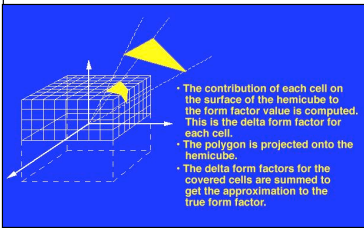


Images from
SIGGRAPH 93 Education Slide Set
by Stephen Spencer

23

Computing Form Factors

- Form factors have a geometric meaning
- "Hemicube" algorithm uses regular scan conversion



Images from
SIGGRAPH 93 Education Slide Set
by Stephen Spencer

24

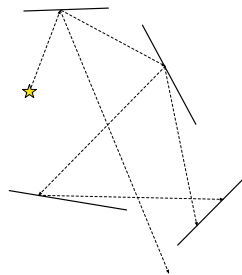
Computing Form Factors

- Form factors have a geometric meaning
- "Hemicube" algorithm uses regular scan conversion
- Also computed by ray-based sampling
- **In practice, computing form factors is the bottleneck**

25

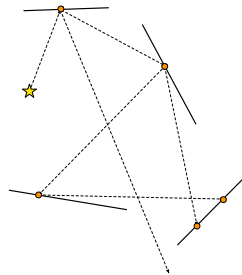
Photon Mapping

- Lights cast "photons" into environment
- Cast in random directions
- Trace into environment
- Store records at intersections



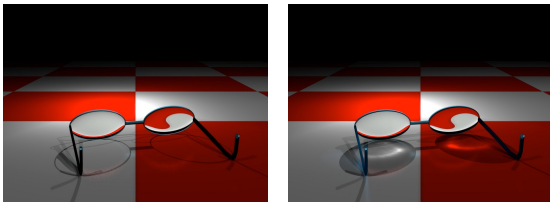
Photon Mapping

- Lights cast "photons" into environment
- Cast in random directions
- Trace into environment
- Store records at intersections
 - With KD-Trees...



27

Comparison



Ray Tracing

Ray Tracing w/ Photon Map

Catherine Bendebury and Jonathan Michaels
CS 184 Spring 2005

28

Photon Mapping



Image by Per Christensen

A ray traced image

Note:
Dark shadows
Unlit corners
Nice reflections

29

Photon Mapping

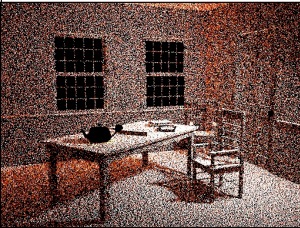


Image by Per Christensen

Raw photons

Note:
Noisy
Sparse

30

Photon Mapping



Image by Per Christensen

Interpolated Photons

Note:
Still noisy
Biased

31

Photon Mapping



Image by Per Christensen

Interpolated Photons
(multiplied by diffuse)

Note:
Still noisy
Biased

32

Photon Mapping

- Final Gather
 - Ray trace scene
 - Direct and specular rays as normal
 - Diffuse rays traced into photon map
- *Diffuse reflection smooths noise*

33

Photon Mapping



Image by Per Christensen

Final Image

Note:
Not noisy
Nice lighting
Reflections
May still be biased

Final gather often
bottleneck...

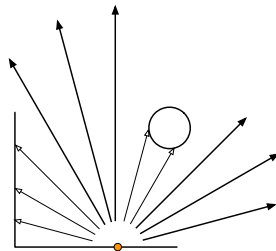
34

Ambient Occlusion

- A "hack" to create more realistic ambient illumination cheaply
- Assume light from everywhere is partially blocked by local objects
 - At a point on the surface cast rays at random
 - Ambient term is proportional to percent of rays that hit nothing
 - Weight average by cosine of angle with normal
 - Take into account how far before occluded

35

Ambient Occlusion



36

