CS-184: Computer Graphics

Lecture 15: Radiometry

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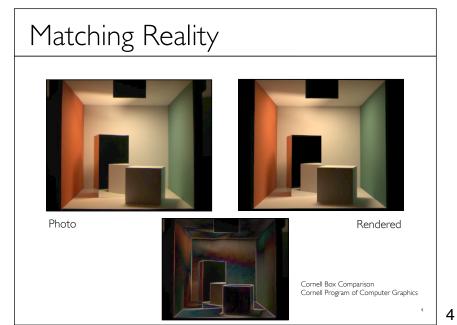
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Matching Reality



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Units

Light energy

- Really power not energy is what we measure
- Joules / second (J/s) = Watts (W)

Spectral energy density

- Power per unit spectrum interval
- Watts / nano-meter (W/nm)
- Properly done as function over spectrum
- Often just sampled for RGB

Often we assume people know we're talking about S.E.D. and just say E...

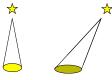
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Irradiance

Total light striking surface from all directions

- Only meaningful w.r.t. a surface
- Power per square meter (W/m^2)
- Really S.E.D. per square meter $(W/m^2/nm)$
- Not all directions sum the same because of foreshortening





Radiant Exitance

Total light *leaving* surface over all directions

- Only meaningful w.r.t. a surface
- Power per square meter $\left(W/m^2\right)$
- Really S.E.D. per square meter $(W/m^2\,/nm)$
- Also called Radiosity
- Sum over all directions \Rightarrow same in all directions



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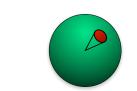


Regular angles measured in $\textit{radians}~[0..2\pi]$

• Measured by arc-length on unit circle

Solid angles measured in *steradians* $[0..4\pi]$

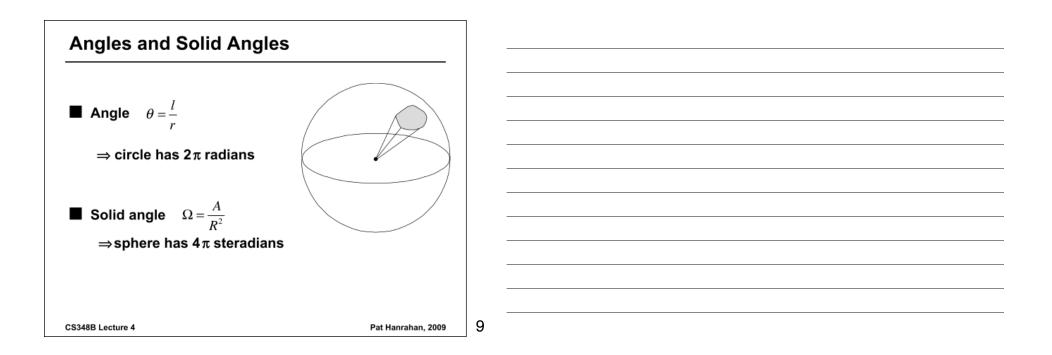
- Measured by area on unit sphere
- Not necessarily little round pieces...

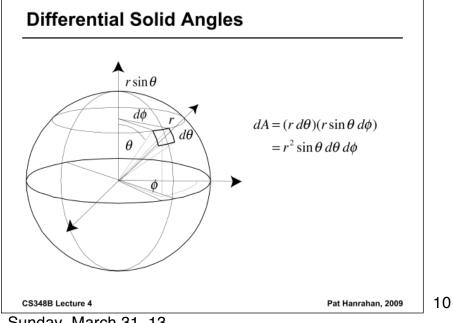


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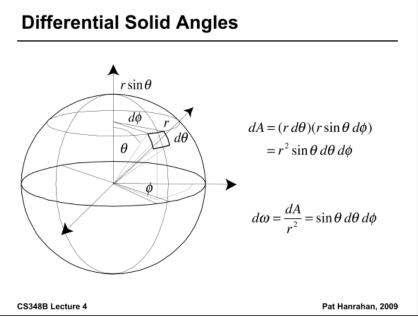
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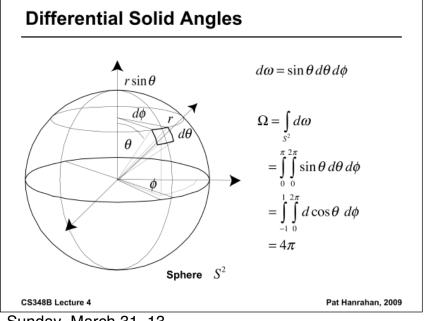














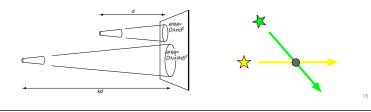
Radiance

Light energy passing though a point in space within a given solid angle

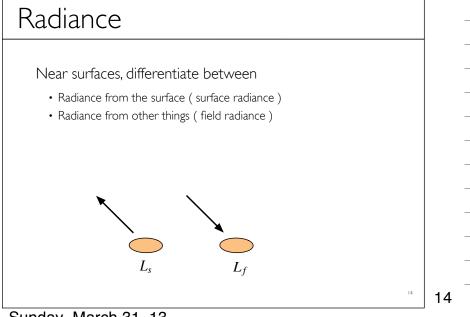
- Energy per steradian per square meter $(W/m^2\,/sr)$
- + S.E.D. per steradian per square meter $(W/m^2/sr\/nm)$

Constant along straight lines in free space

• Area of surface being sampled is proportional to distance and light inversely proportional to squared distance





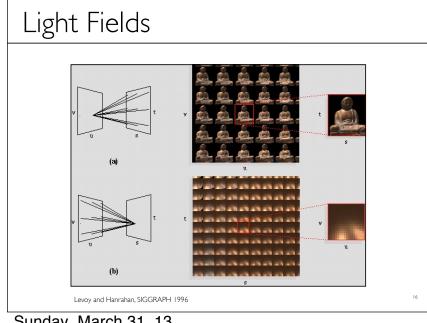


Light Fields

Radiance at every point in space, direction, and frequency: 6D function Collapse frequency to RGB, and assume free space: 4D function Sample and record it over some volume

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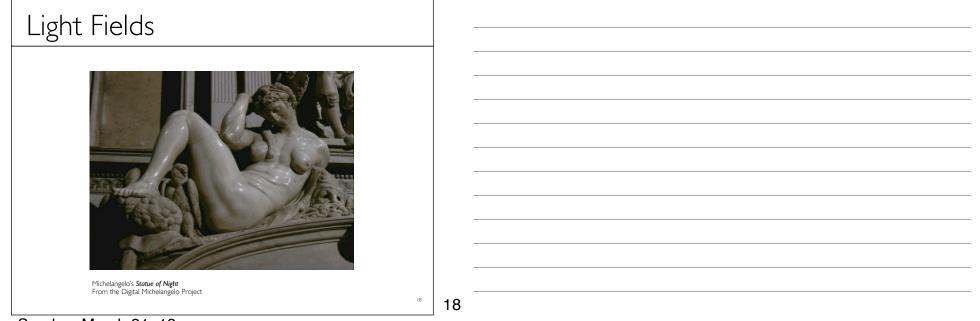
Light Fields



Levoy and Hanrahan, SIGGRAPH 1996

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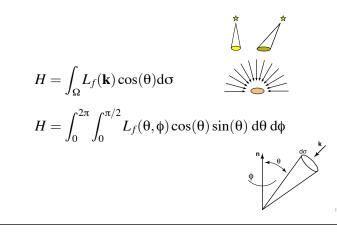
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Computing Irradiance

Integrate incoming radiance (field radiance) over all direction

• Take into account foreshortening





Revisiting The BRDF

How much light from direction k_i goes out in direction k_o

Now we can talk about units:

• BRDF is ratio of surface radiance to the foreshortened field radiance

$$\rho(\mathbf{k}_{i}, \mathbf{k}_{o}) = \frac{L_{s}(\mathbf{k}_{o})}{L_{f}(\mathbf{k}_{i})\cos(\theta_{i})}$$
We left out frequency dependance here...
Also note for perfect Lambertian reflector
with constant BRDF $\rho = 1/\pi$

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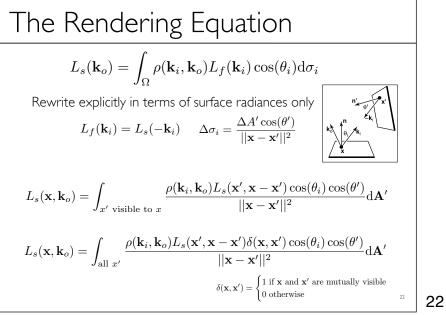
The Rendering Equation

Total light going out in some direction is given by an integral over all incoming directions:

$$L_s(\mathbf{k}_o) = \int_{\Omega} \rho(\mathbf{k}_i, \mathbf{k}_o) L_f(\mathbf{k}_i) \cos(\theta_i) \mathrm{d}\sigma_i$$

• Note, this is recursive (my L_f is another's L_s)

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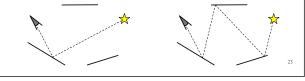


Light Paths

Many paths from light to eye

Characterize by the types of bounces

- Begin at light
- End at eye
- "Specular" bounces
- ''Diffuse'' bounces



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