## CS-184: Computer Graphics

### Lecture 15: Radiometry

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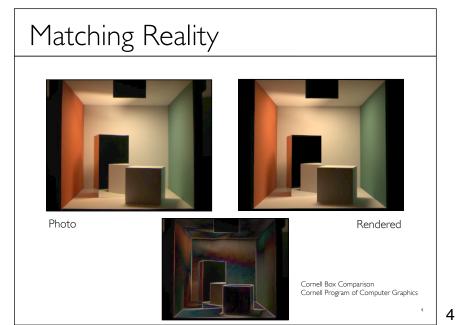
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## Matching Reality



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### Units

### Light energy

- Really power not energy is what we measure
- Joules / second ( J/s ) = Watts ( W )

### Spectral energy density

- Power per unit spectrum interval
- Watts / nano-meter ( W/nm )
- Properly done as function over spectrum
- Often just sampled for RGB

Often we assume people know we're talking about S.E.D. and just say E...

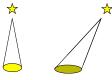
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### Irradiance

Total light striking surface from all directions

- Only meaningful w.r.t. a surface
- Power per square meter  $(W/m^2)$
- Really S.E.D. per square meter  $(W/m^2/nm)$
- Not all directions sum the same because of foreshortening





### Radiant Exitance

Total light *leaving* surface over all directions

- Only meaningful w.r.t. a surface
- Power per square meter  $\left(W/m^2\right)$
- Really S.E.D. per square meter  $(W/m^2\,/nm)$
- Also called Radiosity
- Sum over all directions  $\Rightarrow$  same in all directions



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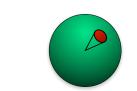


Regular angles measured in  $\textit{radians}~[0..2\pi]$ 

• Measured by arc-length on unit circle

Solid angles measured in *steradians*  $[0..4\pi]$ 

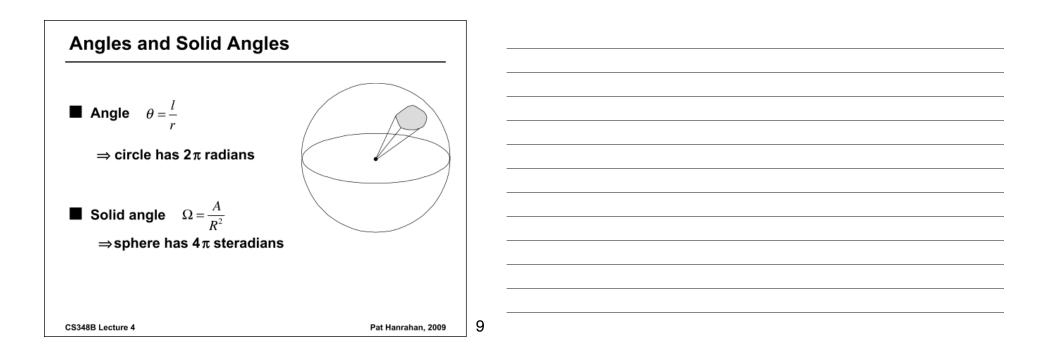
- Measured by area on unit sphere
- Not necessarily little round pieces...

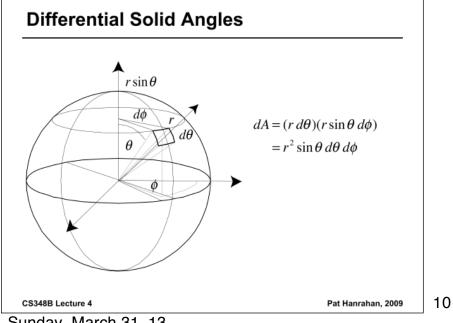


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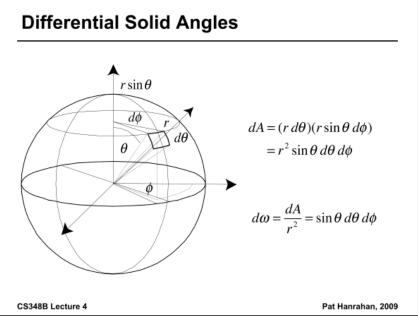
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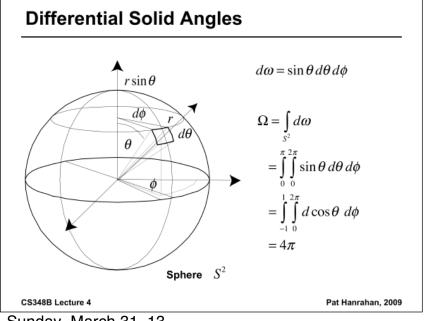














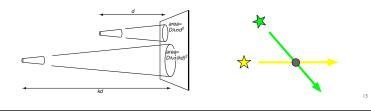
### Radiance

Light energy passing though a point in space within a given solid angle

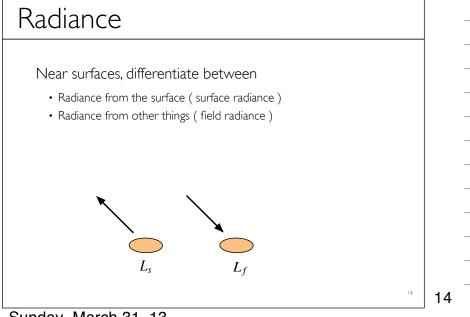
- Energy per steradian per square meter  $(W/m^2\,/sr)$
- + S.E.D. per steradian per square meter  $(W/m^2/sr\/nm)$

Constant along straight lines in free space

• Area of surface being sampled is proportional to distance and light inversely proportional to squared distance





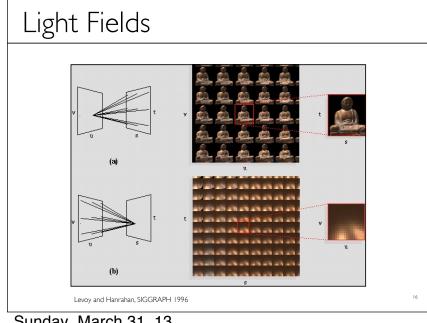


# Light Fields

Radiance at every point in space, direction, and frequency: 6D function Collapse frequency to RGB, and assume free space: 4D function Sample and record it over some volume

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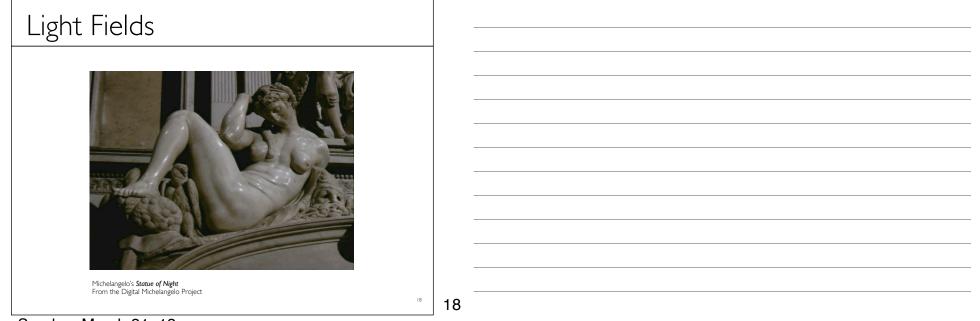
# Light Fields



Levoy and Hanrahan, SIGGRAPH 1996

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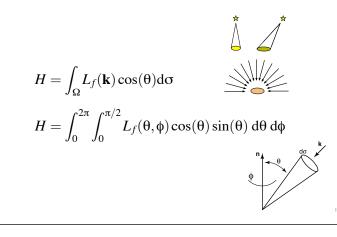
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### Computing Irradiance

Integrate incoming radiance (field radiance) over all direction

• Take into account foreshortening





### Revisiting The BRDF

How much light from direction  $k_i$  goes out in direction  $k_o$ 

Now we can talk about units:

• BRDF is ratio of surface radiance to the foreshortened field radiance

$$\rho(\mathbf{k}_{i}, \mathbf{k}_{o}) = \frac{L_{s}(\mathbf{k}_{o})}{L_{f}(\mathbf{k}_{i})\cos(\theta_{i})}$$
We left out frequency dependance here...
Also note for perfect Lambertian reflector
with constant BRDF  $\rho = 1/\pi$ 

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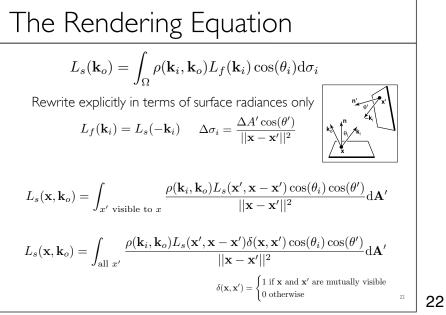
### The Rendering Equation

Total light going out in some direction is given by an integral over all incoming directions:

$$L_s(\mathbf{k}_o) = \int_{\Omega} \rho(\mathbf{k}_i, \mathbf{k}_o) L_f(\mathbf{k}_i) \cos(\theta_i) \mathrm{d}\sigma_i$$

• Note, this is recursive ( my  $L_f$  is another's  $L_s$  )

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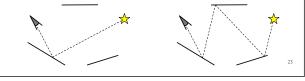


### Light Paths

Many paths from light to eye

Characterize by the types of bounces

- Begin at light
- End at eye
- "Specular" bounces
- ''Diffuse'' bounces



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