CS-184: Computer Graphics	
Lecture #18: Forward and Inverse Kinematics	
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## Forward Kinematics

• Interior joints

- Typically not 6 DOF joints
- Pin rotate about one axis
- Ball arbitrary rotation
- Prism translation along one axis



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![](_page_4_Figure_1.jpeg)

![](_page_5_Figure_0.jpeg)

![](_page_5_Figure_1.jpeg)

## Forward Kinematics

• Composite transformations up the hierarchy

![](_page_6_Picture_2.jpeg)

<sup>13</sup> 13

![](_page_6_Figure_4.jpeg)

![](_page_7_Picture_0.jpeg)

![](_page_7_Picture_1.jpeg)

![](_page_8_Figure_0.jpeg)

![](_page_8_Picture_1.jpeg)


![](_page_9_Figure_0.jpeg)

![](_page_9_Figure_1.jpeg)

![](_page_9_Figure_2.jpeg)

![](_page_10_Figure_0.jpeg)

![](_page_10_Figure_1.jpeg)

Sunday, October 27, 13

![](_page_11_Figure_0.jpeg)

![](_page_11_Figure_1.jpeg)

![](_page_11_Figure_2.jpeg)

![](_page_12_Figure_0.jpeg)

![](_page_12_Figure_1.jpeg)

![](_page_12_Figure_2.jpeg)

![](_page_13_Figure_0.jpeg)

![](_page_13_Figure_1.jpeg)

![](_page_13_Figure_2.jpeg)

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![](_page_14_Figure_0.jpeg)

![](_page_14_Figure_1.jpeg)

![](_page_14_Figure_2.jpeg)

![](_page_14_Figure_3.jpeg)

![](_page_15_Figure_0.jpeg)

![](_page_15_Figure_1.jpeg)

![](_page_15_Figure_2.jpeg)

![](_page_15_Figure_3.jpeg)

Sunday, October 27, ol 3 is well behaved (mostly)

![](_page_16_Figure_0.jpeg)

```
more joints than space so (3
outputs, but lots of inputs – so
underdetermined)
lots of solutions
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Choosing step size: solve pseudoinverse, try a step size, ask if it got closer or further away. Do a line search (criteria is getting

![](_page_16_Figure_3.jpeg)

![](_page_17_Figure_0.jpeg)

![](_page_17_Figure_1.jpeg)

![](_page_17_Figure_2.jpeg)

![](_page_18_Figure_0.jpeg)

![](_page_18_Figure_1.jpeg)

![](_page_18_Figure_2.jpeg)

![](_page_19_Figure_0.jpeg)

![](_page_19_Figure_1.jpeg)

![](_page_20_Figure_0.jpeg)

![](_page_20_Figure_1.jpeg)

![](_page_20_Figure_2.jpeg)

![](_page_20_Figure_3.jpeg)

![](_page_21_Figure_0.jpeg)

![](_page_21_Figure_1.jpeg)

![](_page_21_Figure_2.jpeg)

![](_page_21_Figure_3.jpeg)

## Suggested Reading

- Advanced Animation and Rendering Techniques by Watt and Watt
- Chapters 15 and 16

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