## CS-I 84: Computer Graphics

Lecture \#9: Scan Conversion
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## 2013:80.1.

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- Drawing Lines
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Drawing Curves
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- Filled Polygons $\qquad$
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|  | Drawing a Line |
| :--- | :--- |
|  |  |
| - Basically, its easy... but for the details |  |

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## Drawing a Line

- Basically, its easy... but for the details
- Lines are a basic primitive that needs to be done well...


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- How tas lins $\qquad$
- How should they join up?
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## Drawing a Line

## void drawLine-Error2 (int $x 1, x 2$, int $y 1, y 2$ )

float $m=$ float $(y 2-y 1) /(x 2-x 1)$
int $x=x 1$
int $y=y 1$
float e $=0.0$
while $(x<=x 2)$
setPixel(x, $\square_{,}$PIXEL_ON)
$x+=1 \quad$ No more rounding
e $+=$ m
if (e >=0.5)
$\mathrm{y}+=1$
e-=1. 0

## Drawing a Line

void drawLine-Error3(int $x 1, x 2$, int $y 1, y 2)$
int $x=x 1$
int $y=y 1$
float $e=-0.5$
while $(x<=x 2)$
setPixel( $\left.x, y, P I X E L \_O N\right)$
$\mathrm{x}+=1$
e += float(y2-y1)/(x2-x1)
if (e >=0.0)
$y^{+=1}$
$e-=1.0$

## Drawing a Line

## void drawLine-Error4 (int $x 1, x 2$, int $y 1, y 2$ )

```
int x = x1
    int y = yl
    float e = -0.5*(x2-x1) // was -0.5
    while (x <= x2)
    setPixel(x,Y,PIXEL_ON)
x += 1
    e += y2-y1 // was /(x2-x1)
if (e >= 0.0) // no change
y+=1
    e-=(x2-x1) // was 1.0
setPixel(x,y,PIXEL_ON)
// was 1.0
```

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## Drawing a Line

void drawLine-Error5 (int $x 1, x 2$, int $y 1, y 2$ )
int $x=x 1$
int $y=y 1$
int $e=-(x 2-x 1) \quad / /$ removed $* 0.5$
while $(x<=x 2)$
setPixel(x,y,PIXEL_ON)
$\mathrm{x}+=1$
e += 2* (y2-y1) // added 2*
if $(e>=0.0) \quad / /$ no change
$\mathrm{y}+=1$
e-=2*(x2-x1) // added 2*
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## Drawing a Line

## void drawLine-Bresenham(int $x 1, x 2$, int $y 1, y 2)$

```
int x = xl
    int y = y1
    int e = -(x2-x1)
Faster
Not wrong
0\leqm\leq1
x
    x += 1
    e += 2*(y2-y1)
    if (e >= 0.0)
    Y+=1
    e-=2*(x2-x1)
```


## Drawing Curves



$$
y=f(x)
$$

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Only one value of $y$ for each value of $x$...

| Drawing Curves |
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| - Parametric curves |
| •Both $x$ and $y$ are a function of some third parameter |
| $x=f(u)$ |
| $y=f(u)$ |
| $u=\left[u_{0} \ldots u_{1}\right]$ |


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|  | Drawing Curves |
| :--- | :--- |
| - Draw curves by drawing line segments <br> - Must take care in computing end points for lines <br> - How long should each line segment be? |  |
| $u \in\left[u_{0} \ldots u_{1}\right] \quad$ |  |

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## Drawing Curves

- Draw curves by drawing line segments
- Must take care in computing end points for lines
- How long should each line segment be?
- Variable spaced points


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|  | Drawing Curves |
| :--- | :--- |
| •Midpoint-test subdivision |  |
|  |  |
|  |  |
| $\left\|\mathbf{I}\left(u_{\text {mid }}\right)-\mathbf{l}(0.5)\right\|$ |  |


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|  | Drawing Curves |
| :--- | :--- |
| •Midpoint-test subdivision |  |
|  | $\left\|\mathbf{f}\left(u_{\text {mid }}\right)-\mathbf{l}(0.5)\right\|$ |

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## Drawing Curves

- Midpoint-test subdivision
- Not perfect
- We need more information for a guarantee..
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$\left|\mathbf{f}\left(u_{\text {mid }}\right)-\mathbf{l}(0.5)\right|$
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## Filling Triangles

- Render an image of a geometric primitive by setting pixel colors


## void SetPixel(int $x$, int $y$, Color rgba)

- Example: Filling the inside of a triangle


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## Filling Triangles

- Render an image of a geometric primitive by setting pixel colors
void SetPixel (int $x$, int $y$, Color rgba)
- Example: Filling the inside of a triangle

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## Triangle Scan Conversion

- Properties of a good algorithm
- Symmetric
- Straight edges
- Antialiased edges
- No cracks between adjacent primitives
- MUST BE FAST!



## Triangle Scan Conversion

- Properties of a good algorithm
- Symmetric
- Straight edges
- Antialiased edges
- No cracks between adjacent primitives
- MUST BE FAST!

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## Simple Algorithm

- Color all pixels inside triangle

```
void ScanTriangle(Triangle T, Color rgba){
    for each pixel P at (x,y){
    if (Inside(T, P))
        SetPixel(x, y, rgba)
}
```

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## Line Defines Two Halfspaces

- Implicit equation for a line

$$
\begin{array}{ll}
- \text { On line: } & a x+b y+c=0 \\
\text { - On right: } & a x+b y+c<0 \\
- \text { On left: } & a x+b y+c>0
\end{array}
$$

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## Inside Triangle Test

- Point is inside triangle if it is in positive halfspace of all three boundary lines
- Triangle vertices are ordered counter-clockwise
- Point must be on the left side of every boundary line



## Inside Triangle Test

## Boolean Inside(Triangle T, Point P)

for each boundary line $L$ of $T$ Scalar d = L.a*P.x + L.b*P.y + L.c; if ( $\mathrm{d}<0.0$ ) return FALSE;
\}
return TRUE;
\}

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## Simple Algorithm

- What is bad about this algorithm?

```
void ScanTriangle(Triangle T, Color rgba){
    for each pixel P at (x,y){
    if (Inside(T, P))
        SetPixel(x, y, rgba)
    }
```

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## Triangle Sweep-Line Algorithm

- Take advantage of spatial coherence
- Compute which pixels are inside using horizontal spans
- Process horizontal spans in scan-line order
- Take advantage of edge linearity
- Use edge slopes to update coordinates incrementally



## Triangle Sweep-Line Algorithm

```
void ScanTriangle(Triangle T, Color rgba){
    for each edge pair {
        initialize }\mp@subsup{x}{L}{},\mp@subsup{x}{R}{}
        compute d\mp@subsup{x}{L}{}/d\mp@subsup{y}{L}{}
        for each scanline at y
            for (int x = ceil( (xL); x <= x (r x++)
            SetPixel(x, y, rgba);
        x
        x
    }
}
Bresenham's algorithm
works the same way,
but uses only integer
operations!
```



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## Antialiasing

Desired solution of an integral over pixel

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## Hardware Antialiasing

Supersample pixels

- Multiple samples per pixel
- Average subpixel intensities (box filter)
- Trades intensity resolution for spatial resolution

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## Hardware Scan Conversion

- Convert everything into triangles
- Scan convert the triangles



## Polygon Scan Conversion

- Fill pixels inside a polygon
- Triangle
- Quadrilateral
- Convex
- Star-shaped
- Concave



- Self-intersecting
- Holes





What problems do we encounter with arbitrary polygons?
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## Polygon Scan Conversion

- Need better test for points inside polygon
- Triangle method works only for convex polygons


Convex Polygon


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## Inside Polygon Rule

- What is a good rule for which pixels are inside?


Concave


Self-Intersecting


With Holes
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## Inside Polygon Rule

- Odd-parity rule
- Any ray from P to infinity crosses odd number of edges



## Inside/Outside Testing



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| Filled Polygons |  |
| :--- | :--- |
|  |  |

Filled Polygons


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## Filled Polygons

Toggle inside/outside flag to "OUTSIDE"


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Filled Polygons
Treat (scan $y=$ verte $x$ ) as (scan $y>$ vertex y)


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## Filled Polygons

Horizontal edges


Filled Polygons

Horizontal edges


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Filled Polygons

- Final result:


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Drawing a Line

How thick?

Ends?

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Flood Fill


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|  | $\stackrel{1}{2}$ |
|  | ; |
|  | $\vdots$ |
|  | $\vdots$ |

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## Span-Based Algorithm

Definition: a run is a horizontal span of identically colored pixels

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I. Start at pixel "s", the seed.
2. Find the run containing "s" ("b" to "a").
3. Fill that run with the new color.
4. Search every pixel above run, looking for pixels of interior color 5. For each one found,
6. Find left side of that run ("c"), and push that on a stack.
7. Repeat lines 4-7 for the pixels below ("d").
8. Pop stack and repeat procedure with the new seed
$\qquad$

The algorithm finds runs ending at "e"," "f", "g"," $h$ ", and " "i"
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