

This Homework is due in class on Friday October 9th. It will be graded. Make sure you include your name and section number on your answer sheet.

1. Consider a triangle in the plane defined by points  $a, b, c$ . Fix  $a$  and  $b$ , and suppose that the lengths  $l_1$  of  $ac$  and  $l_2$  for  $bc$  are varied. Derive the forward kinematic equations that express the position of  $c = (c_x, c_y)$  as functions of  $l_1$  and  $l_2$ . This kind of manipulator is different from most. Its called a parallel manipulator. Its forward kinematics are hard, but inverse kinematics is easy (deriving  $l_1$  and  $l_2$  from  $c$  is trivial).
2. The Inertia matrix  $I$  for a block with dimensions  $X, Y, Z$  is

$$I = \frac{M}{12} \begin{pmatrix} Y^2 + Z^2 & 0 & 0 \\ 0 & X^2 + Z^2 & 0 \\ 0 & 0 & X^2 + Y^2 \end{pmatrix}$$

where  $M$  is the mass of the block. Suppose the block is rotated  $90^\circ$  about the x-axis. What is the new matrix? Check your answer using the formula  $I = RI_0R^T$ .

3. Recall that the Euler equation for rotation of a rigid body is

$$T = I\alpha + \omega \times I\omega$$

Assume that  $I$  is a diagonal matrix (as in the last example), with distinct values along the diagonal. Assume  $T = 0$ , for what values of  $\omega$  does the block make a simple rotation (i.e.  $\alpha = 0$ )?

4. Let  $B$  be a block whose orientation is specified by the matrix  $R$ , and suppose that orientation is a  $90^\circ$  rotation about the z-axis. Now suppose that the object starts to spin with  $\omega = (2, 2, 0)$ . What is  $dR/dt$ ?