

# Rings and Runes

## 1 Description

Frodo has entered the mines of Moria and encountered a series of gates. Each gate has written upon it an ancient riddle describing the state of a set of special rings which control that particular gate. By examining the riddle, Frodo can determine whether or not the gate can be opened, or if it is simply a death trap. **Riddles** consist of multiple **runes**. A valid **rune** contains exactly **3 statements** about 3 different rings chosen from the set of rings controlling the gate. Each **statement** in a rune is either **true** or **false**, depending on the **state** (spinning or not spinning) of a specific ring in the set of rings controlling the gate. The riddle for a particular gate does not have to use all of the possible rings contained in the gate's controlling set.

To open the gates, the hobbits must read the riddle, then, decide which of the rings to spin, and which of the rings to leave alone. Once they have the correct rings spinning, they say an incantation, and if the entire riddle for the gate is satisfied the gate will open. For the gate to open, every rune in the riddle must have **at least** one statement in it that is true based on the state of the set of rings ( $3 \leq \text{rings} \leq 22$ ) located outside of a gate.

For example, consider a specific rune: 1 -2 3 0  
this rune will be true if ( ring 1 is spinning ) **OR** ( ring 2 is NOT spinning ) **OR** (ring 3 is spinning), (NOTE: the 0 indicates the end of a rune, and only one of the statements in that rune must be true for that specific rune to be true.) If a ring number in a rune is negative (e.g. -2 ), it means that ring 2 must NOT be spinning for that particular statement in the rune to be true. If the ring number is positive, (e.g. 3) it means that ring 3 **MUST** be spinning for that statement in the rune to be true. A specific ring may only appear one time in a specific rune, however, a ring may be used multiple times in the entire riddle, just not



Figure 1: A gate in the Mines of Moria that is controlled by an ancient Rune

in the same rune!

## 2 Input

The input will consist of the following:

- The first line of input contains a single integer ( $1 \leq g \leq 30$ ) which denotes the number of gates with riddles to be decoded.
- The first line for each gate contains two integers, ( $3 \leq rings \leq 22$ ) and ( $1 \leq runes \leq 100$ ) separated by a space. *rings* is the number of rings in the controlling set, (each ring is numbered from 1 to *rings*, riddles are not required to use every possible ring). *runes* is the number of runes that must be satisfied by the set of *rings*.
- The next *runes* lines contain individual runes that specify the relationships between the rings for that gate. Each rune is represented by a single line containing four numbers:  $r_1$ ,  $r_2$ ,  $r_3$ , and 0. ( $-rings \leq r_1 \leq rings$ ) and ( $-rings \leq r_2 \leq rings$ ) and ( $-rings \leq r_3 \leq rings$ ) each separated by a space and followed by a 0.

## 3 Output

Each gate contains exactly one riddle (consisting of multiple runes), your algorithm should output exactly one line for each gate. If one or more runes in a riddle contain errors, output only the highest priority error for that riddle. The priority of errors is described below:

- If ANY rune in a riddle contains a statement about a null ring, e.g. 0 or -0, this is the most severe error in a riddle, and the whole riddle is invalid. Output "INVALID: NULL RING" as the highest priority error.
- If ANY rune in a riddle contains a statement  $r$  or  $-r$  where ( $r < -rings$ ) or ( $r > rings$ ) specified for the gate, this is the SECOND most severe error in a riddle, output "INVALID: RING MISSING". NOTE: Do NOT output this message if the riddle contained a NULL ring!
- If ANY individual rune in a riddle refers to the same ring two or three times (e.g. -2 2 3 0 OR 3 1 1 0 ) this is the THIRD most severe error in a riddle, output "INVALID: RUNE CONTAINS A REPEATED RING" again, don't output this message if a higher priority error occurred somewhere in the riddle.
- Riddles may contain repeated runes (a form of error detection/correction maybe?) treat all of these repeated runes as a single rune, since they are identical, if one is true all of the repeated runes will be true.

- If there is a configuration of spinning / still rings that satisfies all the runes in the riddle, output “RUNES SATISFIED!”
- If there is no possible configuration of spinning / still rings that satisfies all the runes, output “RUNES UNSATISFIABLE! TRY ANOTHER GATE!”

Sample Input	Sample Output
<pre> 5 3 5 1 2 3 0 1 -2 3 0 1 3 -2 0 -3 -1 2 0 1 2 3 0 3 8 3 1 2 0 3 -1 2 0 3 1 -2 0 3 -1 -2 0 2 1 -3 0 -2 1 -3 0 -1 2 -3 0 -1 -2 -3 0 3 2 -1 1 3 0 0 1 3 0 3 2 -1 1 3 0 7 1 3 0 3 2 -1 1 3 0 2 1 3 0 </pre>	<pre> RUNES SATISFIED! RUNES UNSATISFIABLE! TRY ANOTHER GATE! INVALID: NULL RING INVALID: RING MISSING INVALID: RUNE CONTAINS A REPEATED RING </pre>