

Convolutional Neural Nets II

EECS 442 – David Fouhey

Fall 2019, University of Michigan

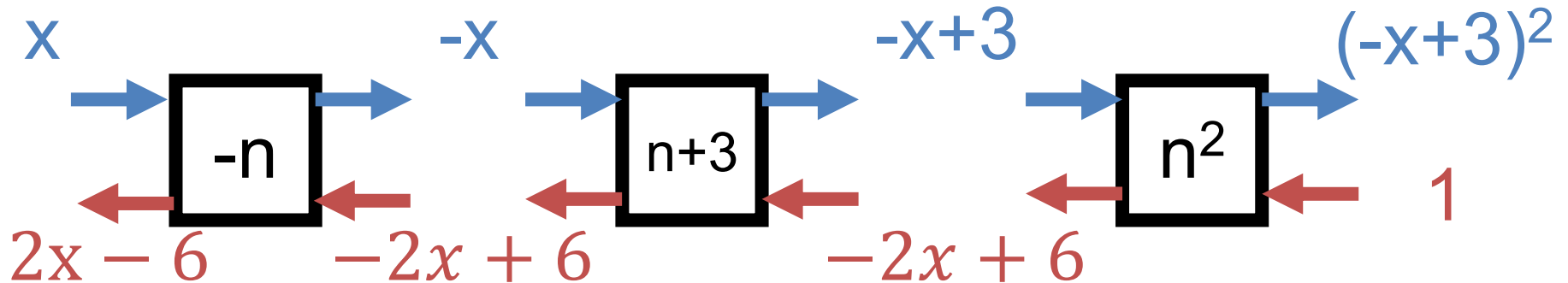
http://web.eecs.umich.edu/~fouhey/teaching/EECS442_F19/

Administrivia

- If you need a team-mate for your project, email me. I'm matching people.

Previously – Backpropagation

$$f(x) = (-x + 3)^2$$



Forward pass: compute function

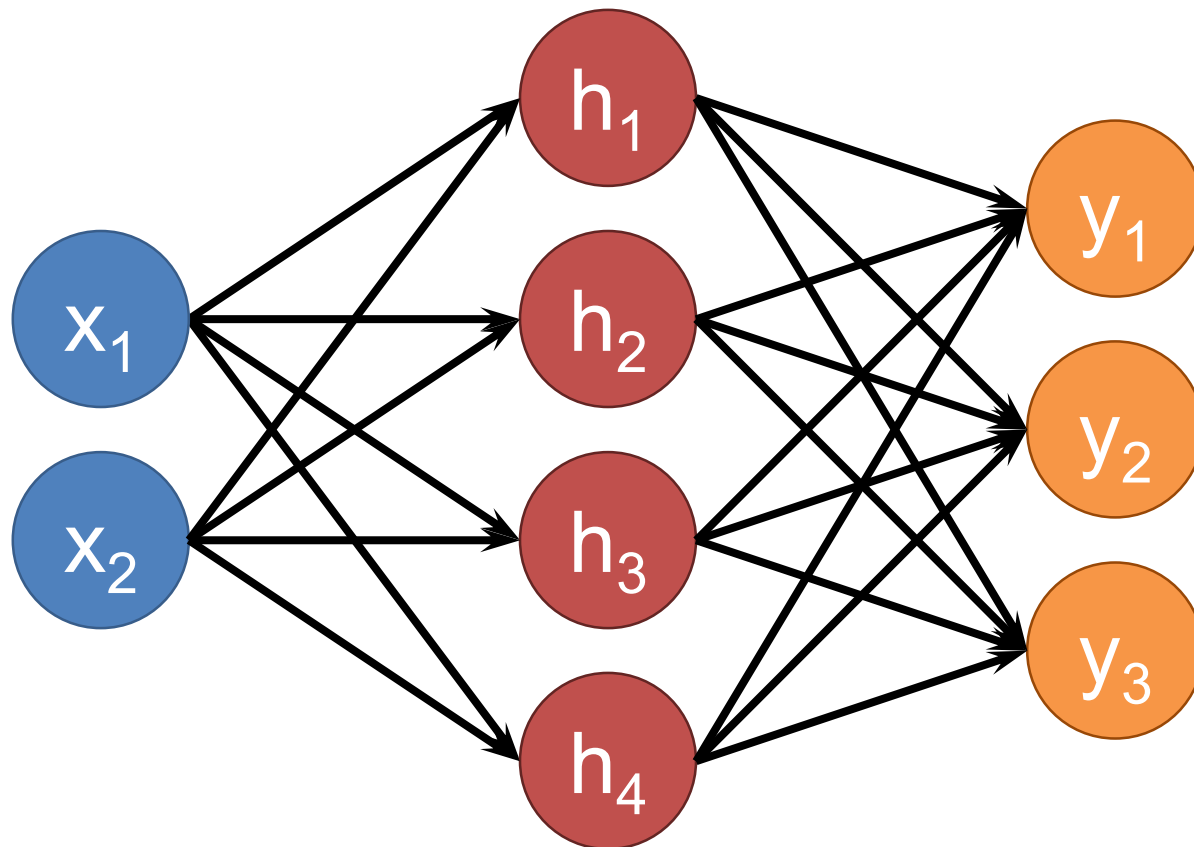
Backward pass: compute derivative of all parts of the function

Setting Up A Neural Net

Input

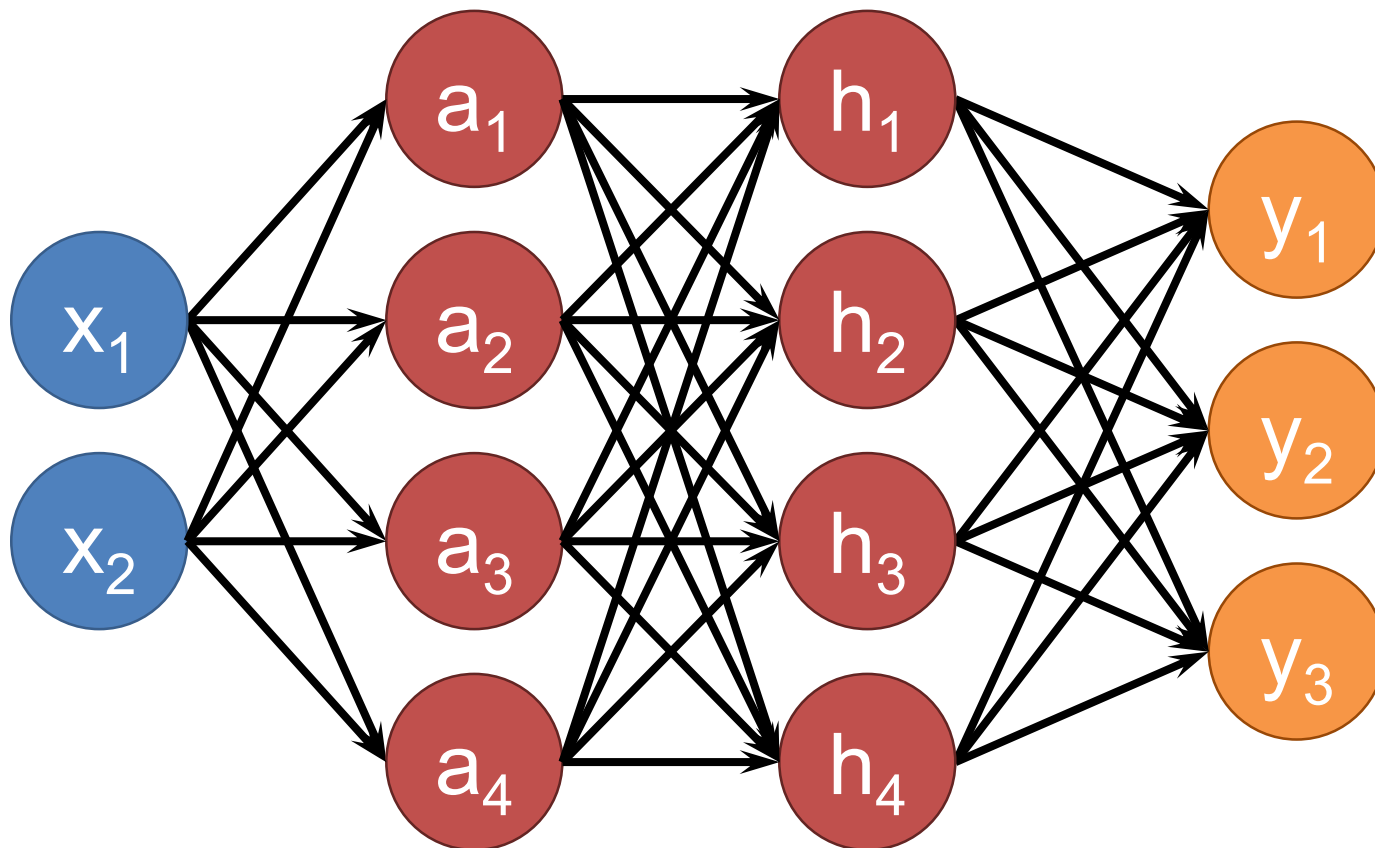
Hidden

Output

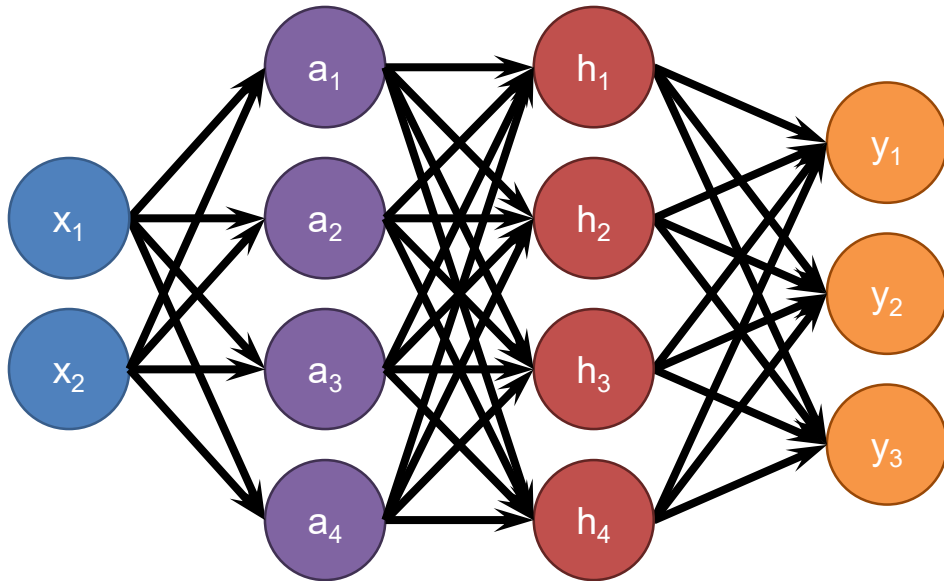


Setting Up A Neural Net

Input Hidden 1 Hidden 2 Output



Fully Connected Network

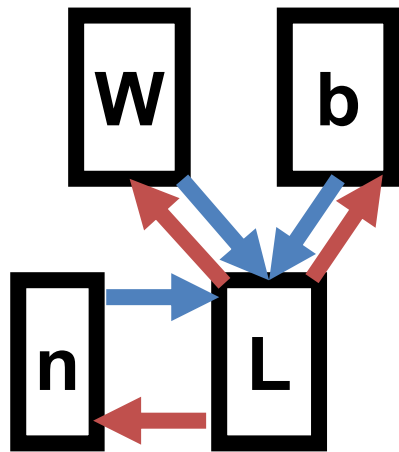


Each neuron connects to each neuron in the previous layer

Fully Connected Network

Define New Block: “Linear Layer”

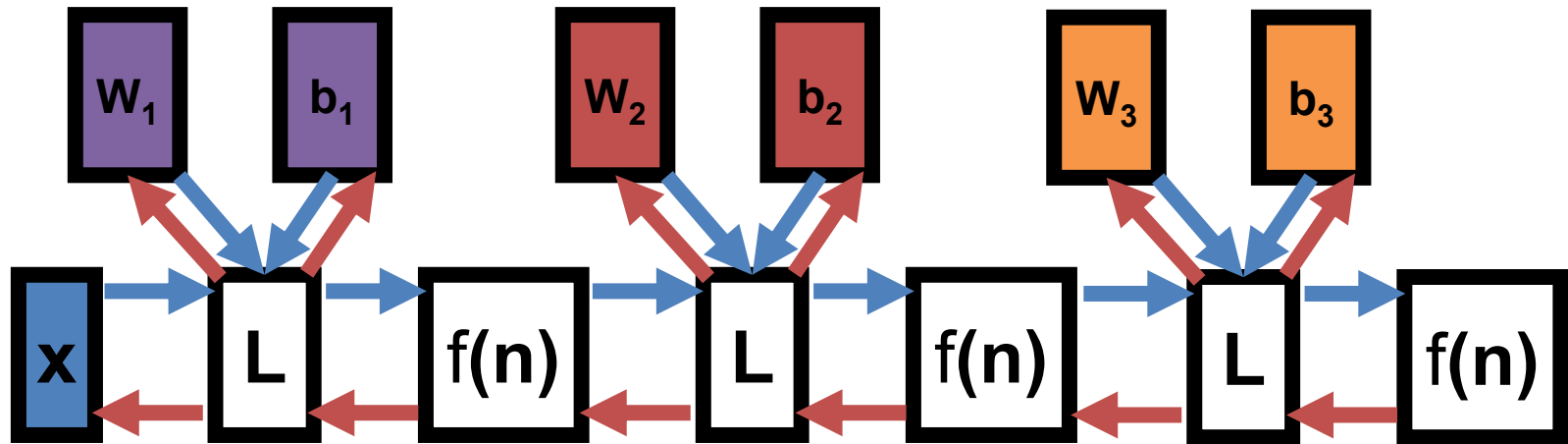
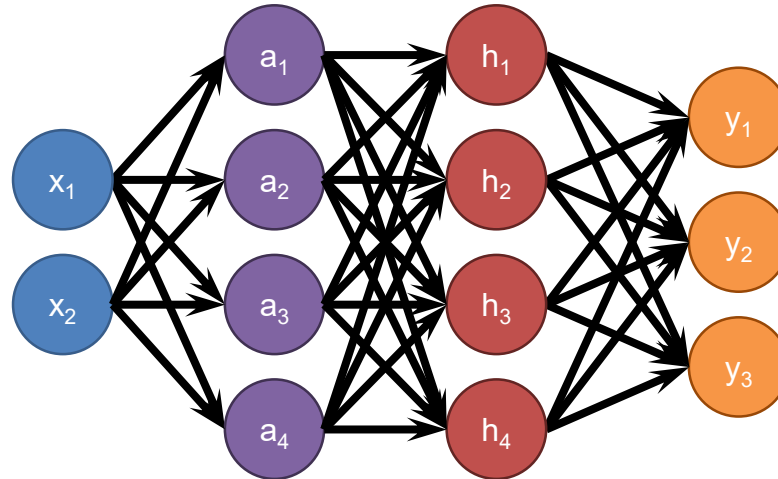
(Ok technically it's Affine)



$$L(\mathbf{n}) = \mathbf{W}\mathbf{n} + \mathbf{b}$$

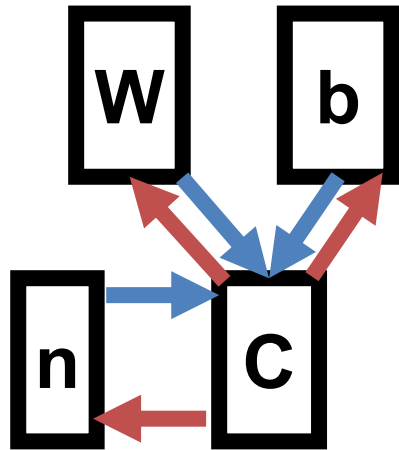
Can get gradient with respect to all the inputs

Fully Connected Network



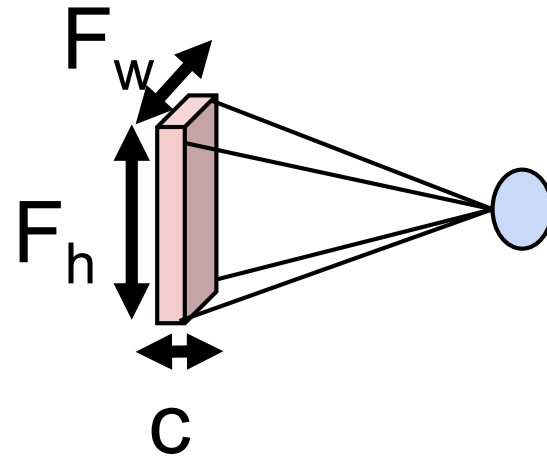
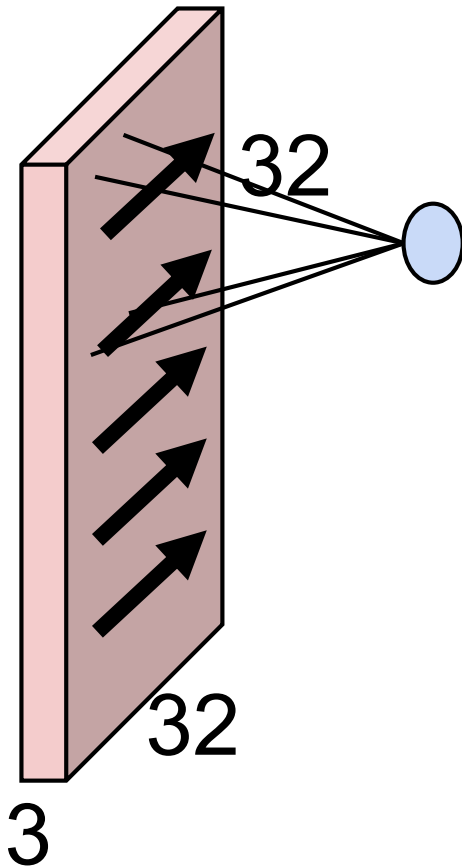
Convolutional Layer

New Block: 2D Convolution



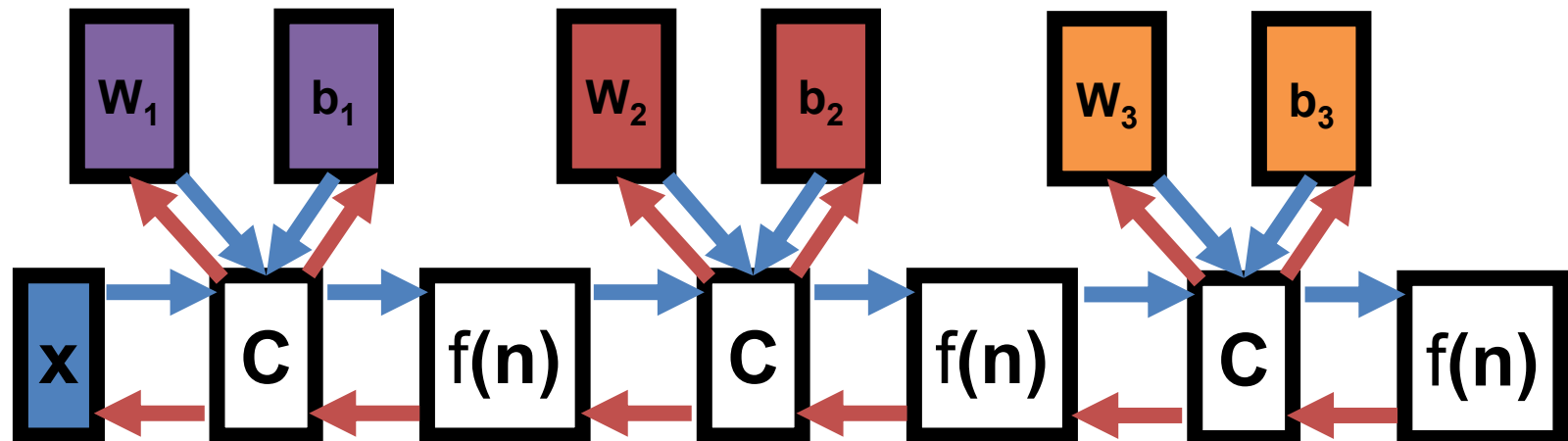
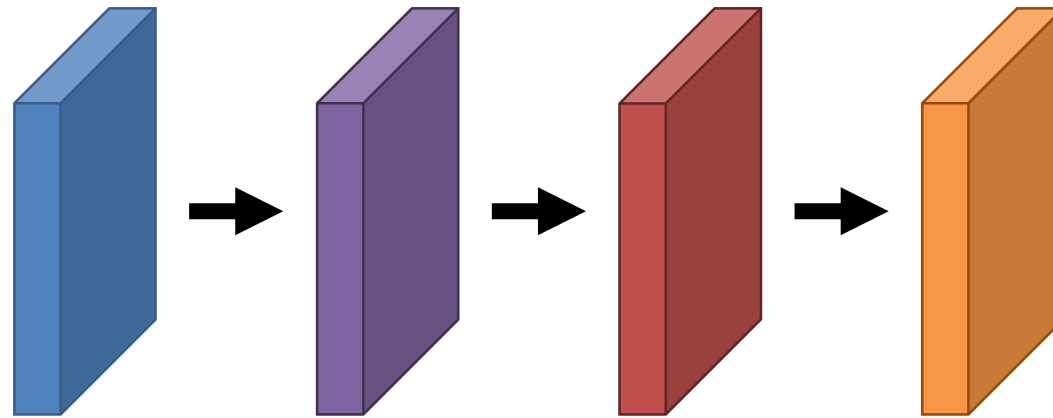
$$C(n) = n * W + b$$

Convolution Layer

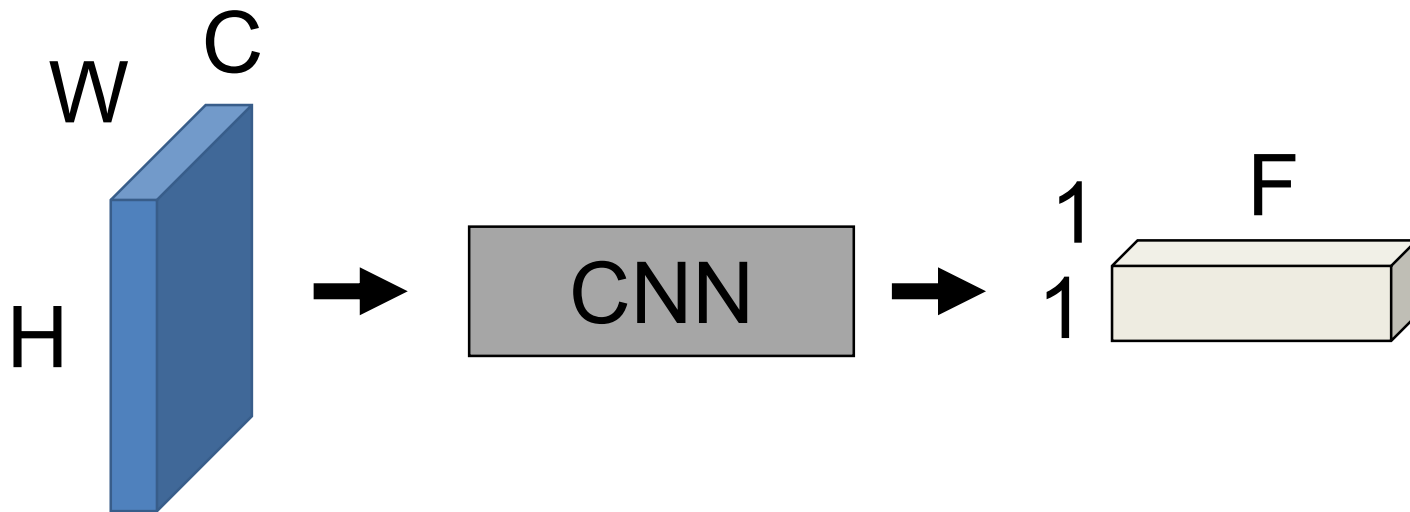


$$b + \sum_{i=1}^{F_h} \sum_{j=1}^{F_w} \sum_{k=1}^c F_{i,j,k} * I_{y+i,x+j,c}$$

Convolutional Neural Network (CNN)



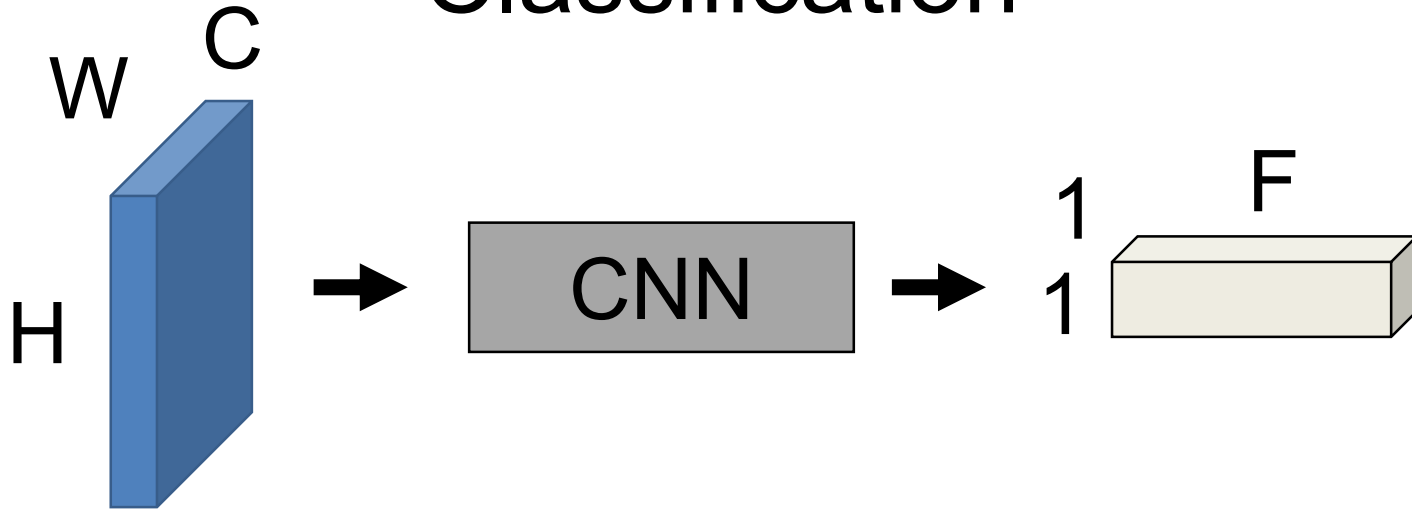
Today



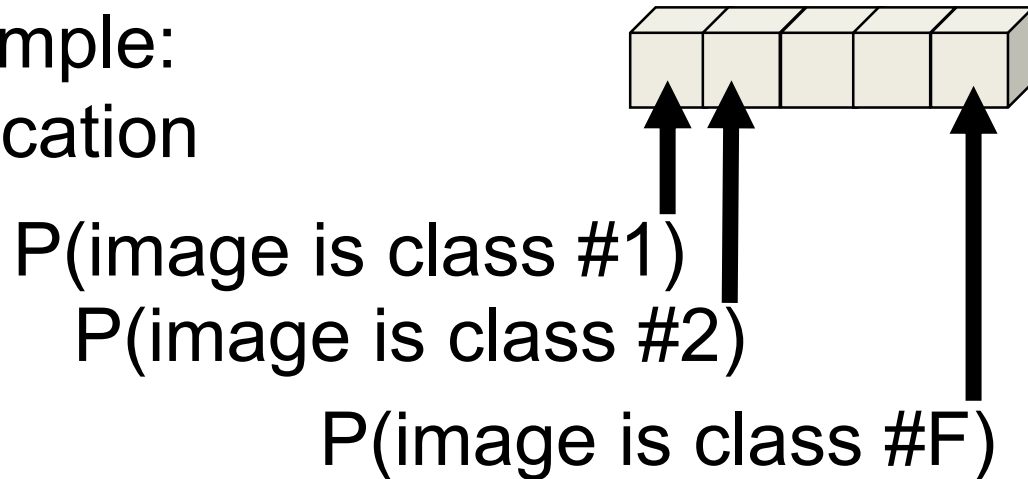
Convert $H \times W$ image into a F -dimensional vector

- What's the probability this image is a cat ($F=1$)
- Which of 1000 categories is this image? ($F=1000$)
- At what GPS coord was this image taken? ($F=2$)
- Identify the X, Y coordinates of 28 body joints of an image of a human ($F=56$)

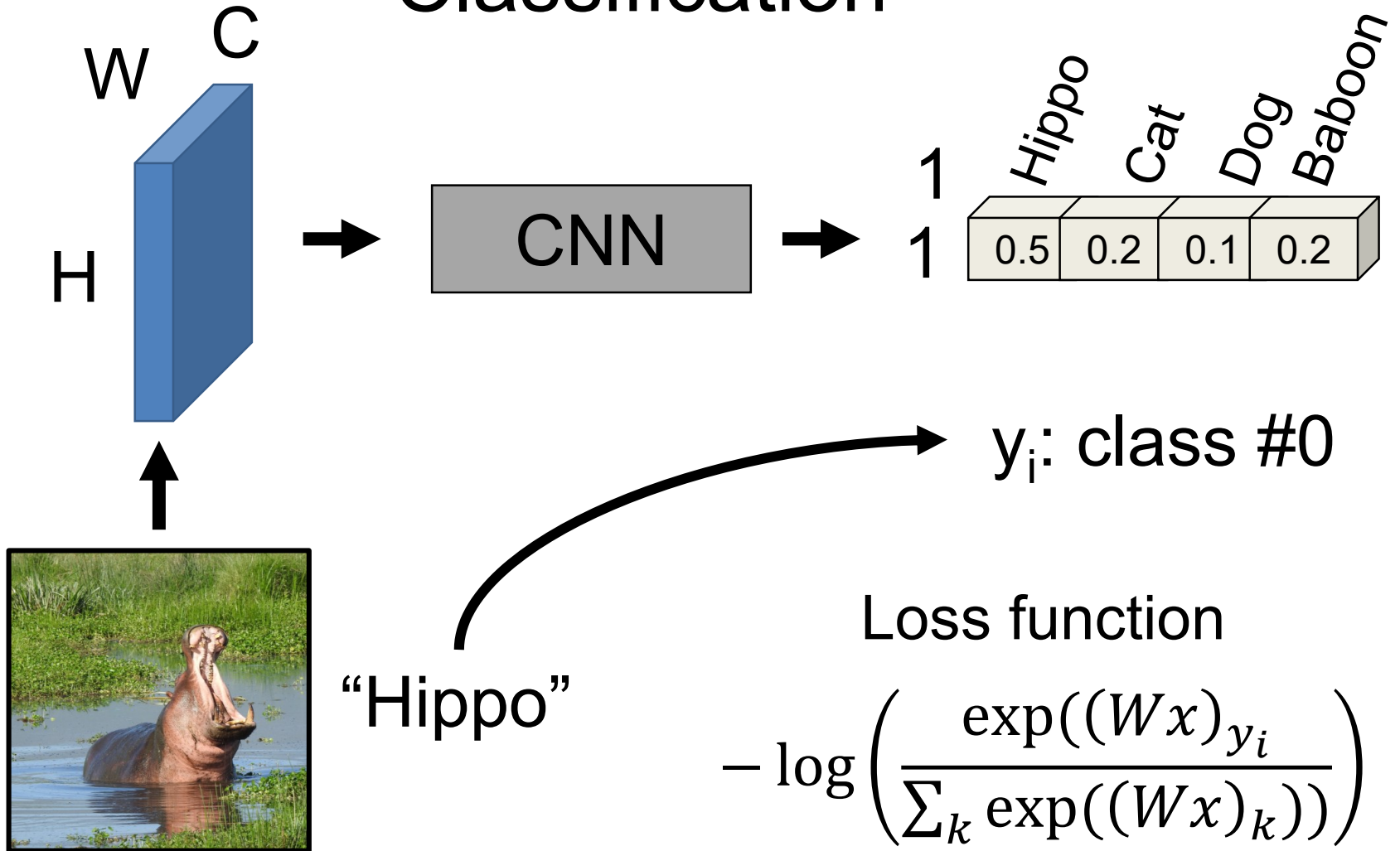
Today's Running Example: Classification



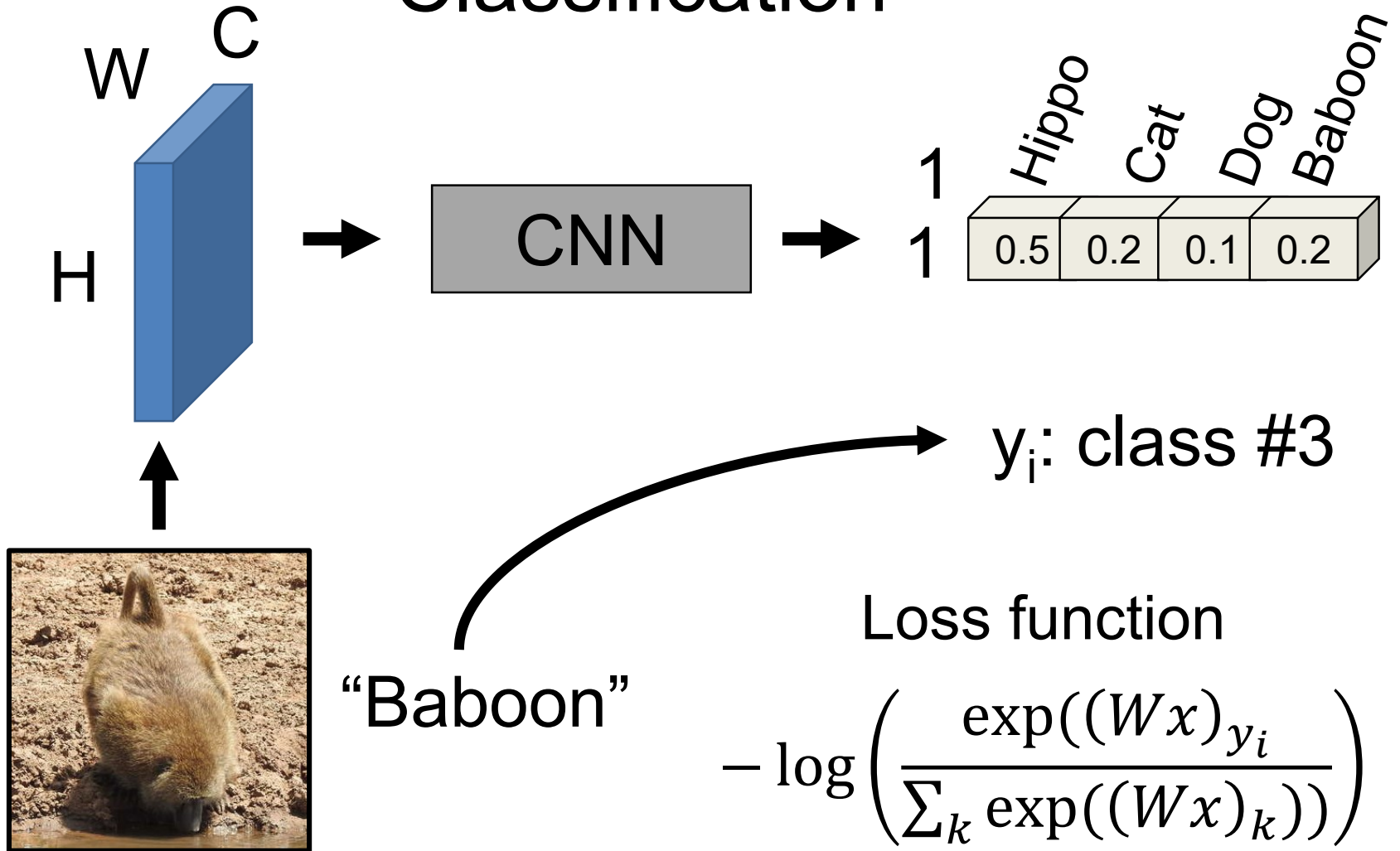
Running example:
image classification



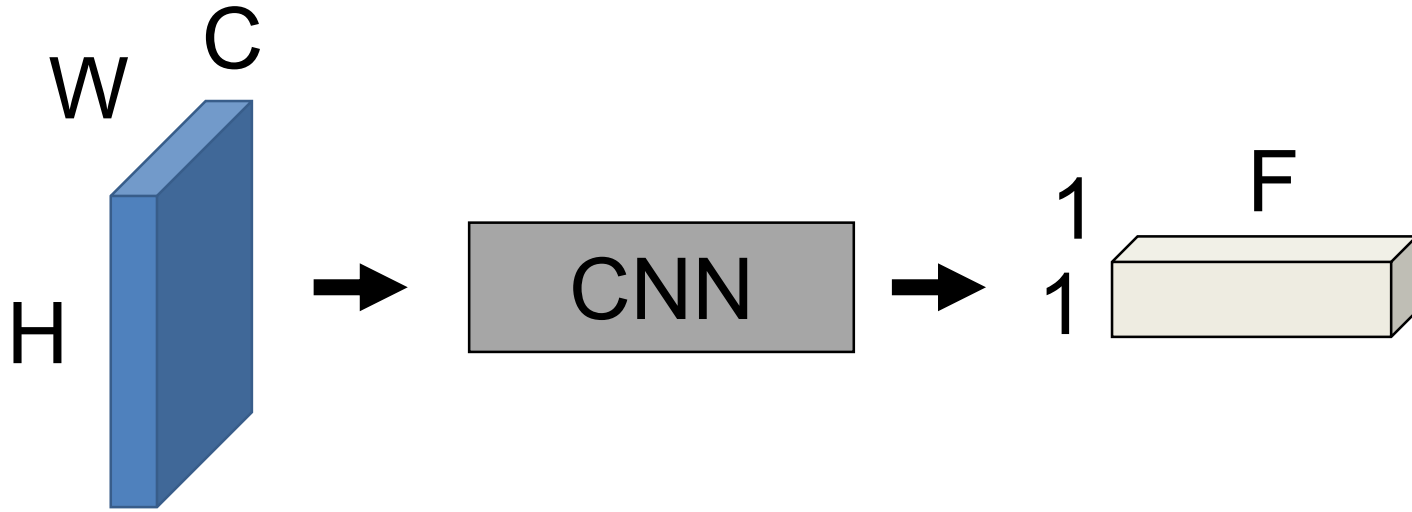
Today's Running Example: Classification



Today's Running Example: Classification



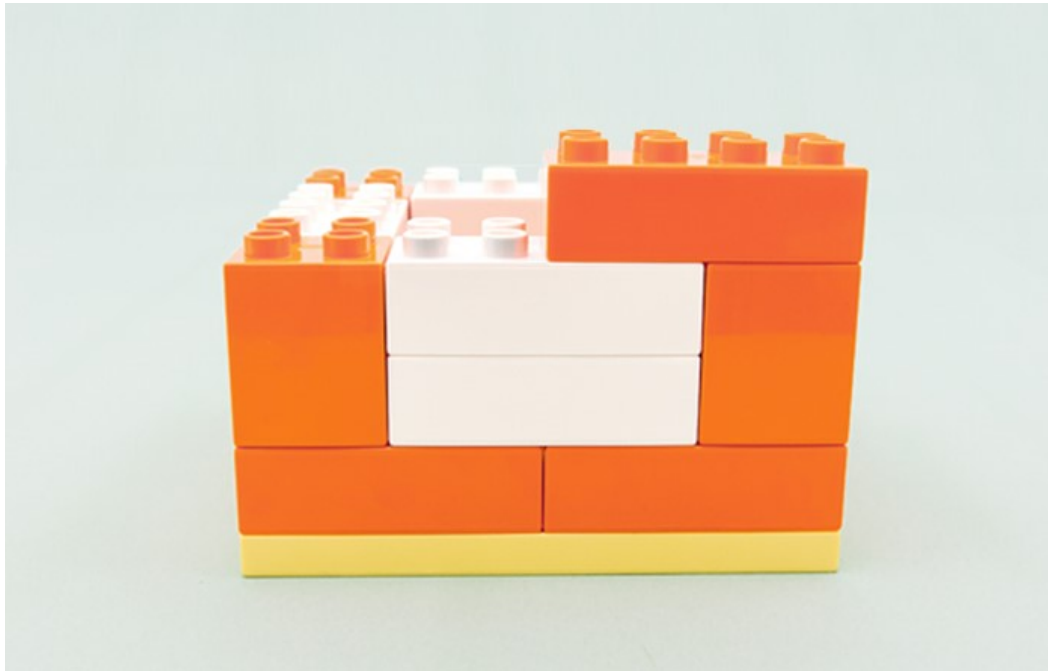
Model For Your Head



- Provide:
 - Examples of images and desired outputs
 - Sequence of layers producing a $1 \times 1 \times F$ output
 - A *loss* function that measures success
- Train the network -> network figures out the parameters that makes this work

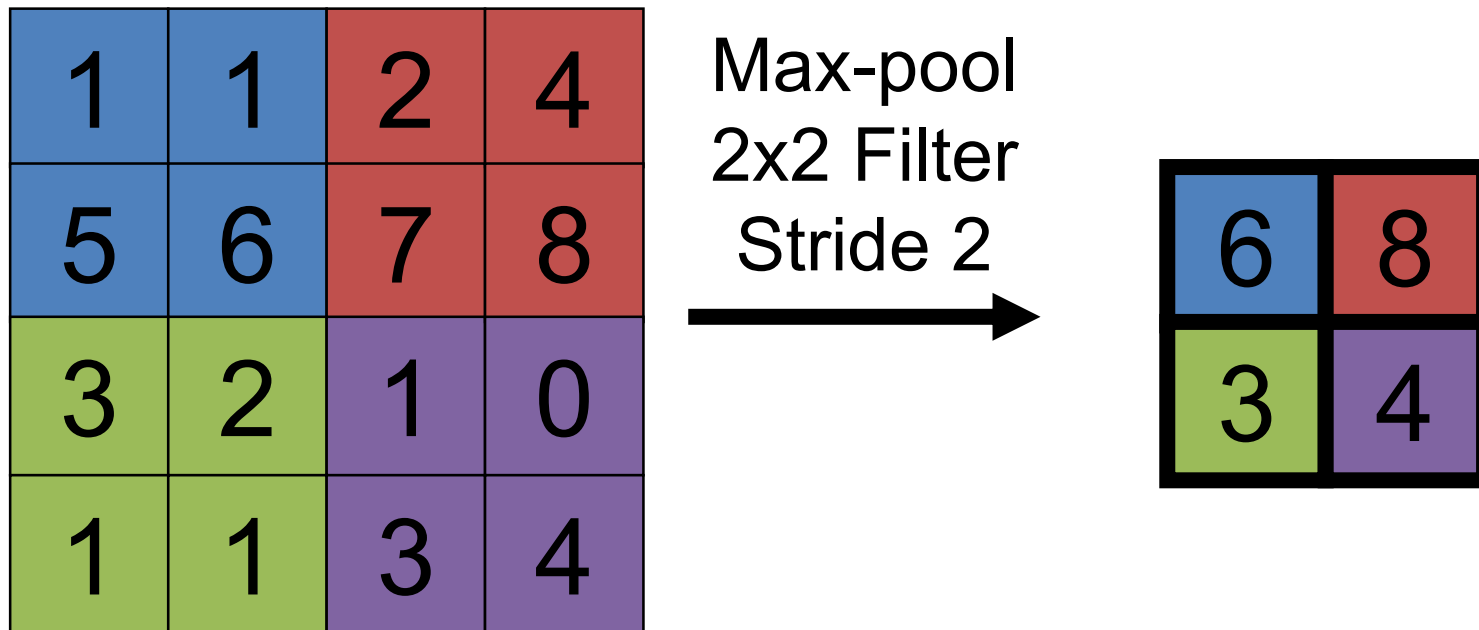
Layer Collection

You can construct functions out of layers. The only requirement is the layers “fit” together. Optimization figures out what the parameters of the layers are.

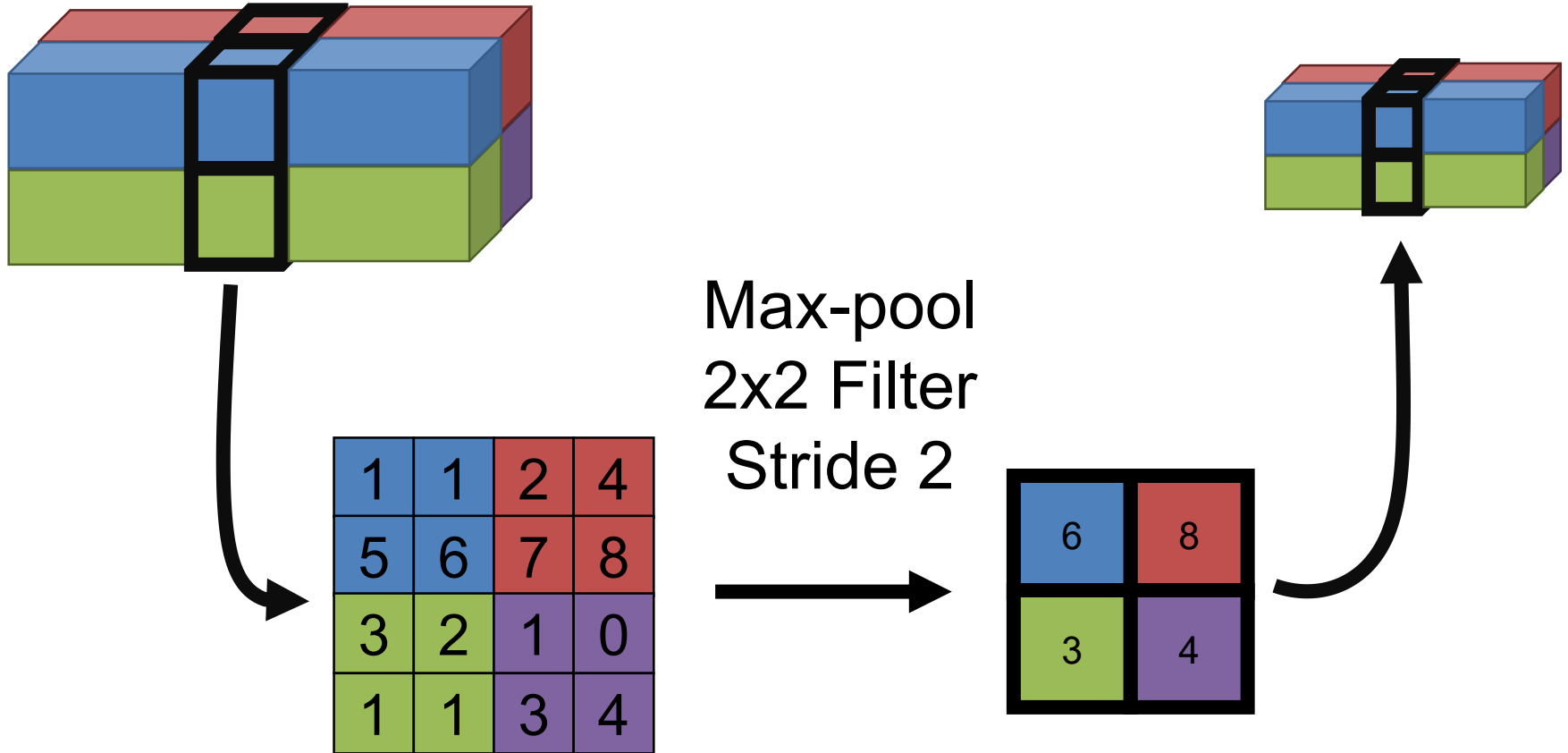


Review – Pooling

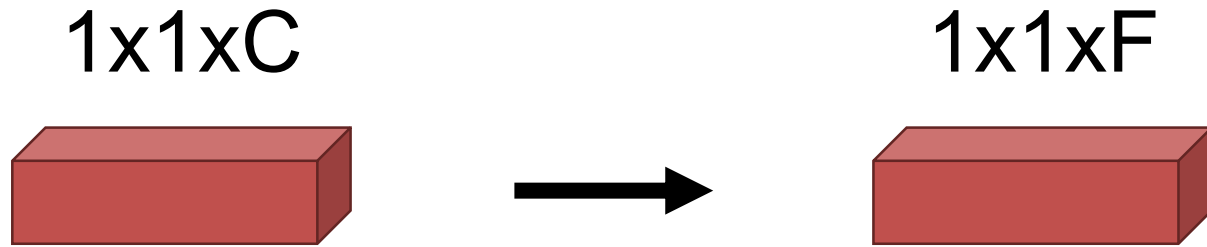
Idea: just want spatial resolution of activations
/ images smaller; applied per-channel



Review – Pooling



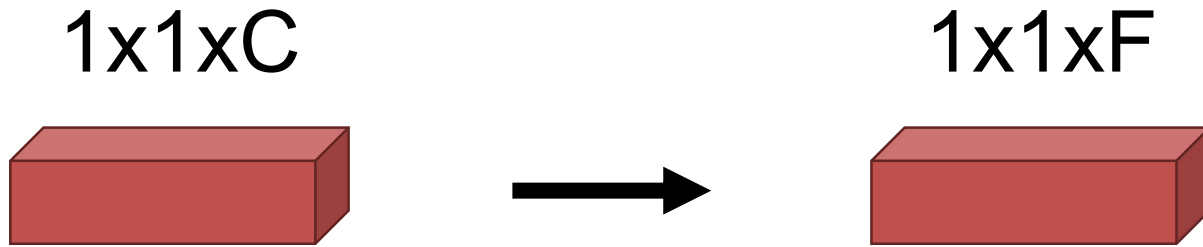
Other Layers – Fully Connected



Map C-dimensional feature to F-dimensional feature using linear transformation
 W (FxC matrix) + b (Fx1 vector)

How can we write this as a convolution?

Everything's a Convolution



Set $F_h=1$, $F_w=1$

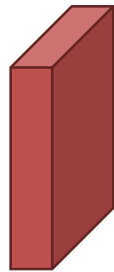
1x1 Convolution with F Filters

$$b + \sum_{i=1}^{F_h} \sum_{j=1}^{F_w} \sum_{k=1}^c F_{i,j,k} * I_{y+i,x+j,c} \longrightarrow b + \sum_{k=1}^c F_k * I_c$$

Converting to a Vector

HxWxC

1x1xF

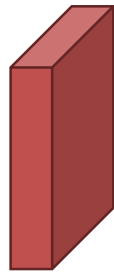


How can we do this?

Converting to a Vector* – Pool

HxWxC

1x1xF



| | | | |
|---|---|---|---|
| 1 | 1 | 2 | 4 |
| 5 | 6 | 7 | 8 |
| 3 | 2 | 1 | 0 |
| 1 | 1 | 3 | 4 |

Avg Pool
HxW Filter
Stride 1

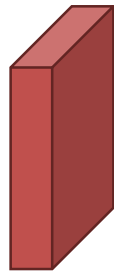


*(If $F == C$)

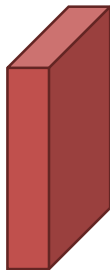
Converting to a Vector – Convolve

HxWxC

1x1xF



HxW Convolution with F Filters



*



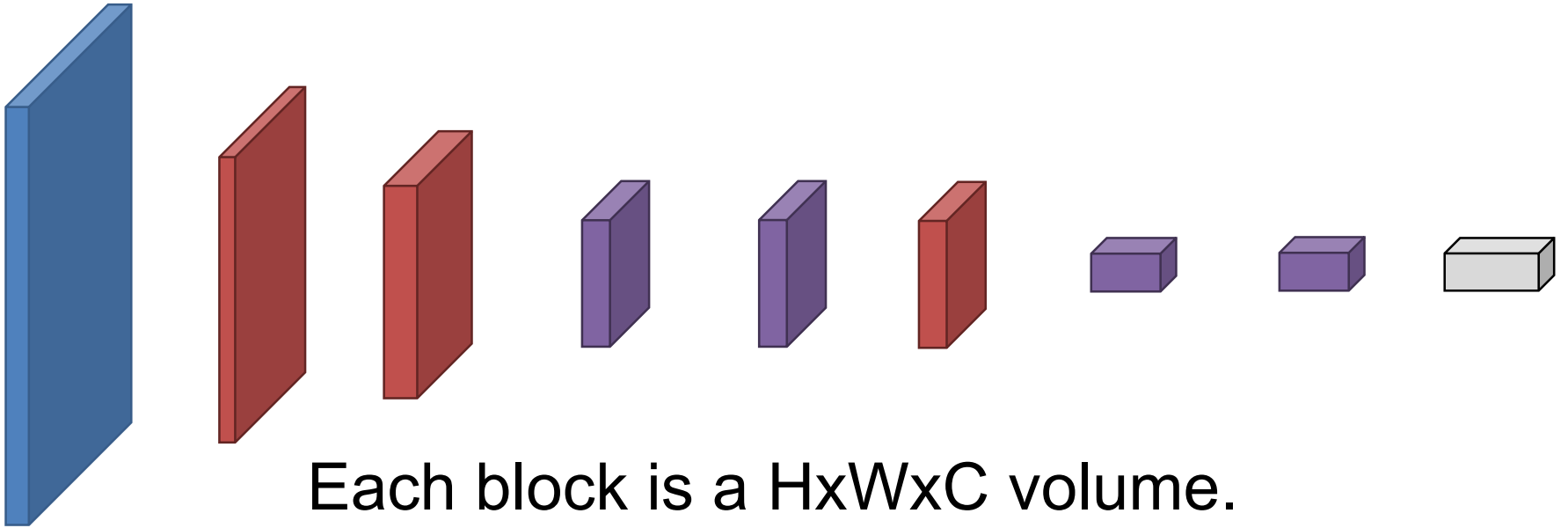
Single value
Per-filter

Looking At Networks

- We'll look at 3 landmark networks, each trained to solve a 1000-way classification output (Imagenet)
 - Alexnet (2012)
 - VGG-16 (2014)
 - Resnet (2015)

AlexNet

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |

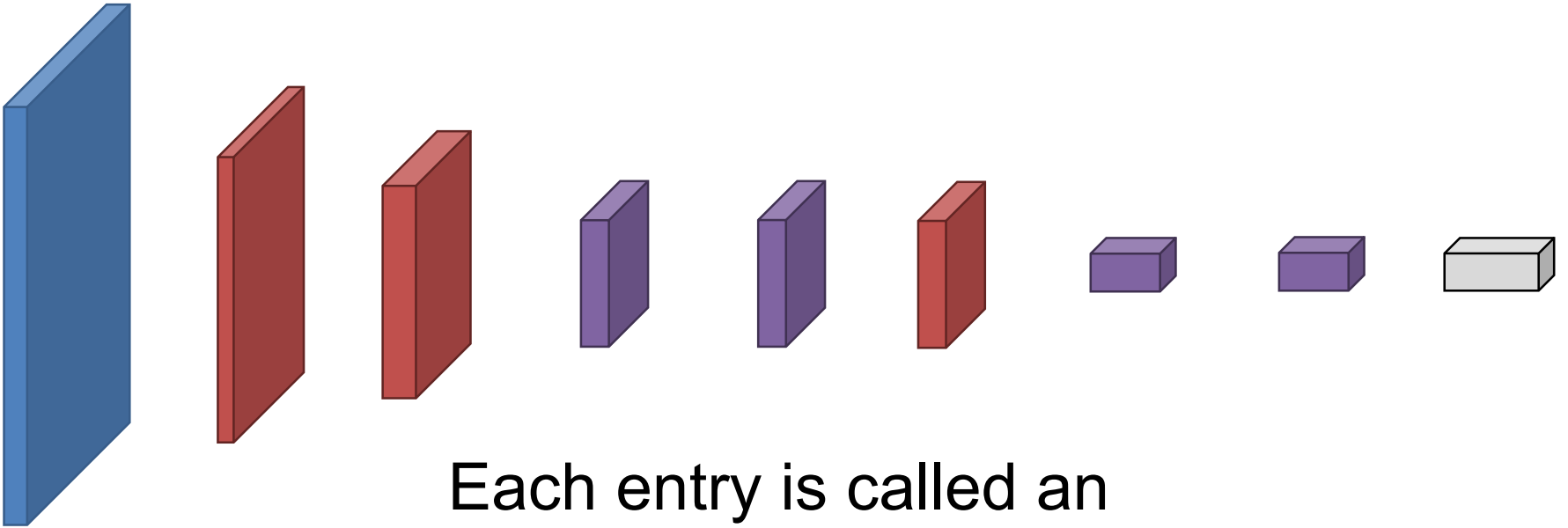


Each block is a HxWxC volume.

You transform one volume to another with convolution

CNN Terminology

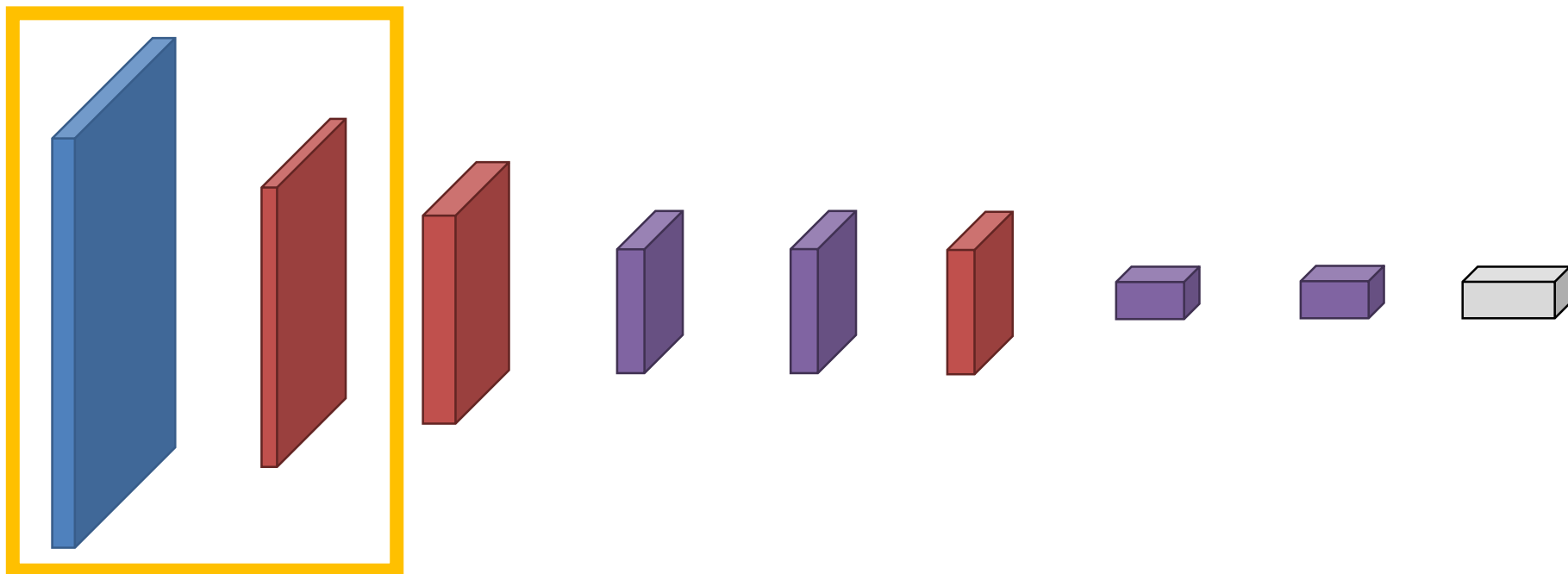
| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |



Each entry is called an
“activation”/“neuron”/“feature”

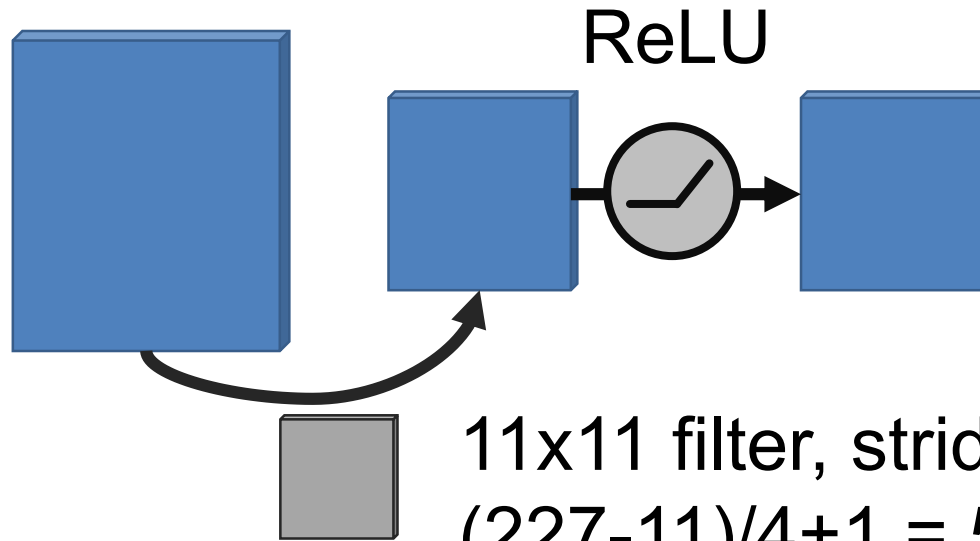
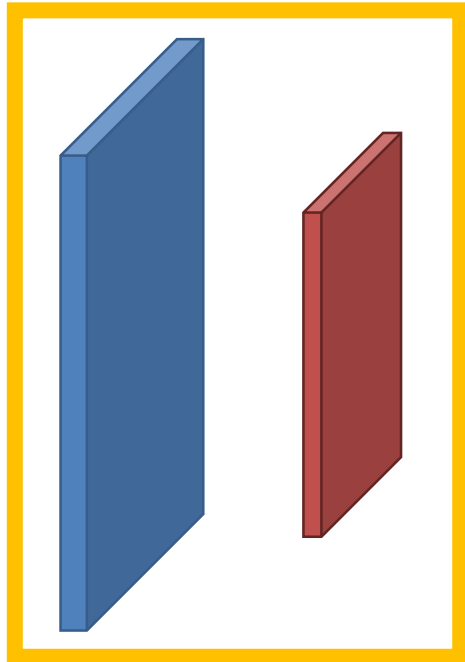
AlexNet

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |



AlexNet

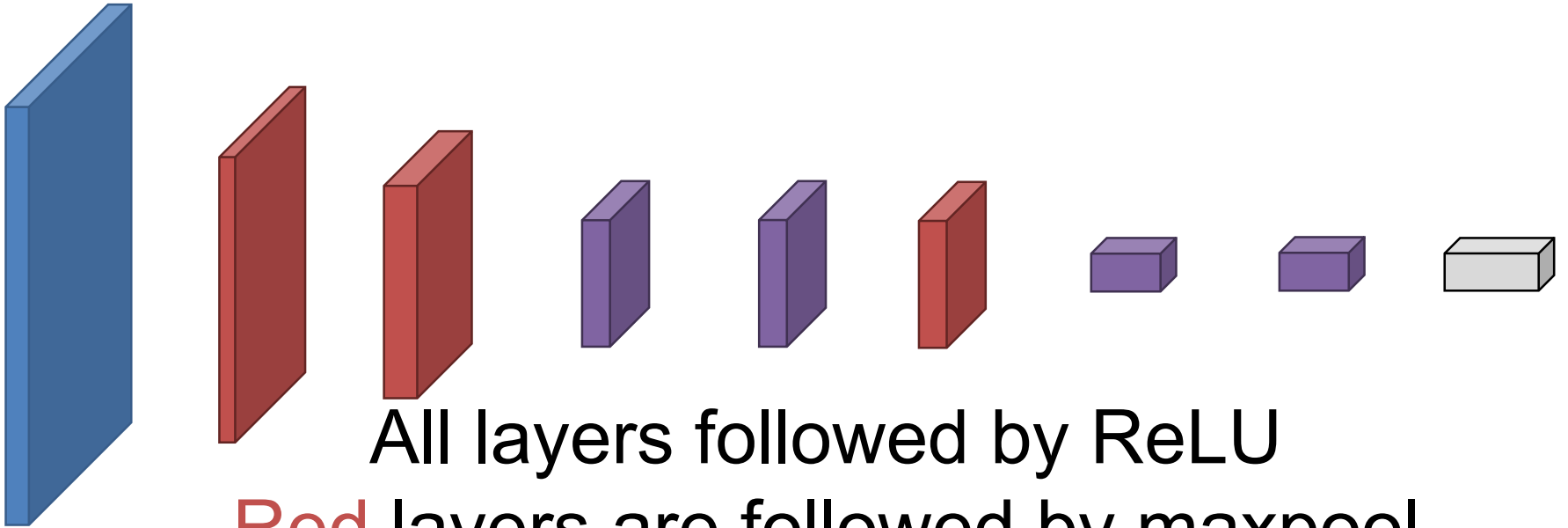
| Input | Conv 1 | | | |
|---------|--------|---------|-------|-------|
| 227x227 | 55x55 | 227x227 | 55x55 | 55x55 |
| 3 | 96 | 3 | 96 | 96 |



11x11 filter, stride of 4
 $(227-11)/4+1 = 55$

AlexNet

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |



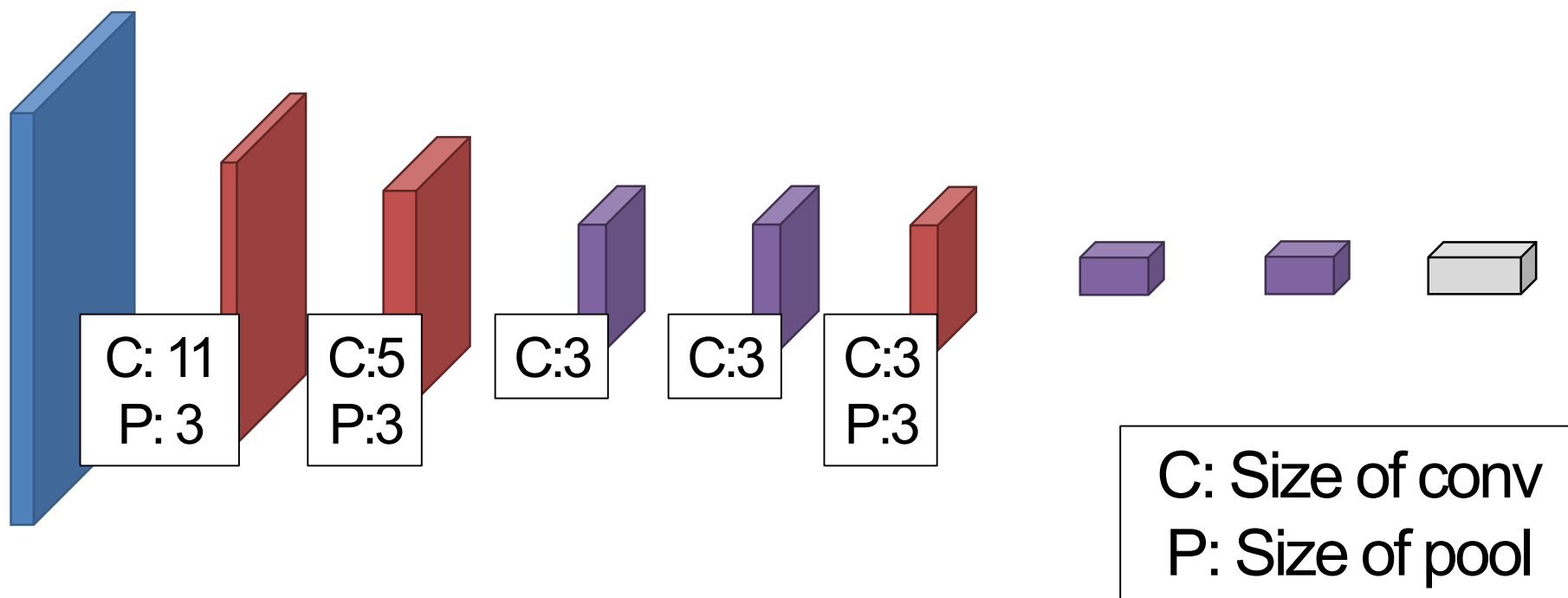
All layers followed by ReLU

Red layers are followed by maxpool

Early layers have “normalization”

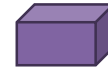
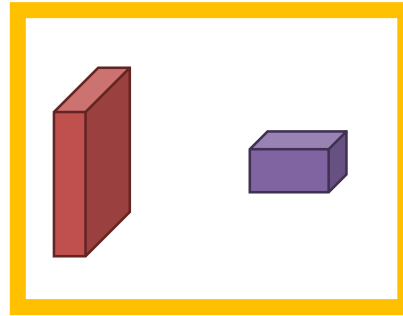
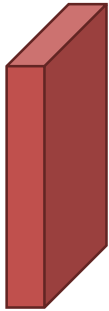
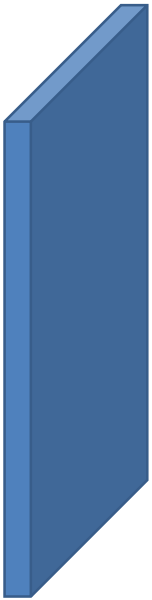
AlexNet – Details

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|---------|-----------|-----------|-----------|-----------|-----------|---------|---------|--------|
| 227x227 | 55x55 | 27x27 | 13x13 | 13x13 | 13x13 | 1x1 | 1x1 | 1x1 |
| 3 | 96 | 256 | 384 | 384 | 256 | 4096 | 4096 | 1000 |



AlexNet

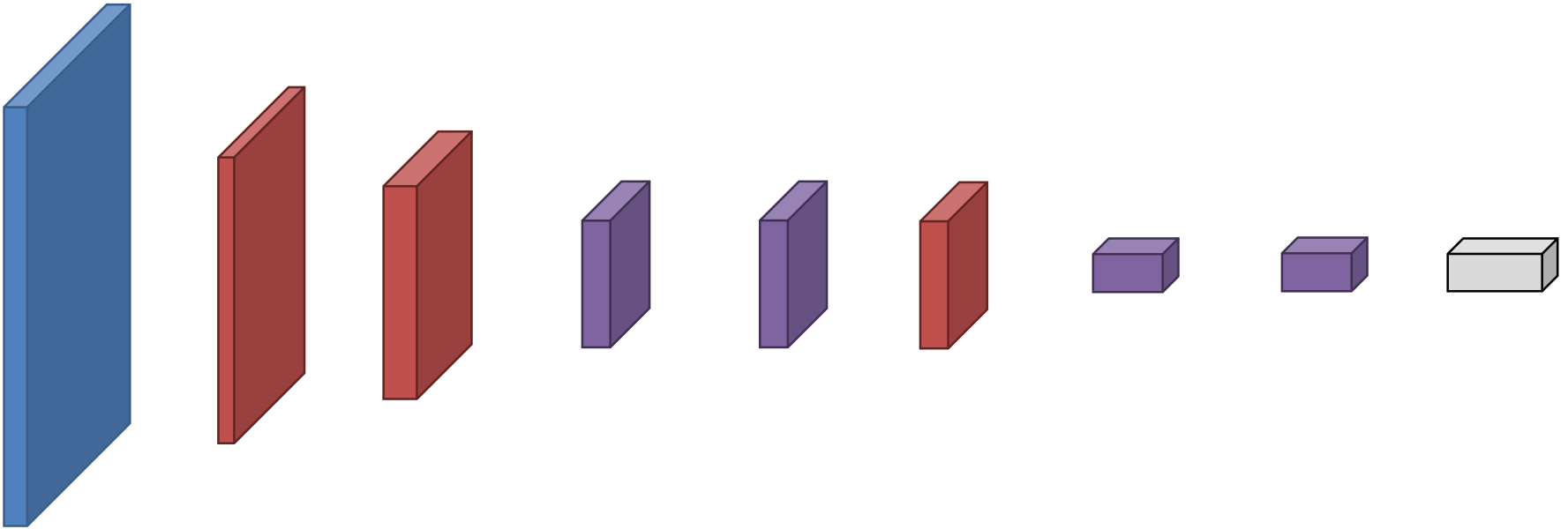
| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |



13x13 Input, 1x1 output. How?

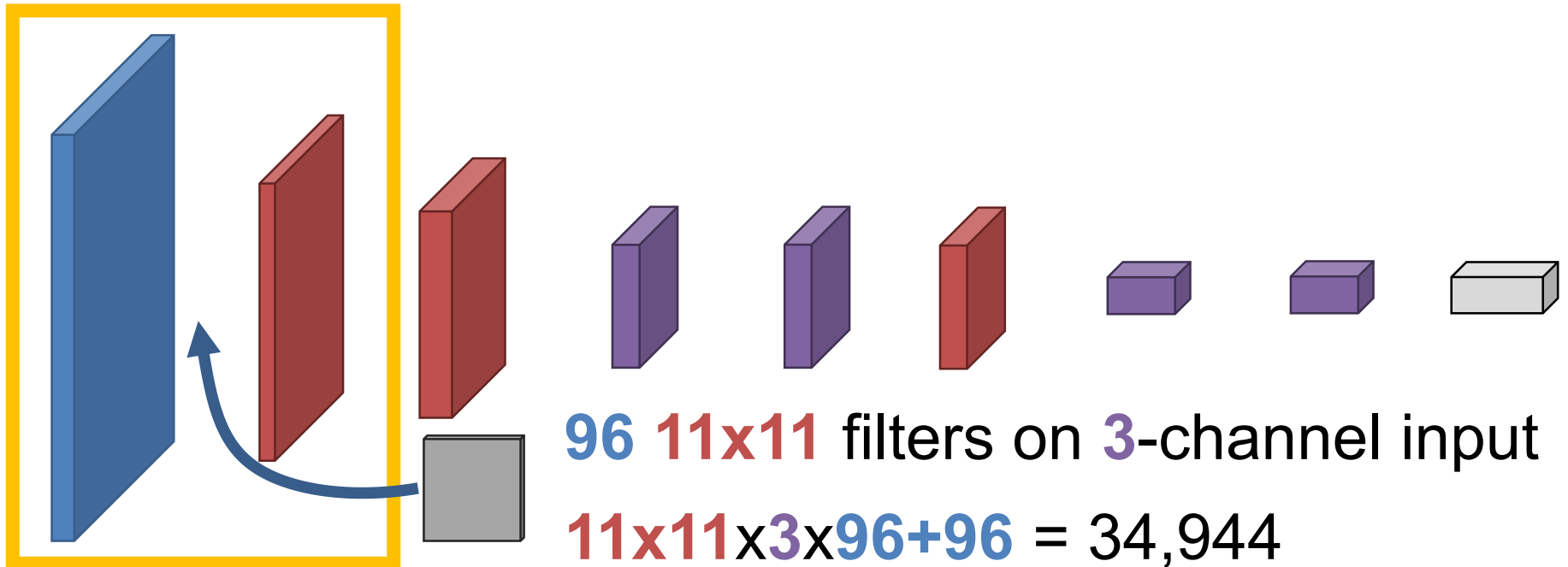
Alexnet – How Many Parameters?

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |



Alexnet – How Many Parameters?

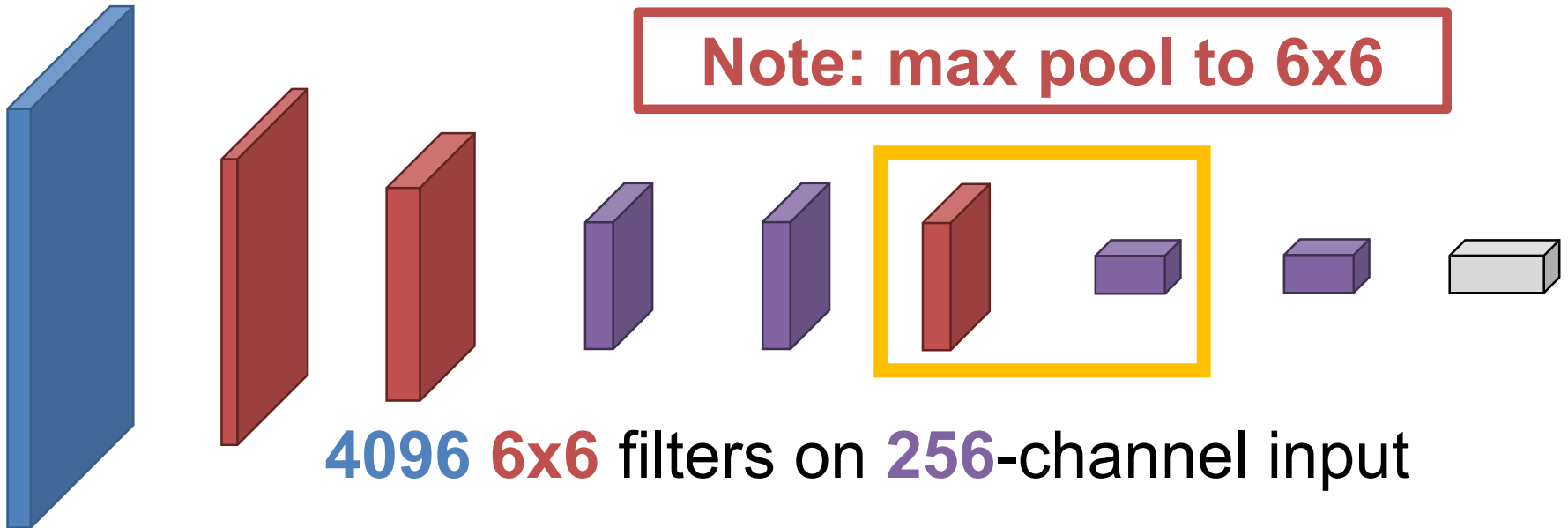
| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |



Alexnet – How Many Parameters?

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |

Note: max pool to 6x6



4096 6x6 filters on 256-channel input

$$6 \times 6 \times 256 \times 4096 + 4096 = 38 \text{ million}$$

Alexnet – How Many Parameters?

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |



4096 **1x1** filters on **4096**-channel input

$$1x1 \times 4096 \times 4096 + 4096 = 17 \text{ million}$$

Alexnet – How Many Parameters

How long would it take you to list the parameters of Alexnet at 4s / parameter?

1 year?

4 years?

8 years?

16 years?

- 62.4 million parameters
- *Vast majority in fully connected layers*
 - But... paper notes that removing the convolutions is disastrous for performance.

Dataset – ILSVRC

- Imagenet Largescale Visual Recognition Challenge
- 1.4M images
- 1000 Categories, often ridiculously precise

Dataset – ILSVRC

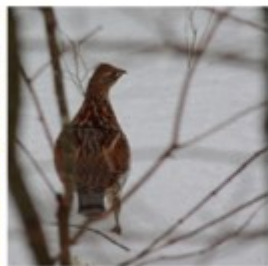
birds



flamingo



cock



ruffed grouse



quail



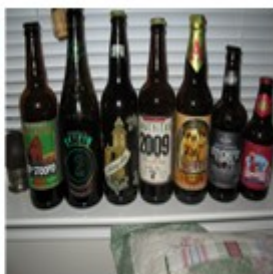
partridge

...

bottles



pill bottle



beer bottle



wine bottle



water bottle



pop bottle

...

cars



race car



wagon



minivan



jeep

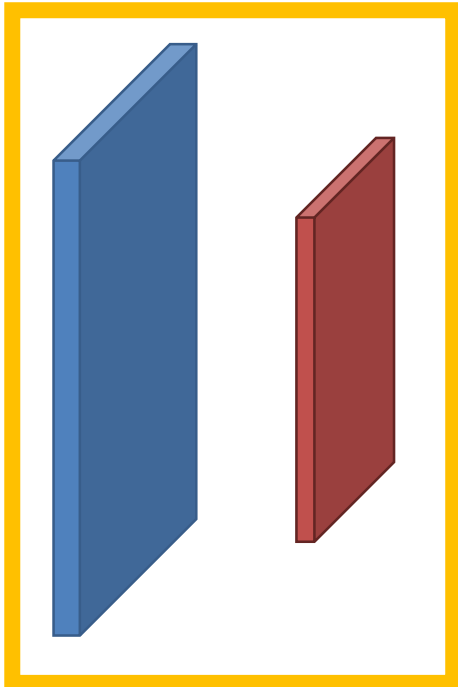


cab

...

Visualizing Filters

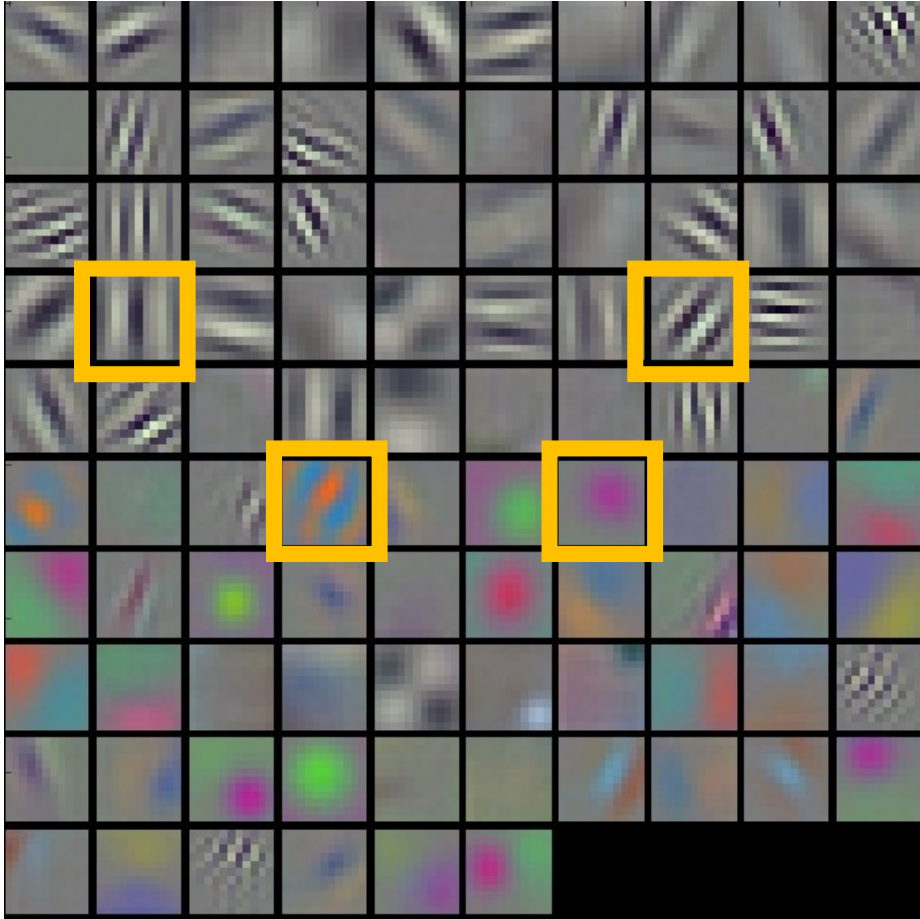
| Input | Conv |
|---------|-------|
| | 1 |
| 227x227 | 55x55 |
| 3 | 96 |



Conv 1 Filters

- **Q. How many input dimensions?**
 - A: 3
- **What does the input mean?**
 - R, G, B, duh.

What's Learned

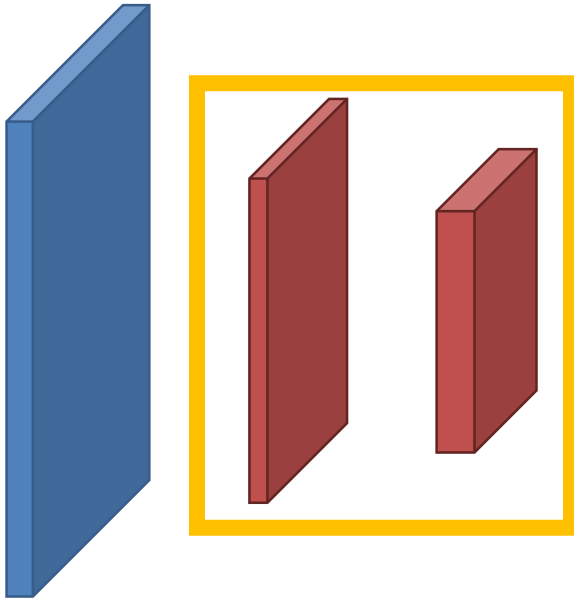


First layer filters of a network trained to distinguish 1000 categories of objects

Remember these filters go over color.

Visualizing Later Filters

| Input | Conv 1 | Conv 2 |
|---------|-----------|-----------|
| 227x227 | 55x55 | 27x27 |
| 3 | 96 | 256 |



Conv 2 Filters

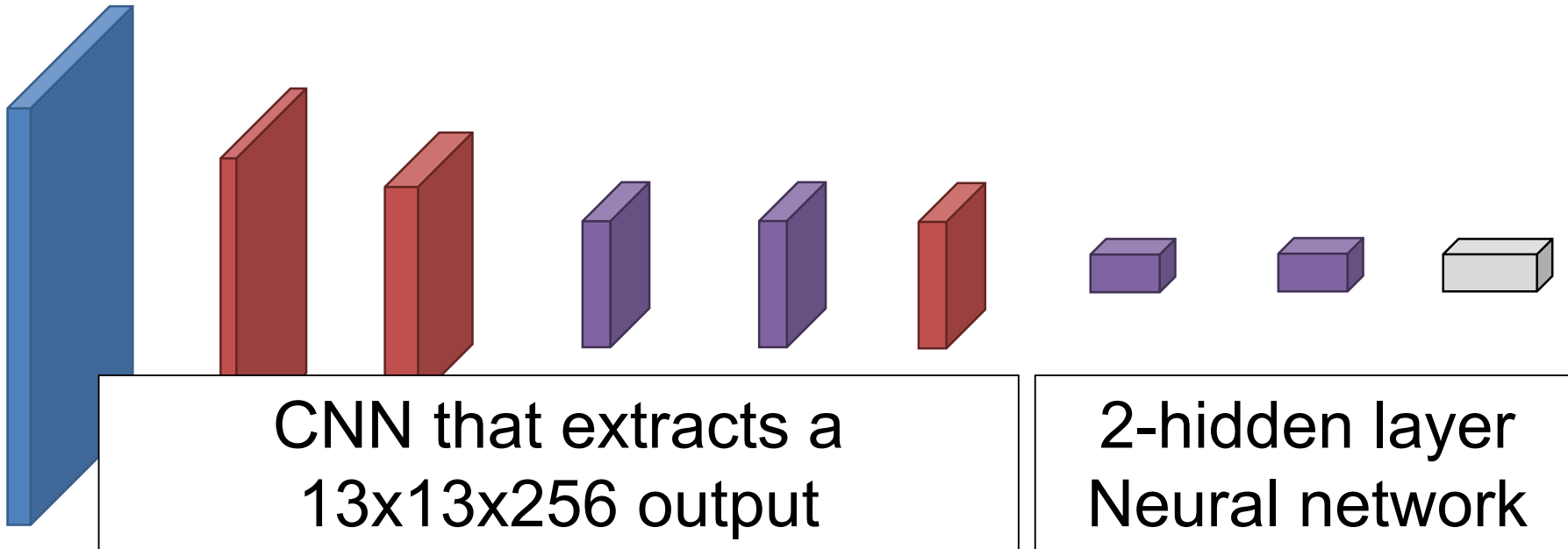
- **Q. How many input dimensions?**
 - A: 96.... hmmm
- **What does the input mean?**
 - Uh, the uh, previous slide

Visualizing Later Filters

- Understanding the meaning of the later filters *from their values* is typically impossible: too many input dimensions, not even clear what the input means.

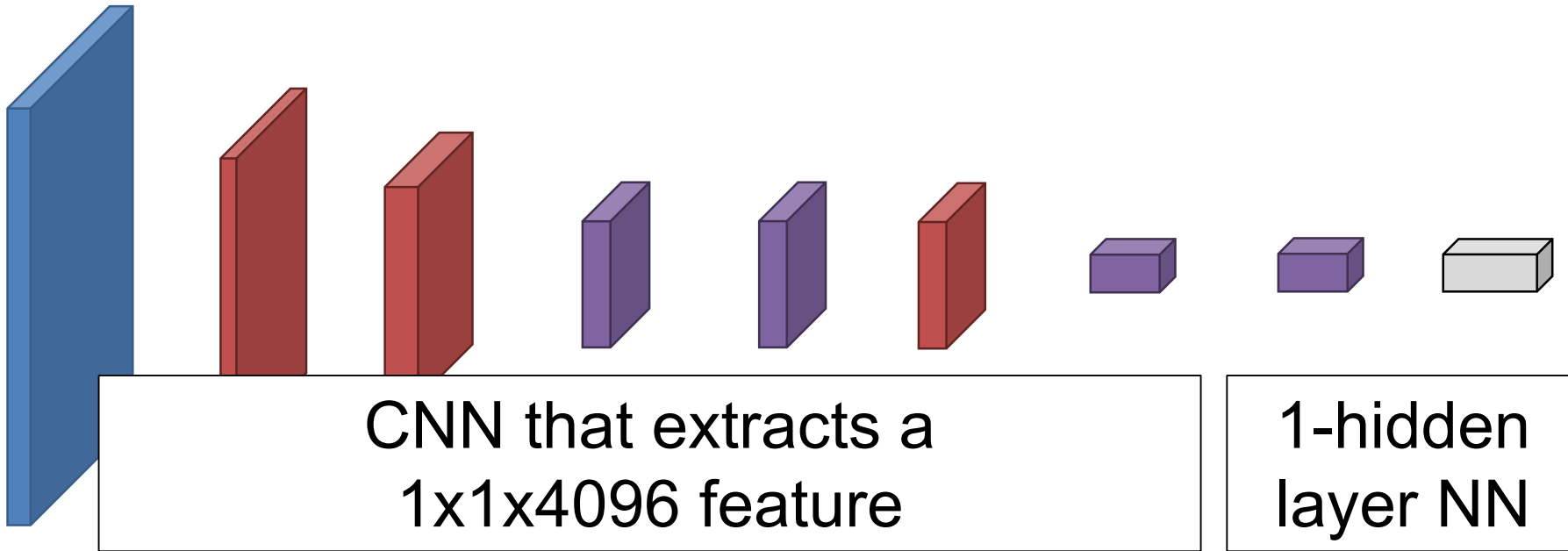
Understanding Later Filters

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |



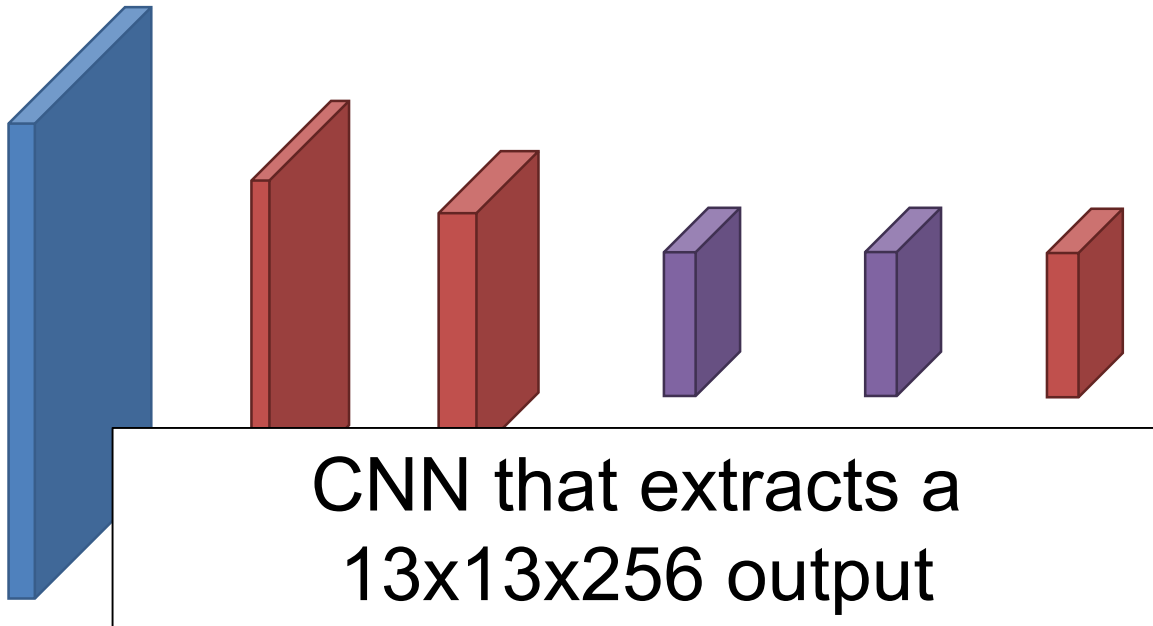
Understanding Later Filters

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |



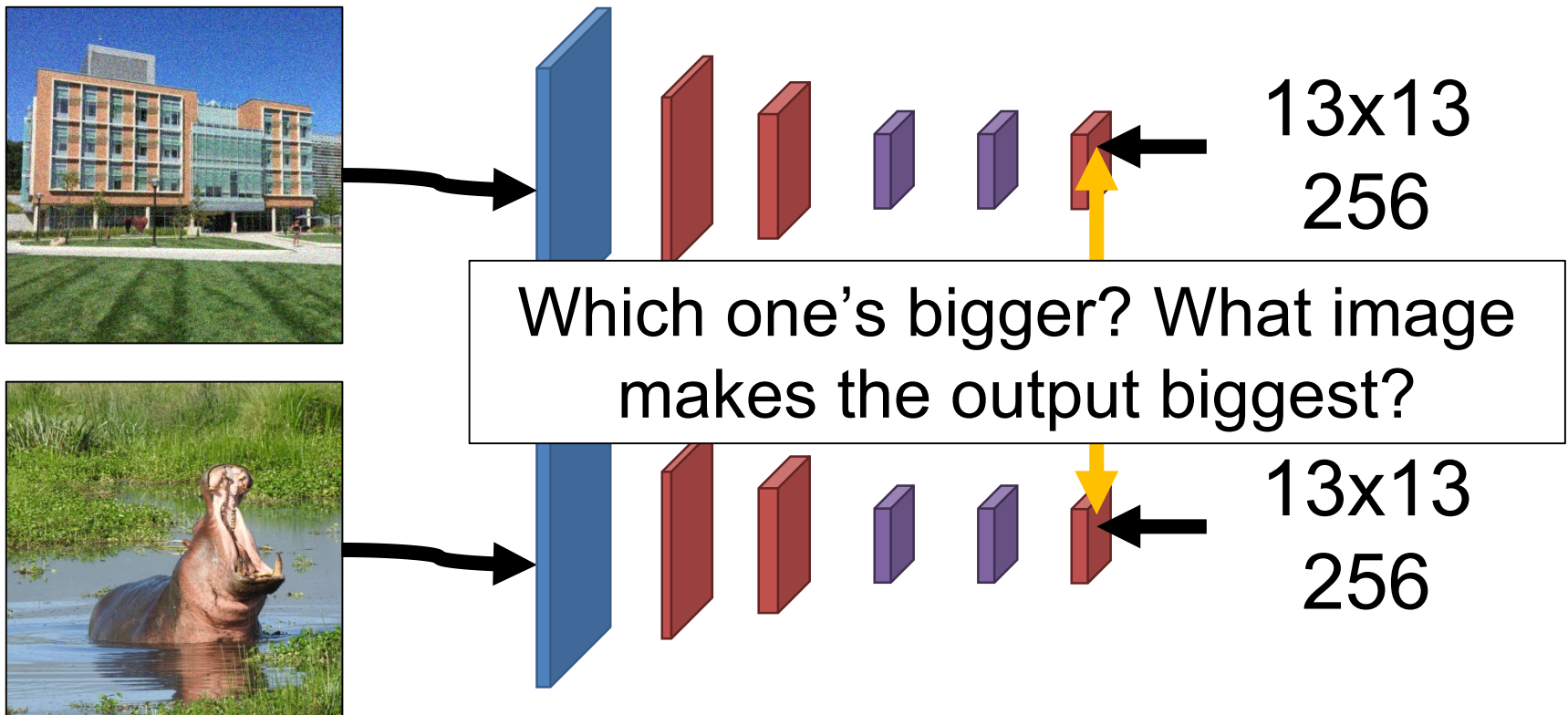
Understanding Later Filters

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 |
|--------------|-------------|--------------|--------------|--------------|--------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 |



Understanding Later Filters

Feed an image in, see what score the filter gives it. A more pleasant version of a real neuroscience procedure.



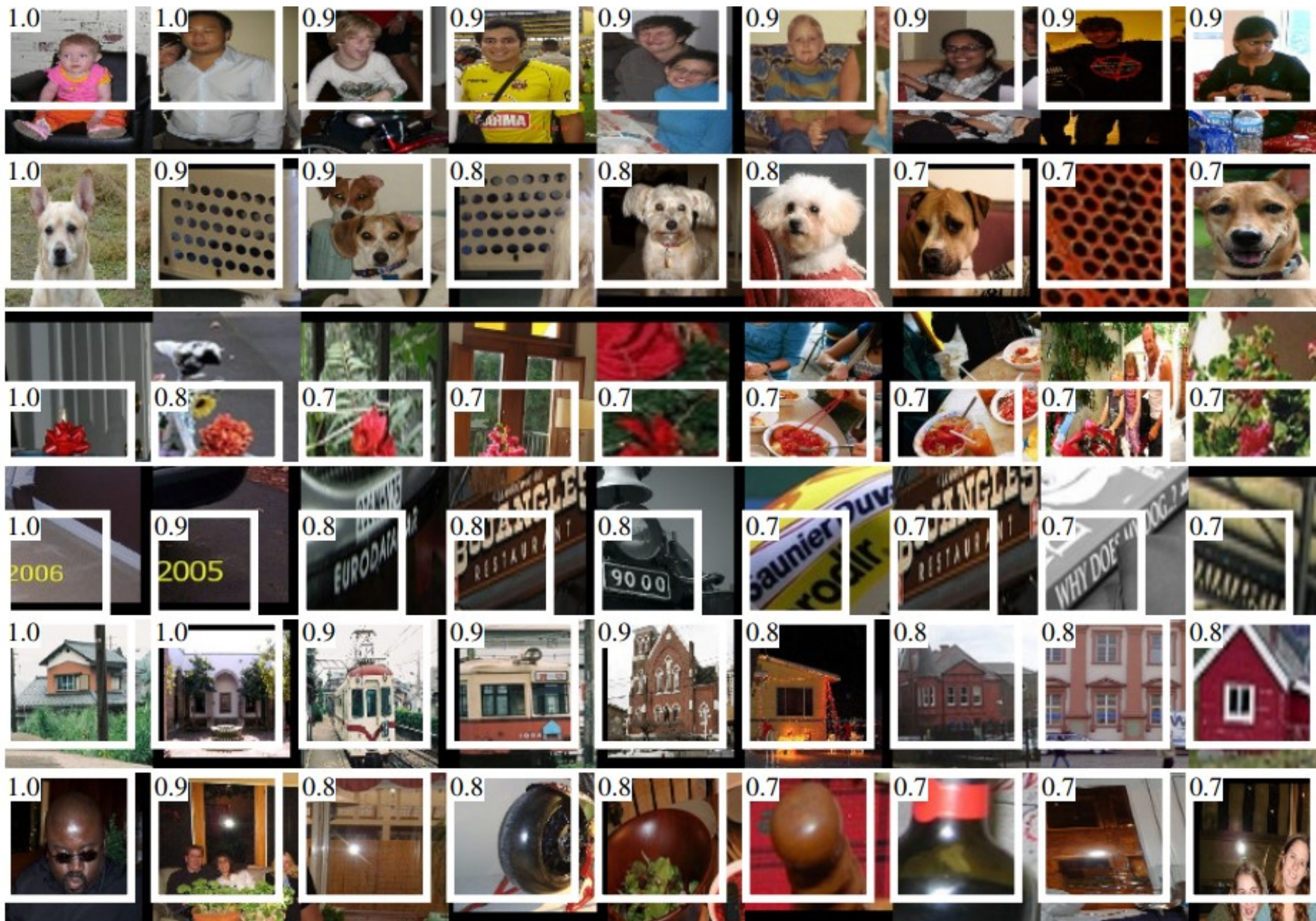
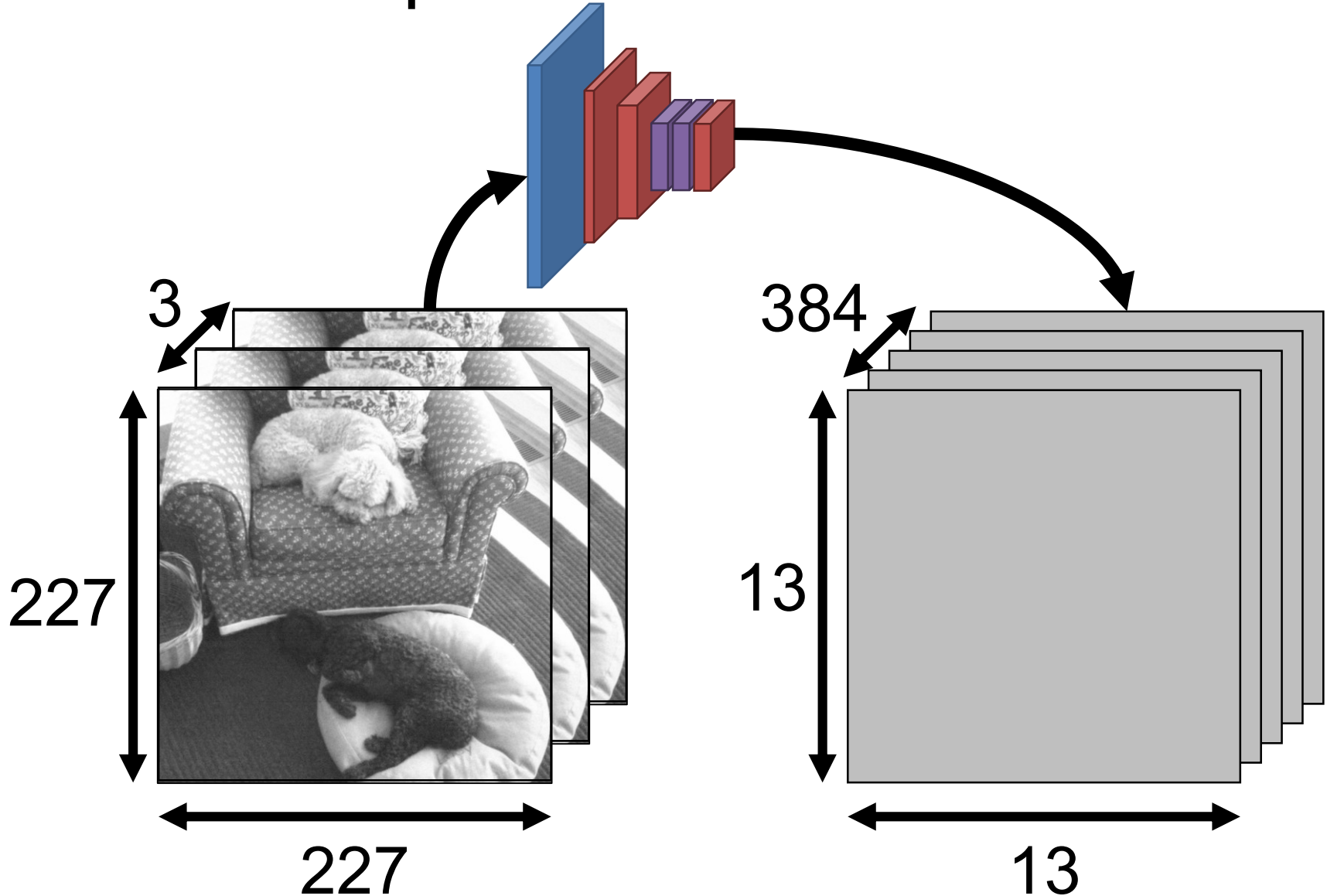
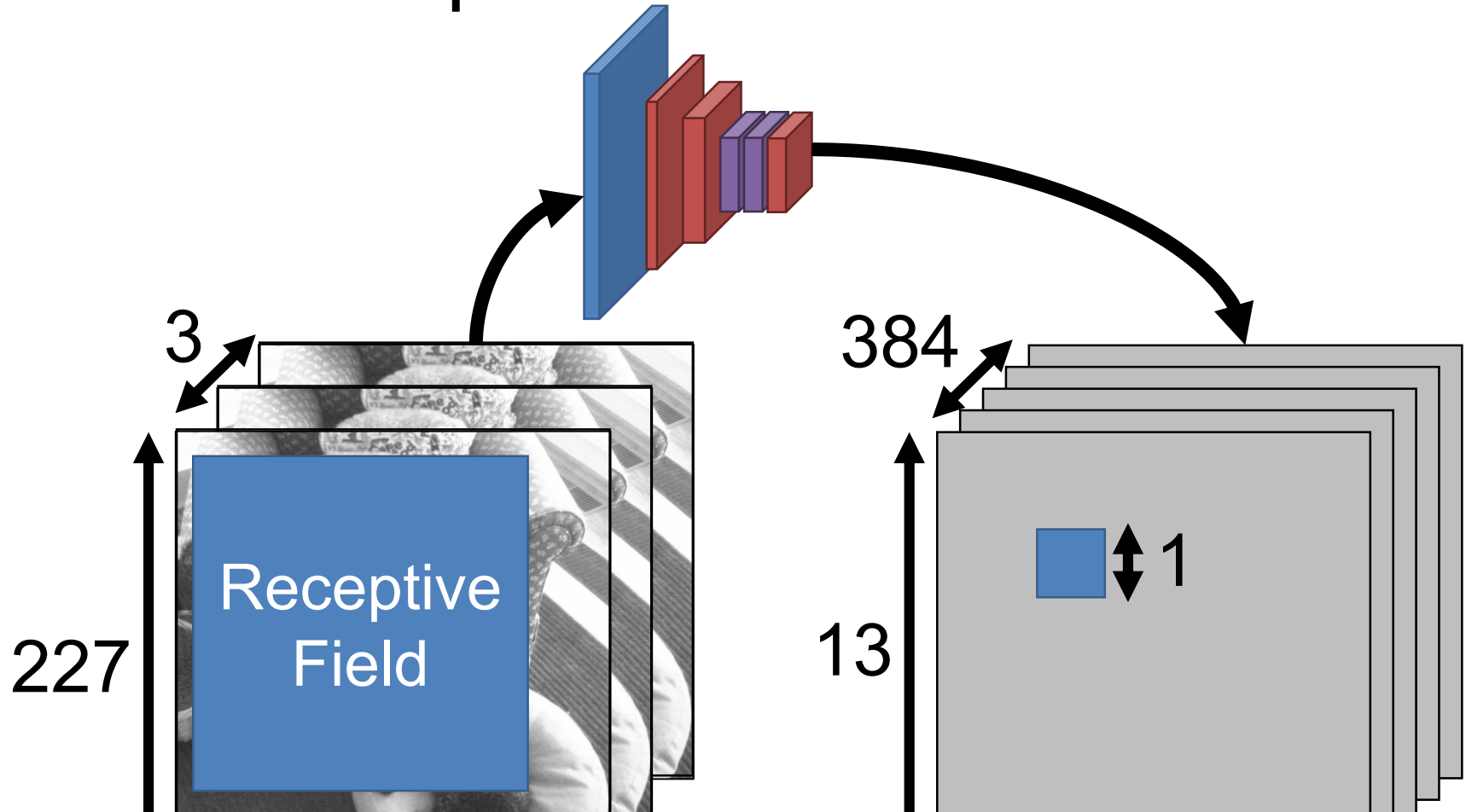


Figure Credit: Girschick et al. CVPR 2014.

What's Up With the White Boxes?



What's Up With the White Boxes?



Due to convolution, each later layer's value depends on / "sees" only a fraction of the input image.

Can use receptive fields to see where the network is “looking” to make its decisions

prison



A very active area of research
(lots of great work done by Bolei Zhou, MIT → CUHK)

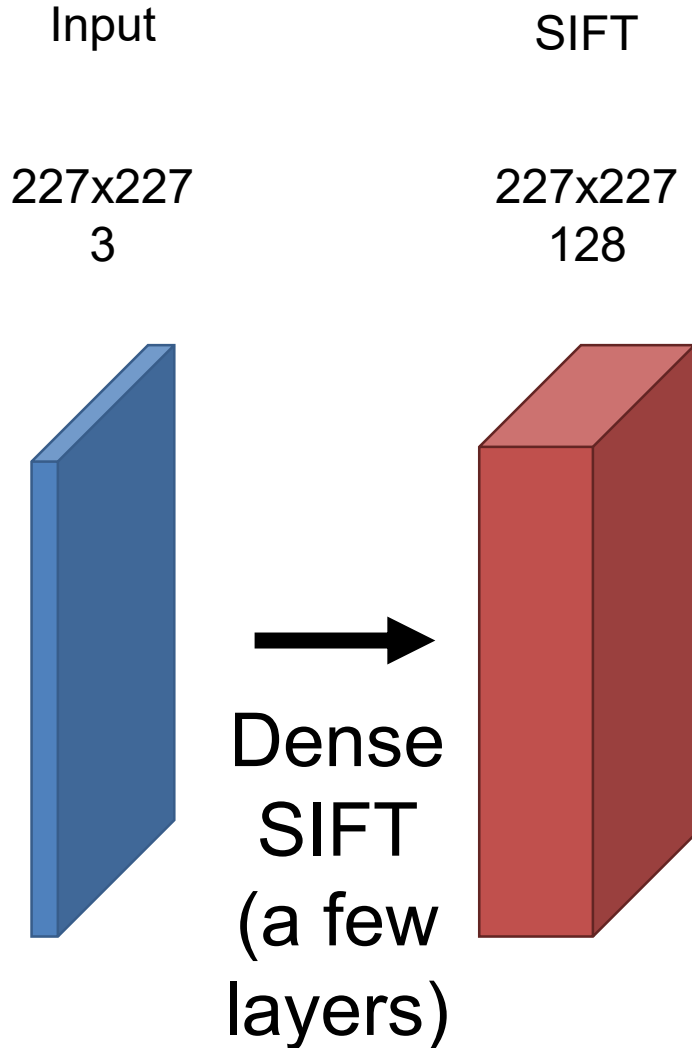
Classic Recognition

Input

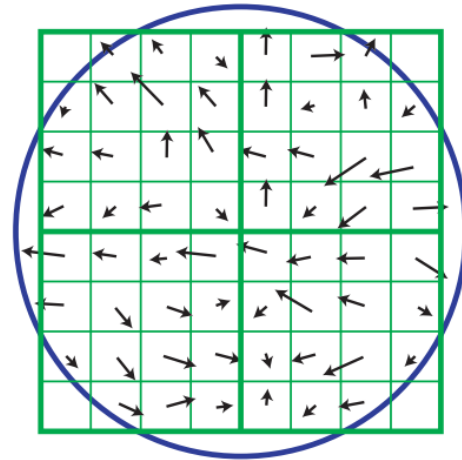
227x227
3



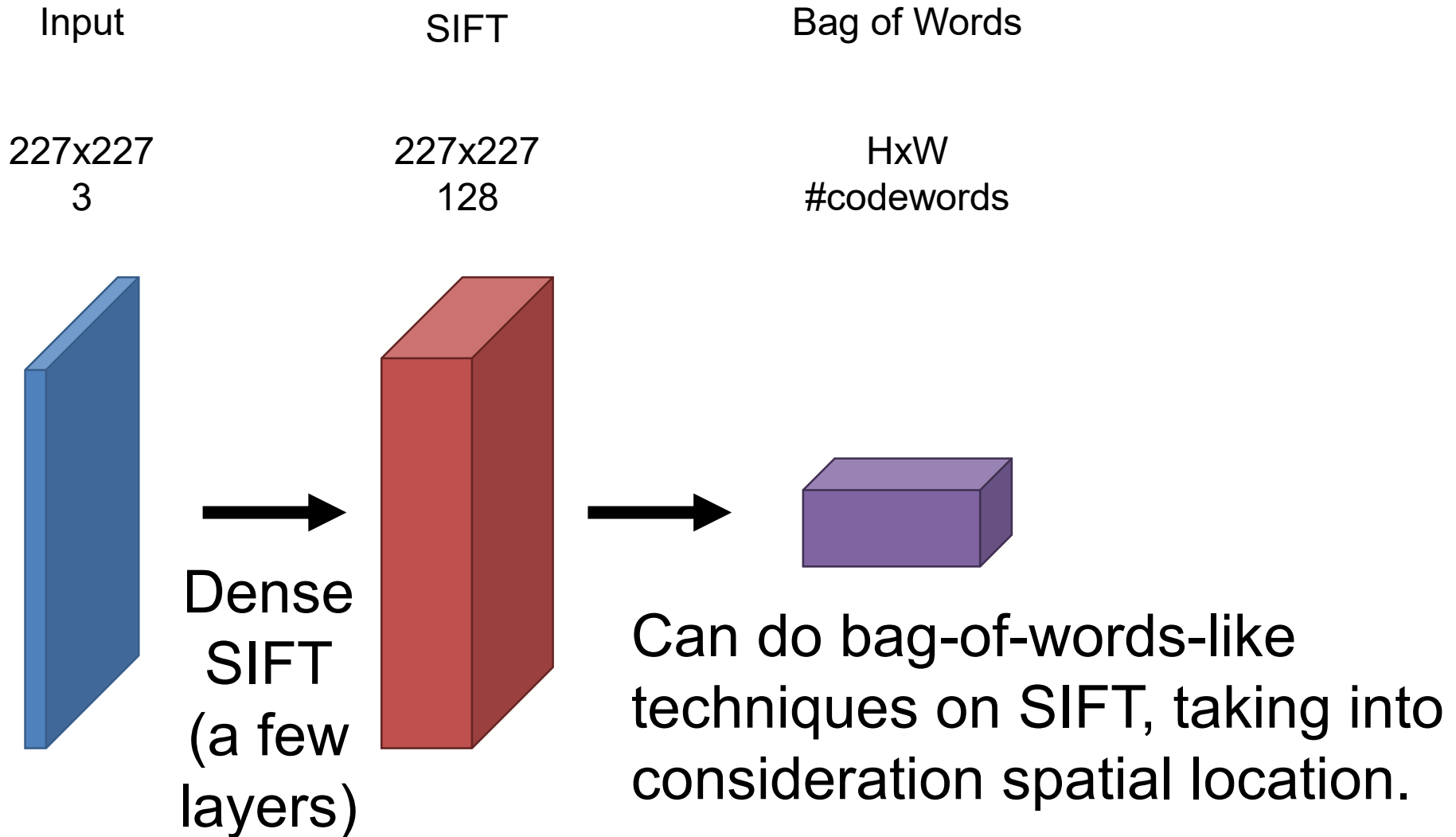
Classic Recognition



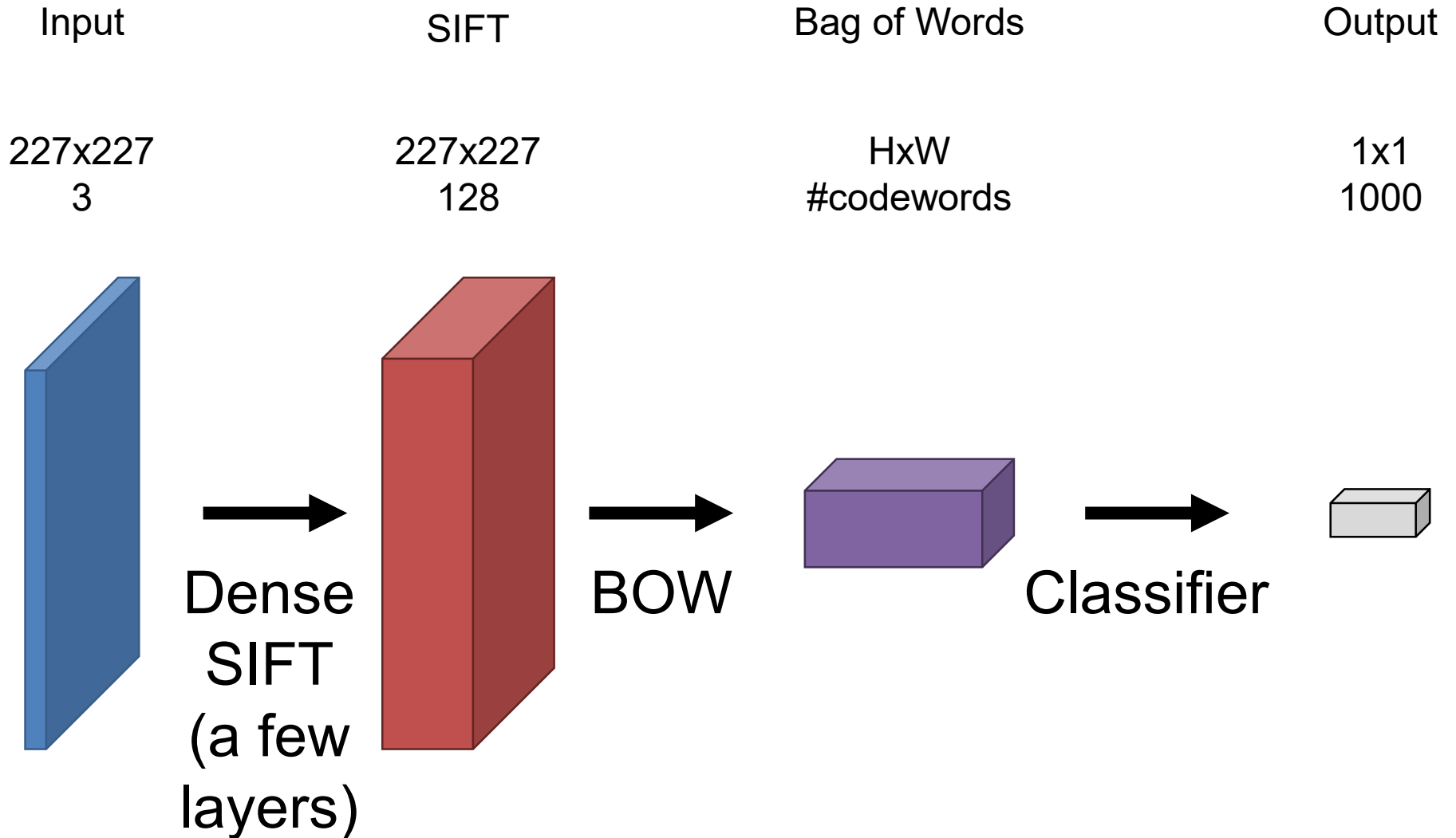
Recall: can compute a descriptor based on histograms of image gradients. Do it densely (at each pixel).



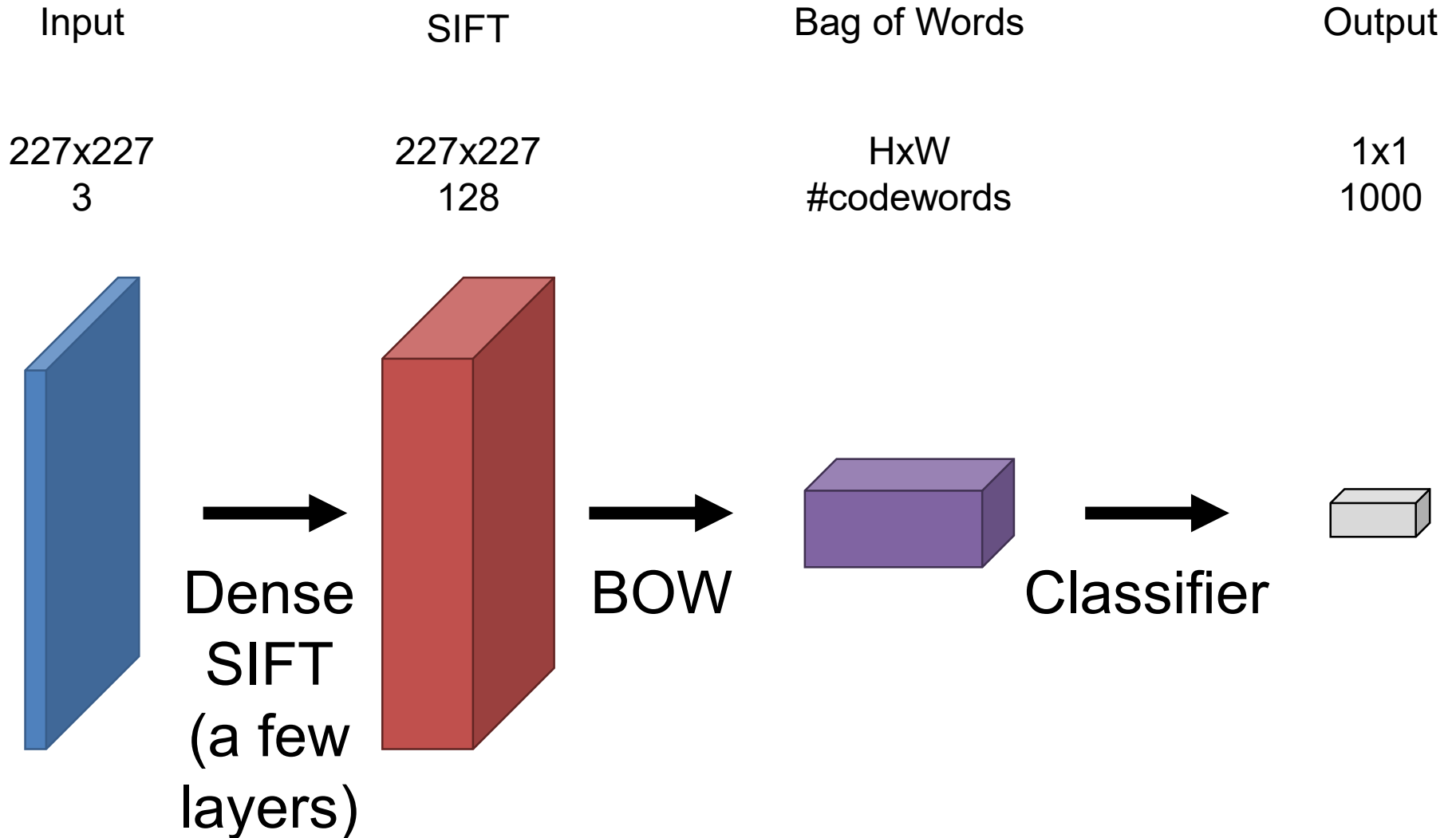
Classic Recognition



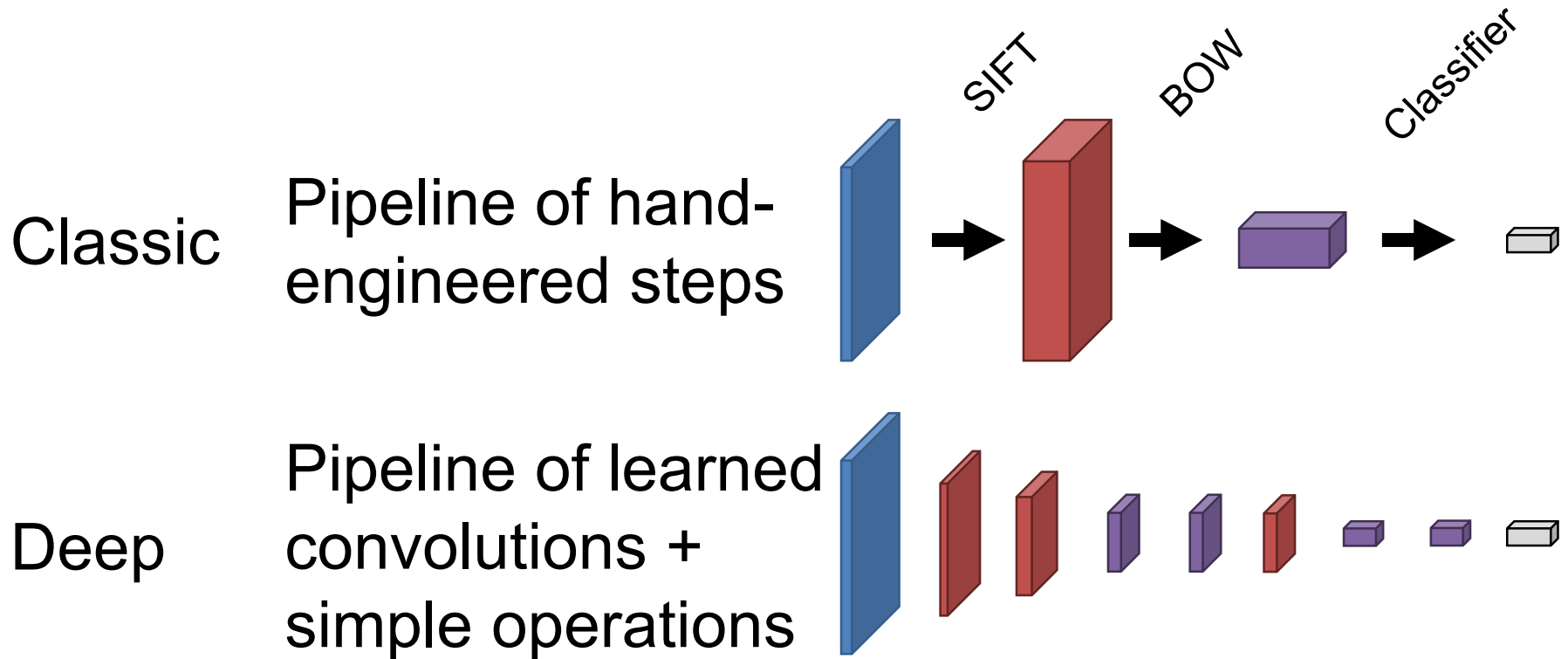
Classic Recognition



Classic Recognition



Classic vs Deep Recognition

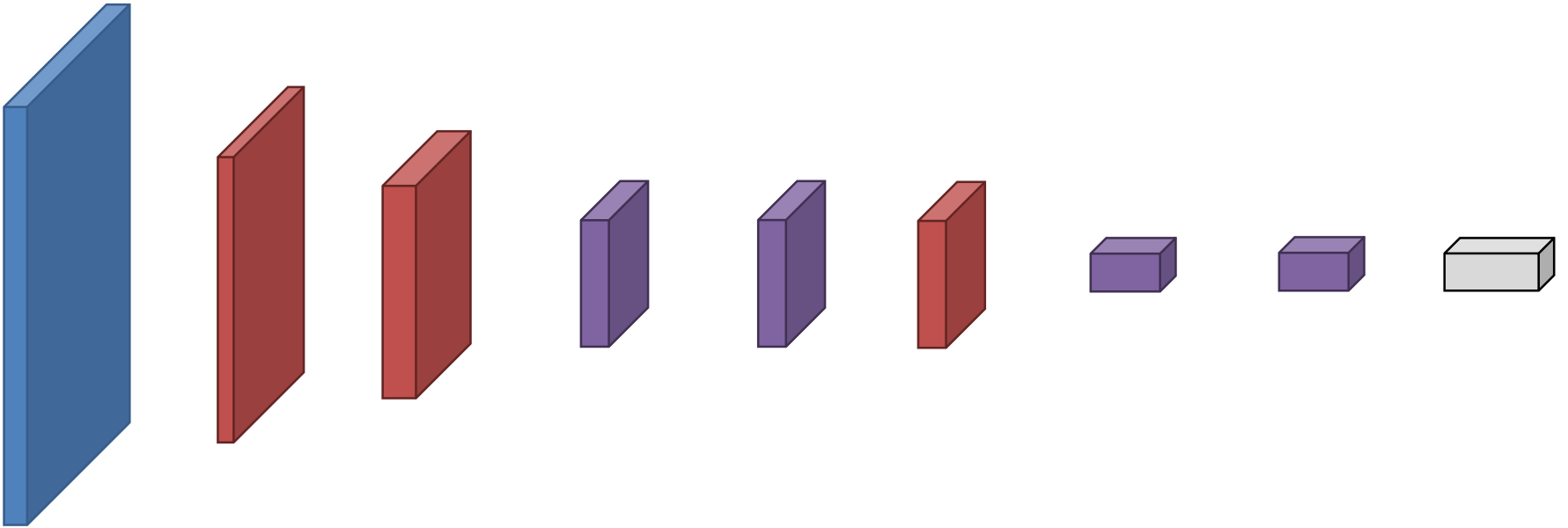


What are some differences?

The classic steps don't: talk to each other or have many parameters that are learned from data.

Last Time on EECS 442

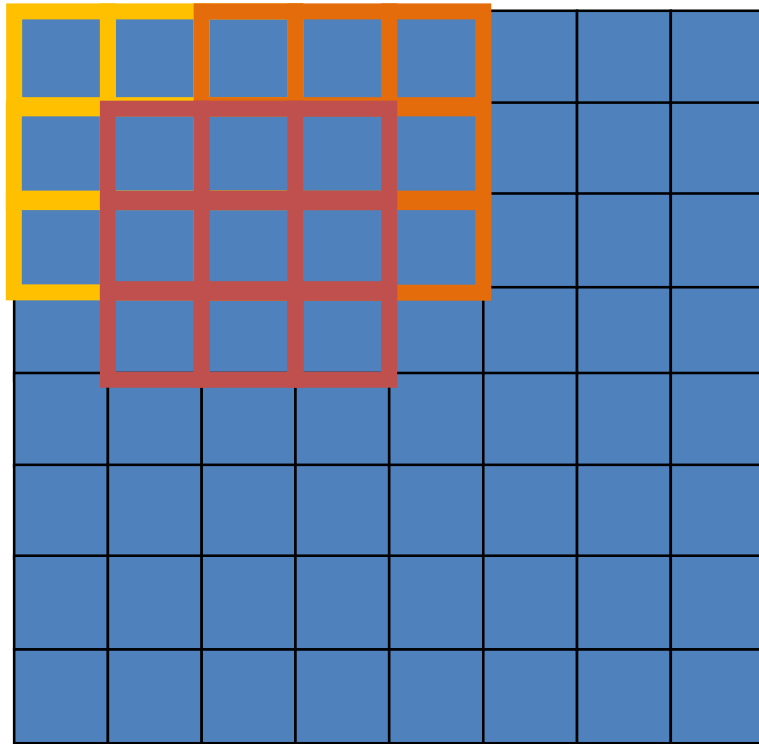
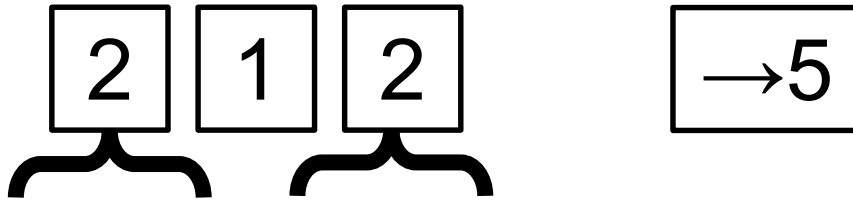
| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|-------------|--------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 227x227 3 | 55x55 96 | 27x27 256 | 13x13 384 | 13x13 384 | 13x13 256 | 1x1 4096 | 1x1 4096 | 1x1 1000 |



3 Key Developments Since Alexnet

- 3x3 Filters
- Batch Normalization
- Residual Learning

Key Idea – 3x3 Filters

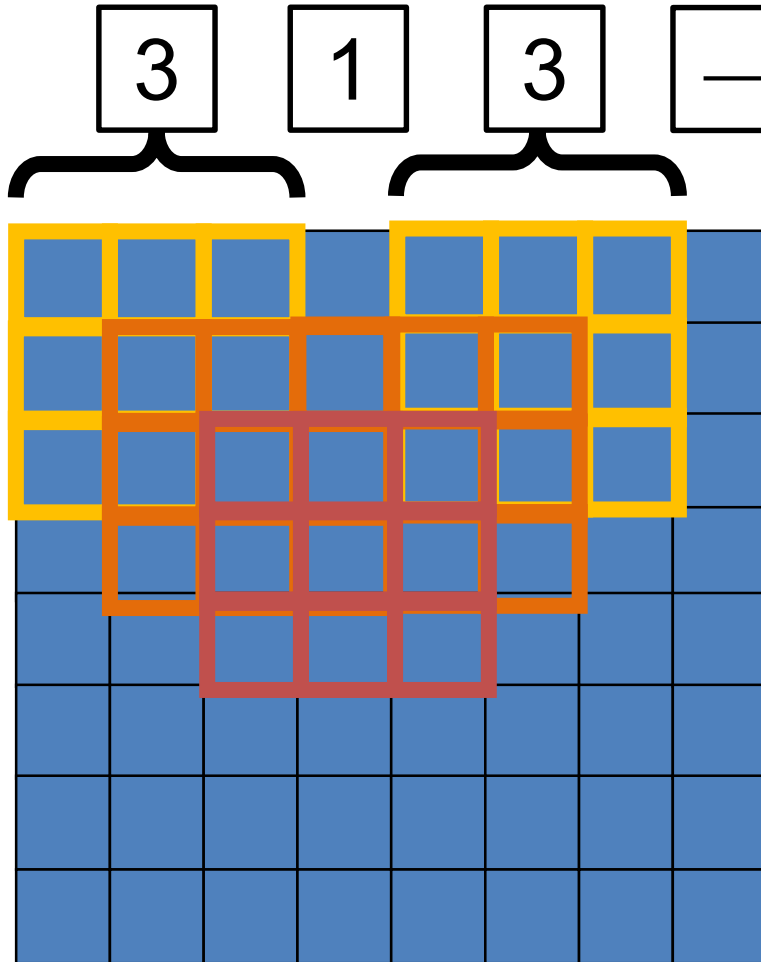


3x3 filter followed by
3x3 filter



Filter with 5x5
receptive field

Key Idea – 3x3 Filters

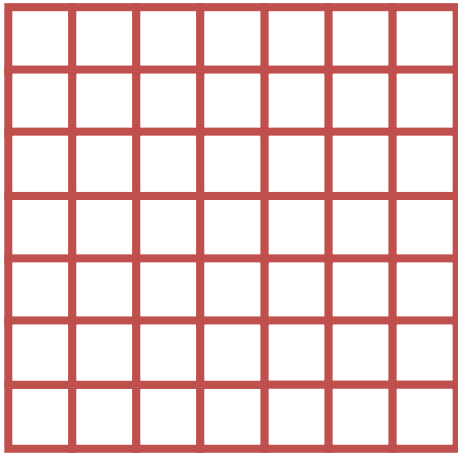


3x3 filter followed by
3x3 filter followed by
3x3 filter

→

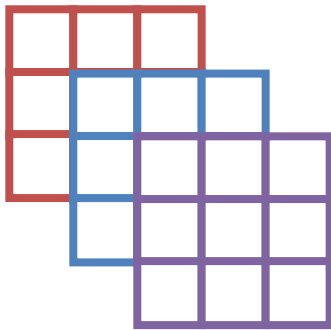
Filter with 7x7
receptive field

Why Does This Make A Difference?

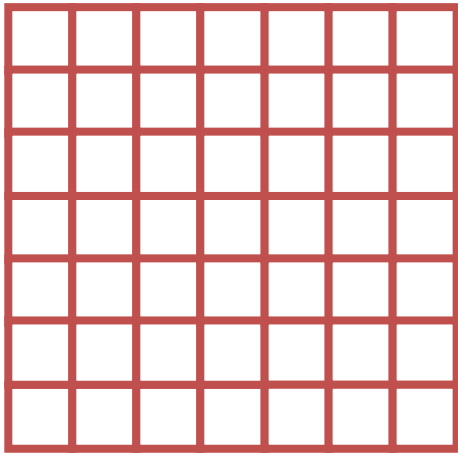


Empirically, repeated 3x3 filters do better compared to a 7x7 filter.

Why?



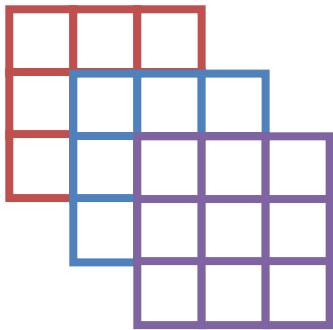
Key Idea – 3x3 Filters



Receptive Field: 7x7 pixels

Parameters/channel: 49

Number of ReLUs: 1



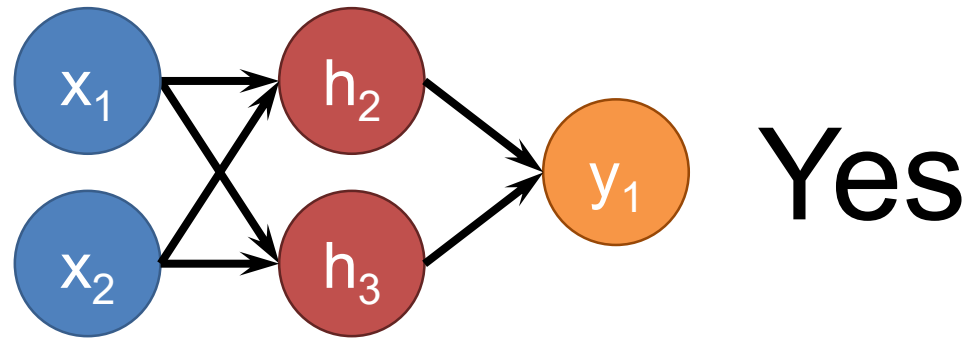
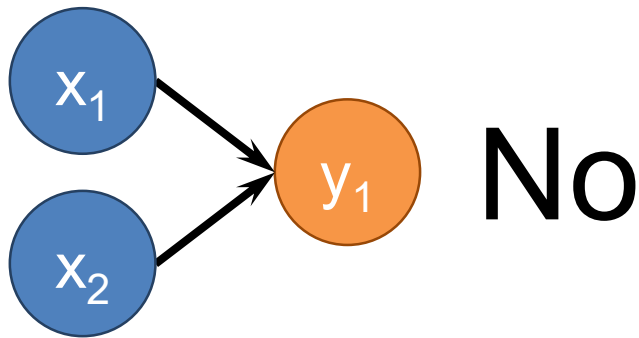
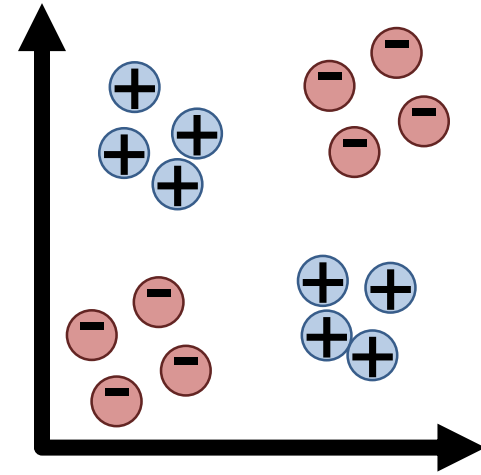
Receptive Field: 7x7 pixels

Parameters/channel: $3 \times 3 \times 3 = \mathbf{27}$

Number of ReLUs: **3**

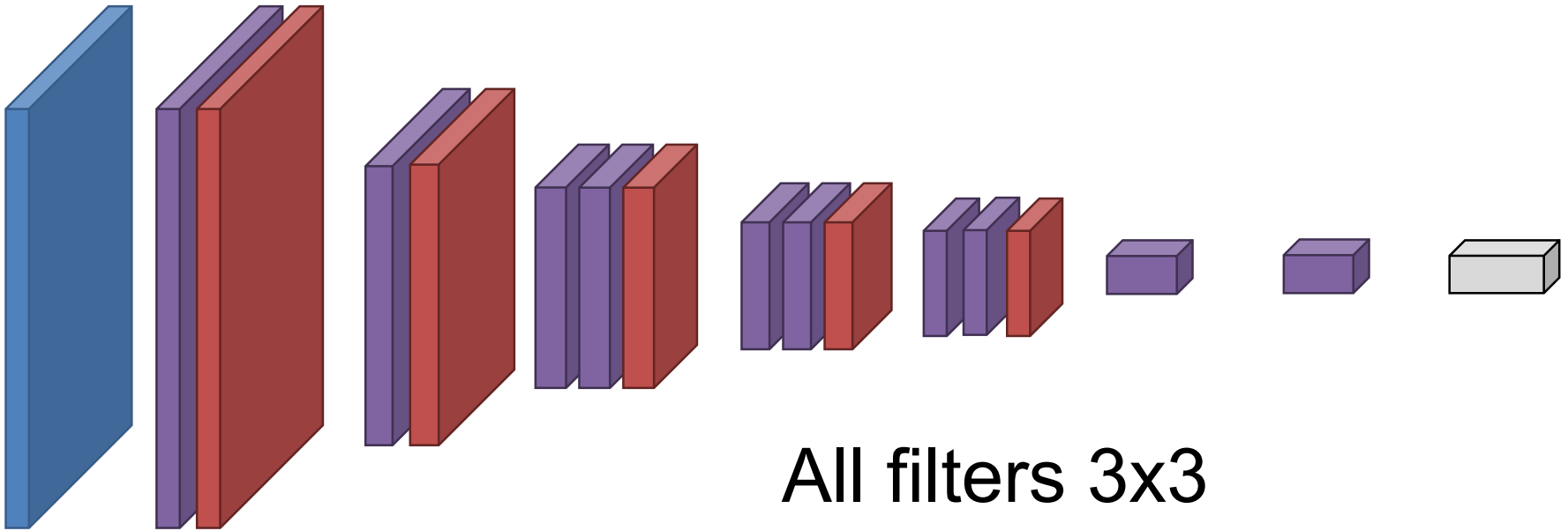
We Want More Non-linearity!

Can they implement xor?



VGG16

| Input | Conv 1 | Conv 2 | Conv 3 | Conv 4 | Conv 5 | FC 6 | FC 7 | Output |
|--------------|---------------|----------------|--------------|--------------|--------------|-------------|-------------|-------------|
| 224x224 3 | 224x224 64 | 112x112 128 | 56x56 256 | 28x28 512 | 14x14 512 | 1x1 4096 | 1x1 4096 | 1x1 1000 |

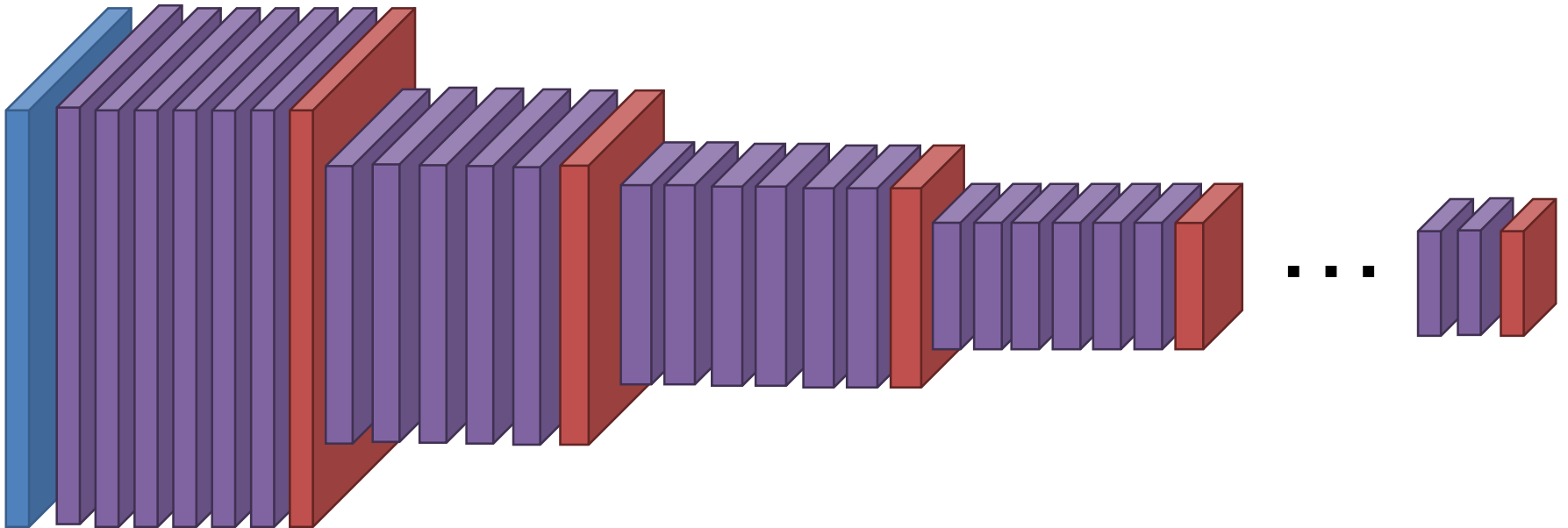


All filters 3x3
All filters followed by ReLU

Training Deeper Networks

Why not just stack continuously?

What will happen to gradient going back?



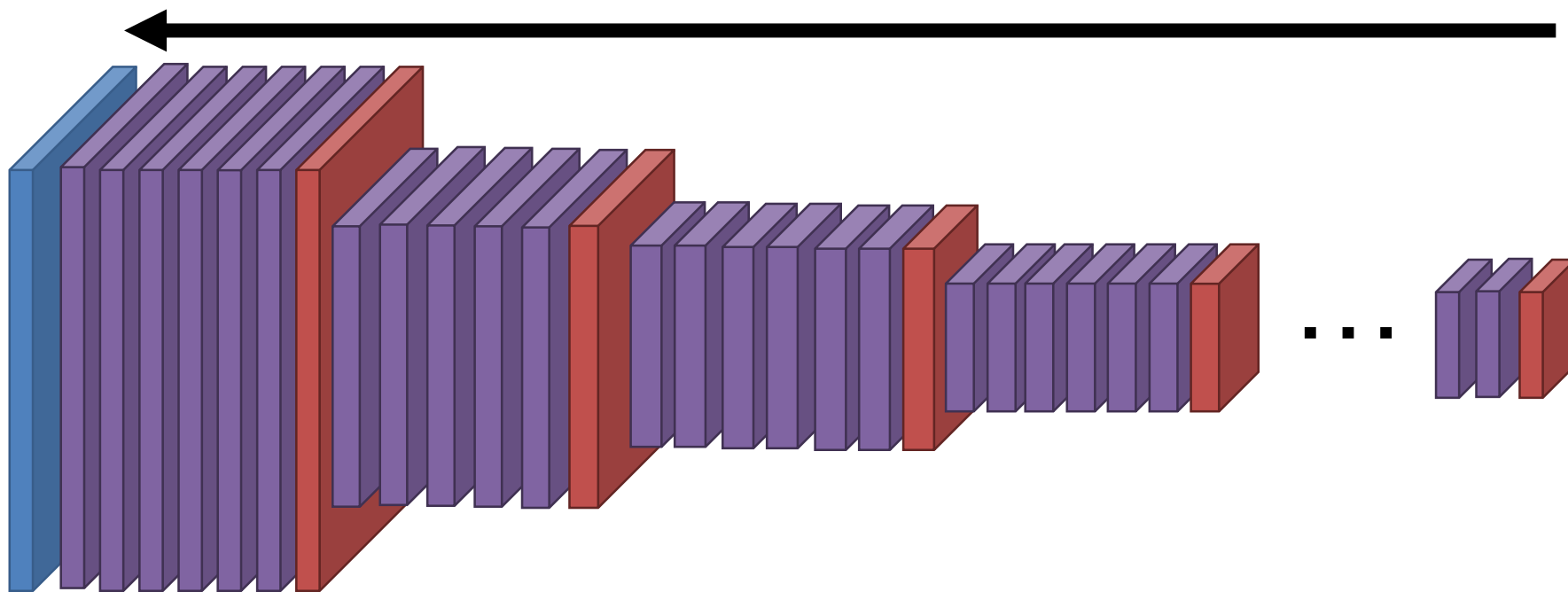
Backprop

Every backpropagation step multiplies the gradient by the local gradient

$$1 * d * d * d \dots * d = d^{n-1}$$

What if $d \ll 1$, n big?

Vanishing Gradients



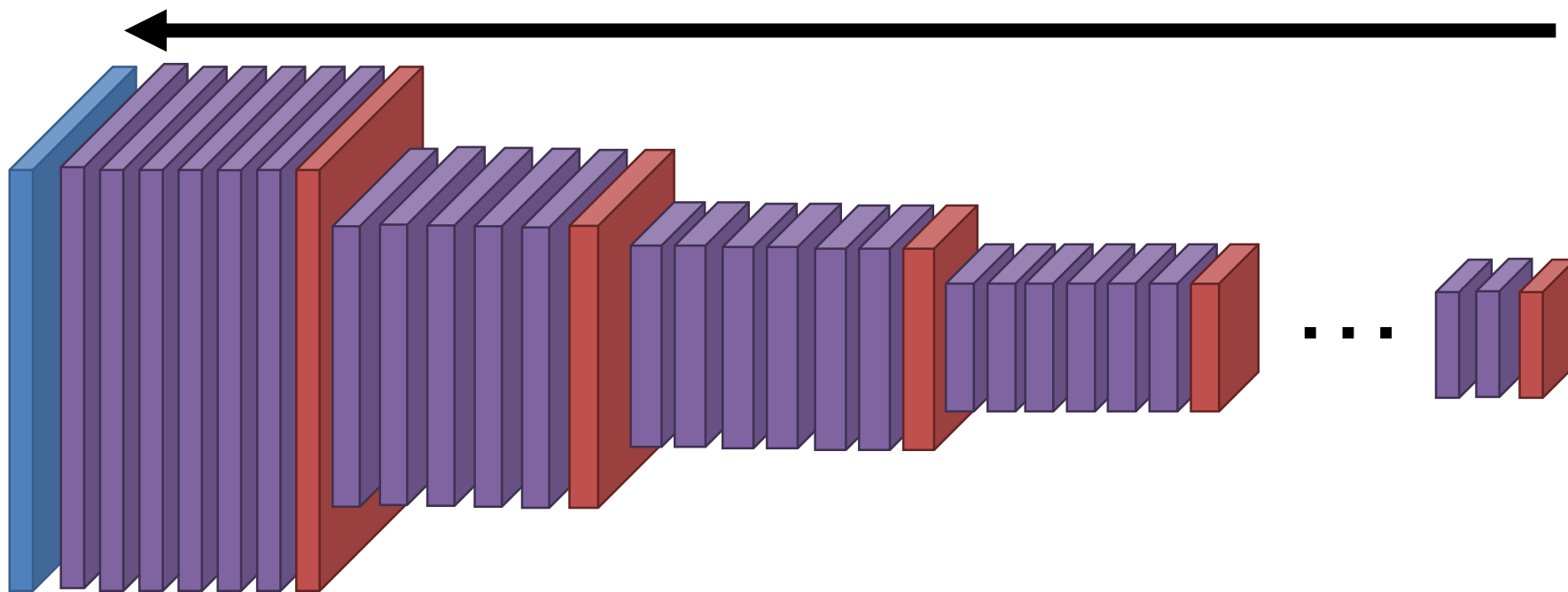
Backprop

Every backpropagation step multiplies the gradient by the local gradient

$$1 * d * d * d \dots * d = d^{n-1}$$

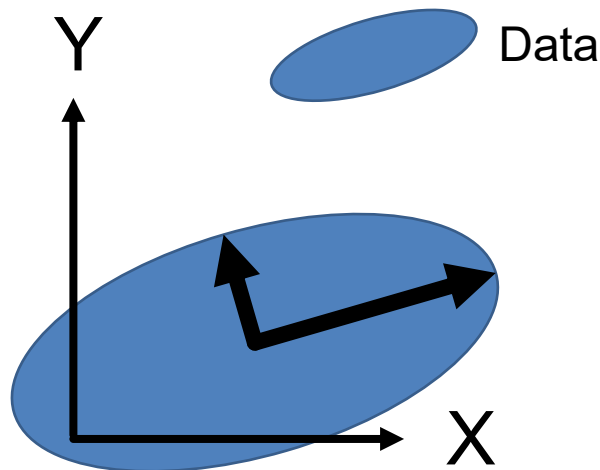
What if $d \gg 1$, n big?

Exploding Gradients

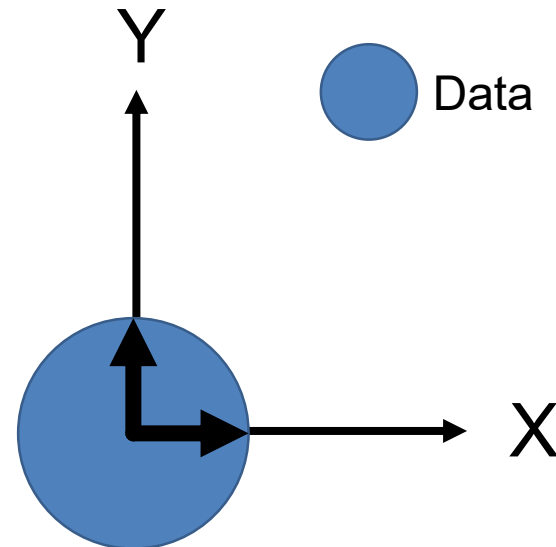


Solution 1 – Batch Normalization

Learning algorithms work far better when data looks like the right as opposed to the left

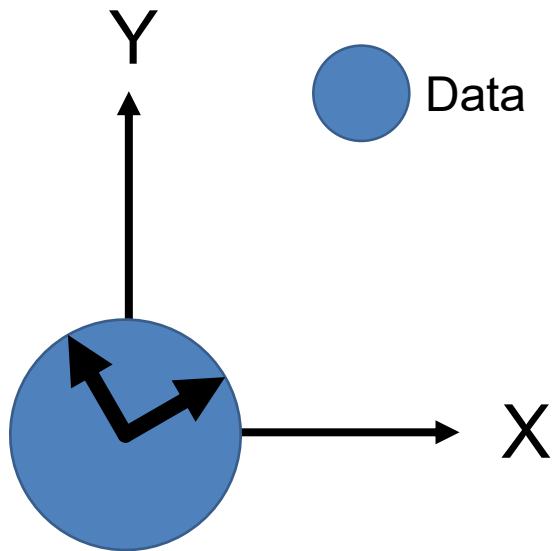


$$\begin{aligned}\text{Mean}(x) &\neq \text{Mean}(Y) \neq 0 \\ \text{Var}(x) &\neq \text{Var}(y) \neq 0 \\ \text{Cov}(x,y) &\neq 0\end{aligned}$$



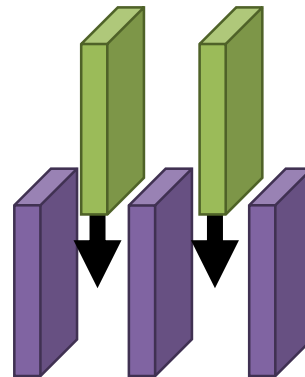
$$\begin{aligned}\text{Mean}(x) &= \text{Mean}(Y) = 0 \\ \text{Var}(x) &= \text{Var}(y) = 1 \\ \text{Cov}(x,y) &= 0\end{aligned}$$

Solution 1 – Batch Normalization



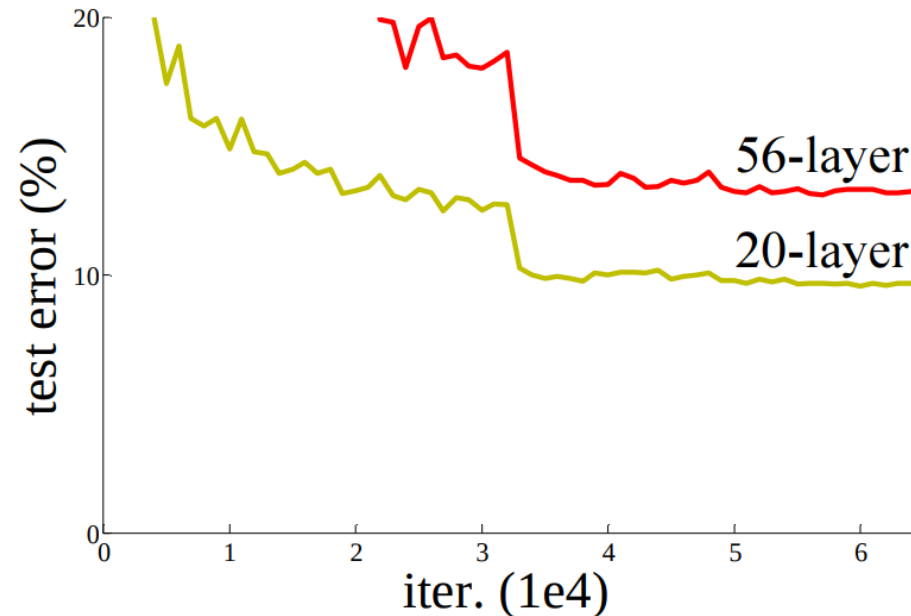
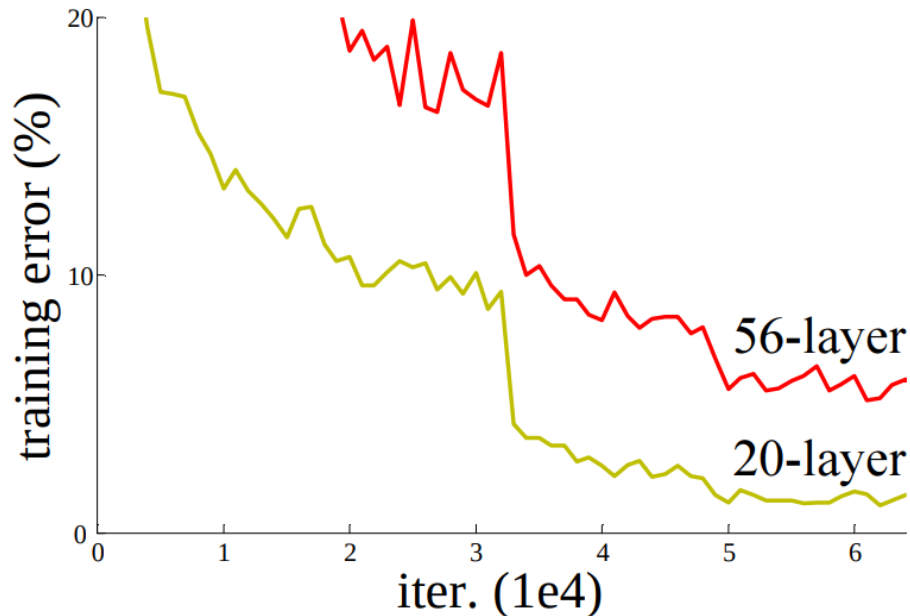
$$\text{Mean}(x) = \text{Mean}(Y) = 0$$
$$\text{Var}(x) = \text{Var}(y) = 1$$

Idea: make layer (**Batch Norm**) that normalizes things going through it based on estimates of $\text{Var}(x_i)$ in each batch.
Stick in between **other layers**



There exists vs. We Can Find

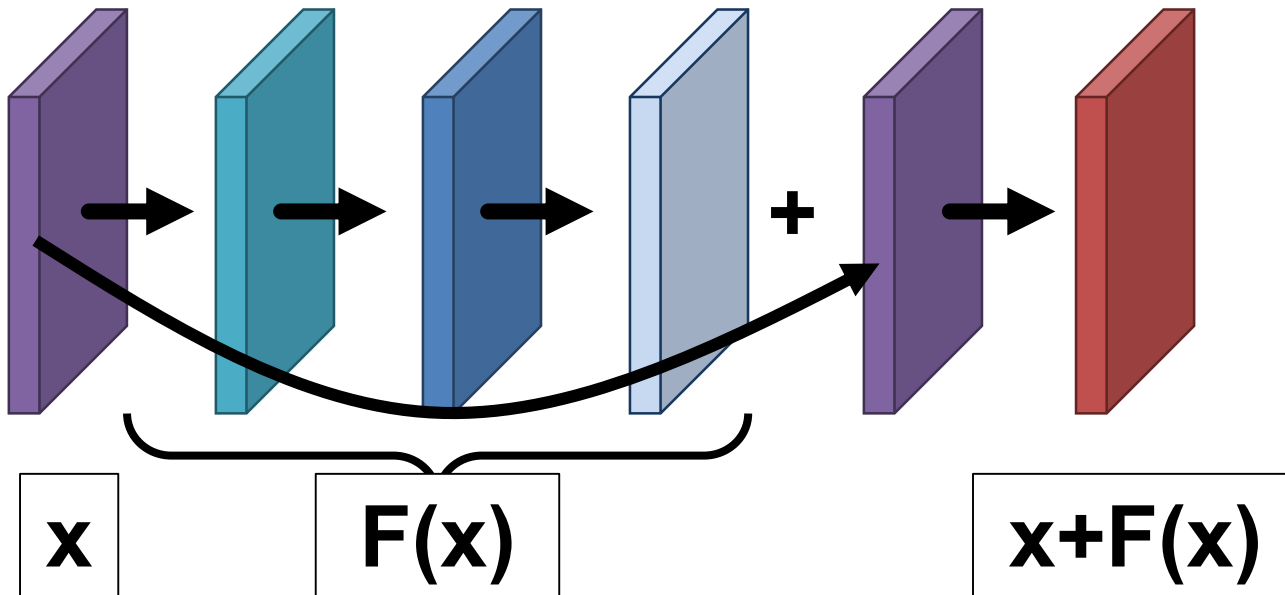
- Still can't **fit** models to the data: **Deeper model** fits worse than **shallower model** on the training data.
- **There exists a deeper model that's identical to the shallow model. Why?**



Residual Learning

New Building Block: $x + F(x)$

Lets you train networks with 100s of layers.



Evaluating Results

At training time, we minimize: $-\log\left(\frac{\exp((Wx)_{y_i})}{\sum_k \exp((Wx)_k)}\right)$

At test time, we evaluate, given predicted class \hat{y}_i :

$$\text{Accuracy: } \frac{1}{n} \sum_{i=1}^n 1(y_i = \hat{y}_i)$$

Evaluating Many Categories

Does this image depict a cat or a dog?



To avoid penalizing ambiguous images, many challenges let you make five guesses (top-5 accuracy):

Your prediction is correct if one of the guesses is right.

Accuracy over the Years

| | Top 1 Error | Top 5 Error |
|---------------|-------------|-------------|
| Best Pre-Deep | - | 26.2%* |
| Alexnet | 43.5% | 20.9% |
| VGG-16 | 28.4% | 9.6% |
| +Batch Norm | 26.6% | 8.5% |
| Resnet-152 | 21.7% | 5.9% |
| Human* | - | 5.1% |

A Practical Aside

- People usually use hardware specialized for matrix multiplies (the card below does 13.4T flops if it's matrix multiplies).
- The real answer to why we love homogeneous coordinates?
 - Makes rendering matrix multiplies →
 - leads to matrix multiplication hardware →
 - deep learning.



Training a CNN

- Download a big dataset
- Initialize network weights randomly
- for epoch in range(epochs):
 - Shuffle dataset
 - for each minibatch in dataset.:
 - Put data on GPU
 - Compute gradient
 - Update gradient with SGD

Training a CNN from Scratch

Need to start \mathbf{w} somewhere

- AlexNet: weights $\sim \text{Normal}(0, 0.01)$, bias = 1
- “Xavier” initialization: $\text{Uniform}\left(\frac{-1}{\sqrt{n}}, \frac{1}{\sqrt{n}}\right)$ where n is the number of neurons
- “Kaiming” initialization: $\text{Normal}(0, \sqrt{2/n})$

Take-home: important, but use defaults

Training a ConvNet

- Convnets typically have millions of parameters:
 - AlexNet: 62 million
 - VGG16: 138 million
- Convnets typically fit on ~1.2 million images
- Remember least squares: if we have fewer data points than parameters, we're in trouble
- Solution: need regularization / more data

Training a CNN – Weight Decay

SGD
Update

$$\mathbf{w}_{t+1} = \mathbf{w}_t - \epsilon \frac{\partial L}{\partial \mathbf{w}_t}$$

+Weight
Decay

$$\mathbf{w}_{t+1} = \mathbf{w}_t - \eta \epsilon \mathbf{w}_t + \epsilon \frac{\partial L}{\partial \mathbf{w}_t}$$

What does this remind you of?

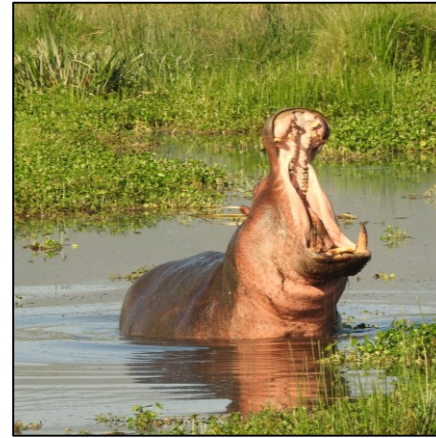
Weight decay is very similar to regularization but might not be the same for more complex optimization techniques.

Quick Quiz

Raise your hand if it's a hippo



Horizontal
Flip



Color
Jitter

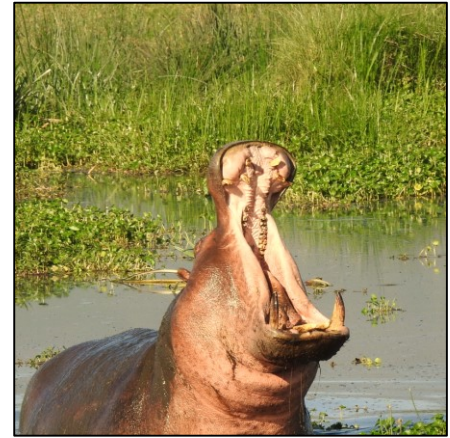
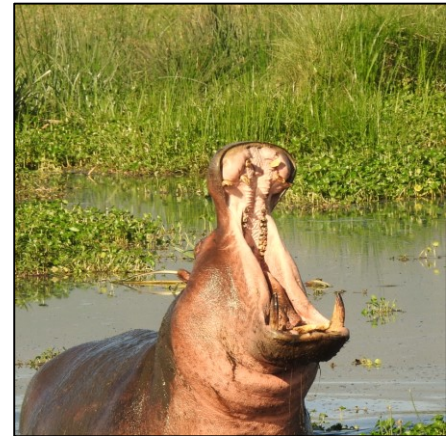
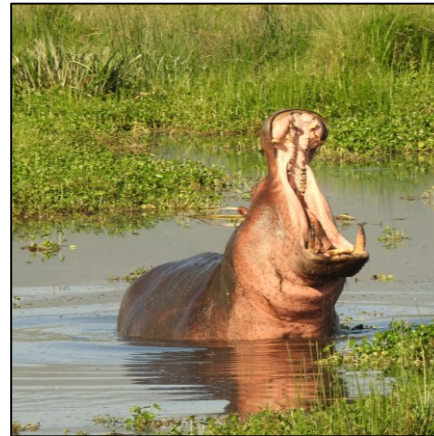
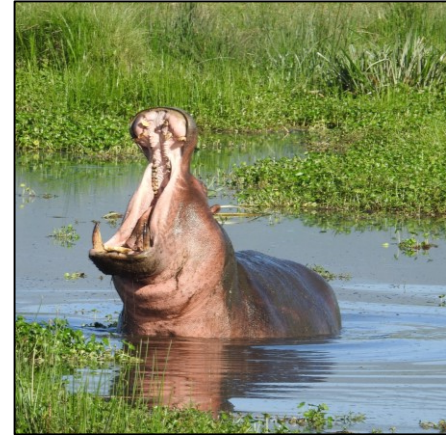


Image
Cropping

Training a CNN –Augmentation

- Apply transformations that don't affect the output
- Produces more data but you have to be careful that it doesn't change the meaning of the output

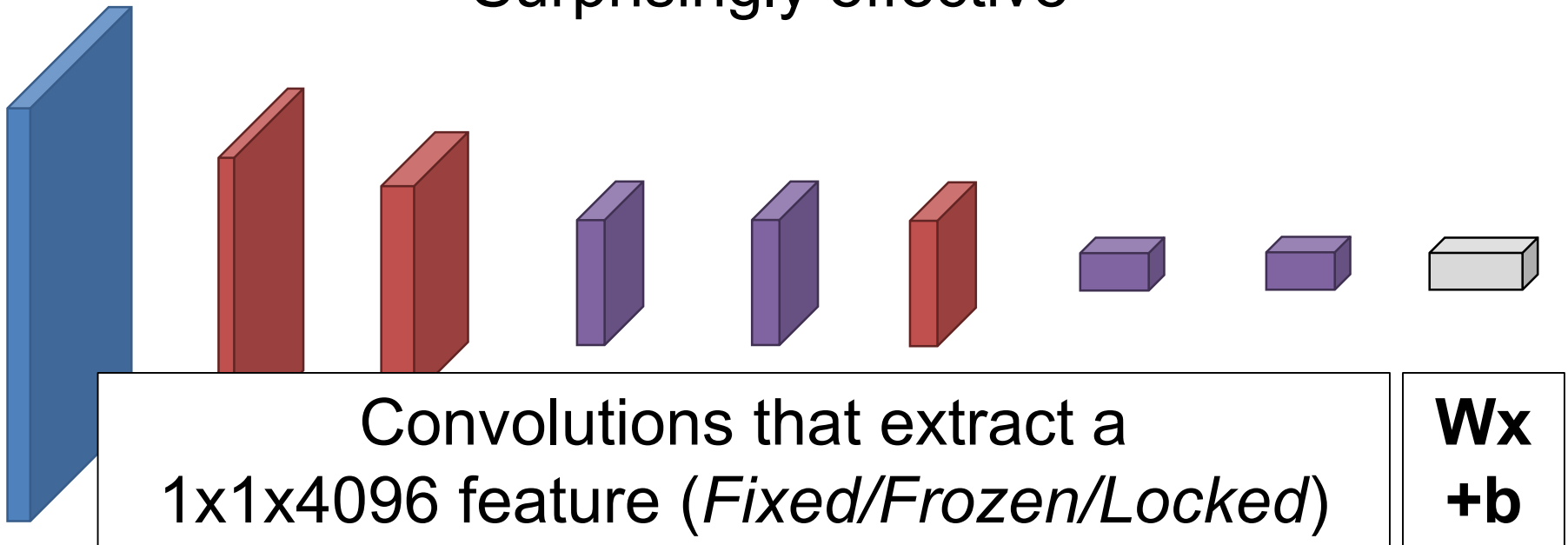


Training a CNN – Fine-tuning

- What if you don't have data?

Fine-Tuning: Pre-trained Features

1. Extract some layer from an existing network
 2. Use as your new feature.
 3. Learn a linear model.
- Surprisingly effective



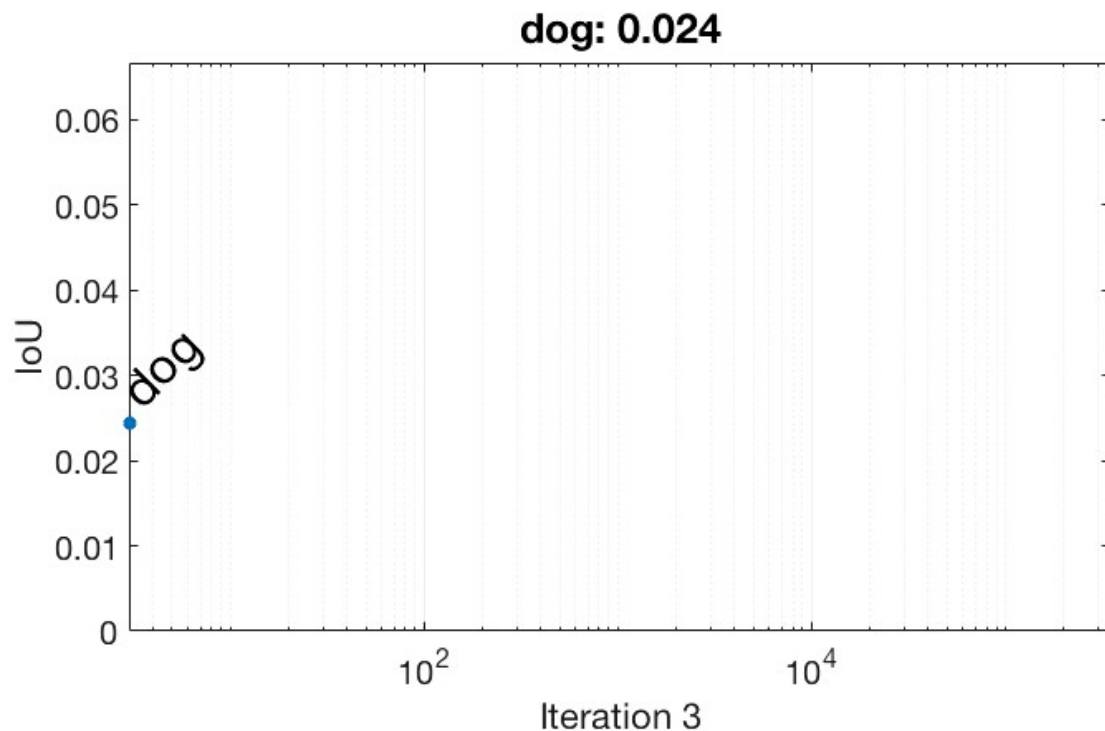
Fine-Tuning: Transfer Learning

- Rather than initialize from random weights, initialize from some “pre-trained” model that does something else.
- Most common model is trained on ImageNet.
- Other pretraining tasks exist but are less popular.

Fine-Tuning: Transfer Learning

Why should this work?

Transferring from objects (dog) to scenes (waterfall)



Recommendations

- <10K images: features
- **Always** try fine-tuning
- >100K images: consider trying from scratch

Summary

- We learned about converting an image into a vector output (e.g., which of K classes is this image, or predict K continuous outputs)
- We learned about some building blocks for doing this