

# Light and Shading

EECS 442 – David Fouhey

Fall 2019, University of Michigan

[http://web.eecs.umich.edu/~fouhey/teaching/EECS442\\_F19/](http://web.eecs.umich.edu/~fouhey/teaching/EECS442_F19/)

# Administrivia –Corrections

- I do my best, but we all make mistakes. If you find a substantial one in my slides, tell me!
- I'm really happy if you find mistakes and tell me politely (but don't go fishing)
- Shengyu found a few mistakes last time and I was *delighted* to hire him as an IA
- Periodically, I'll bring donuts (or the equivalent – it's a bit late for donuts) for those who have caught substantial errors and congratulate them on the course website

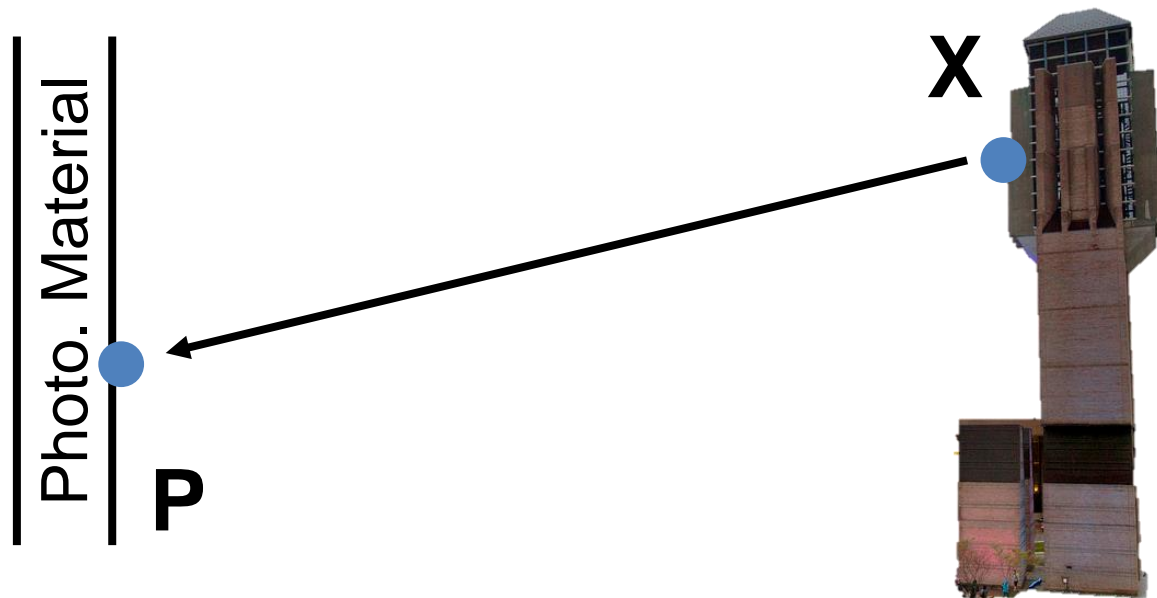
# Administrivia – Mastery Assignment

- If you're rusty and want to wait – please do!
- We're covering a bunch of linear algebra and math next week
- It's not due until December 11, and HW1 won't require a ton of linear algebra

# Recap: Projection

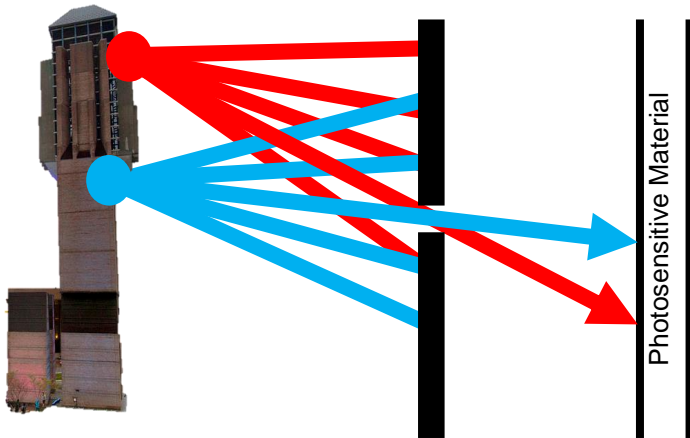
$$\text{Image} \rightarrow \mathbf{P} = \mathbf{K}[\mathbf{R}, \mathbf{t}] \mathbf{X} \leftarrow \text{World}$$

*Intrinsic*  $\nearrow$   $\nwarrow$  *Extrinsic*



# Recap: Lenses

## Pinhole Model



Mathematically correct  
Not quite correct in practice  
Reasonable approximation

## Reality: Lenses

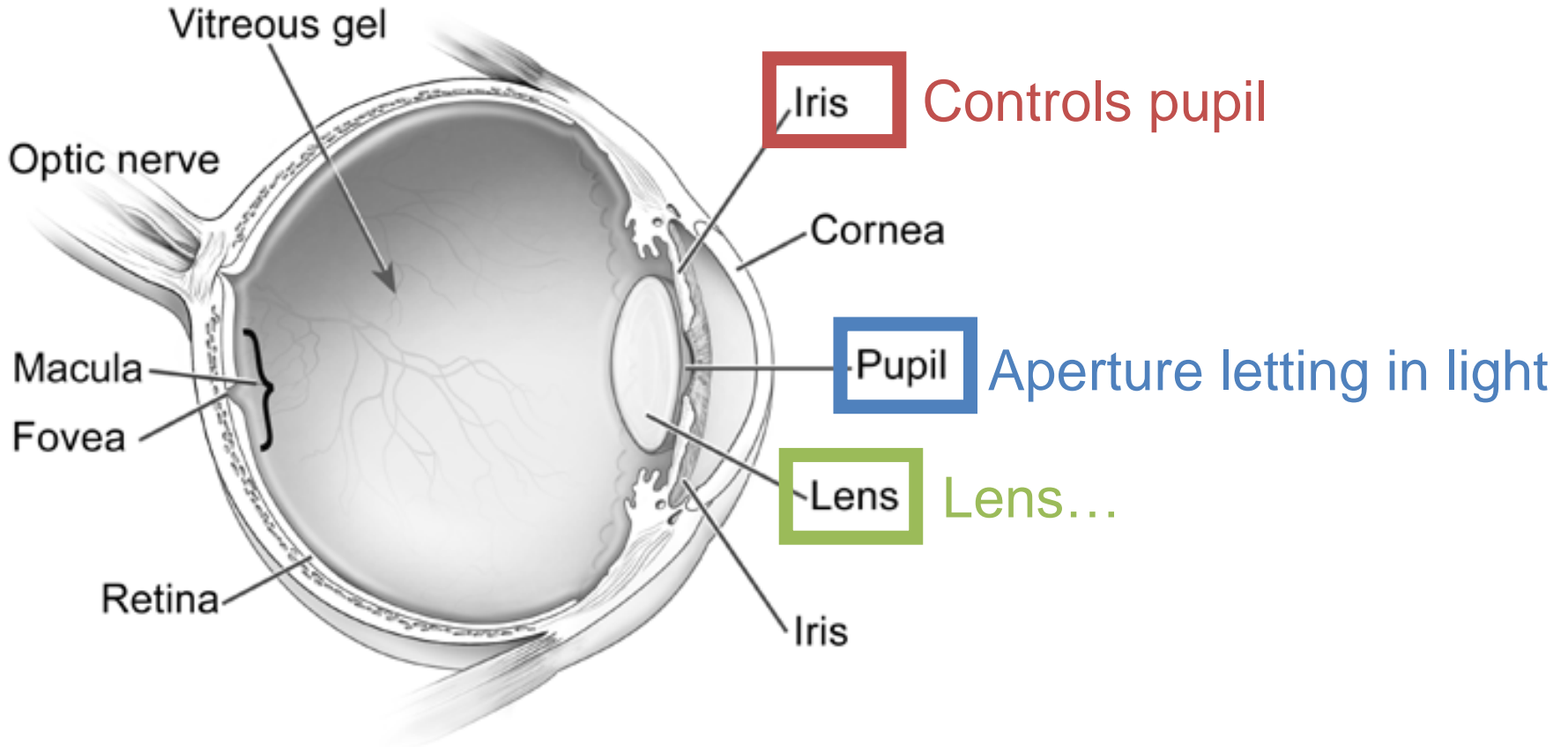


Necessary in practice  
Introduce complications  
Complications fixable

# Today

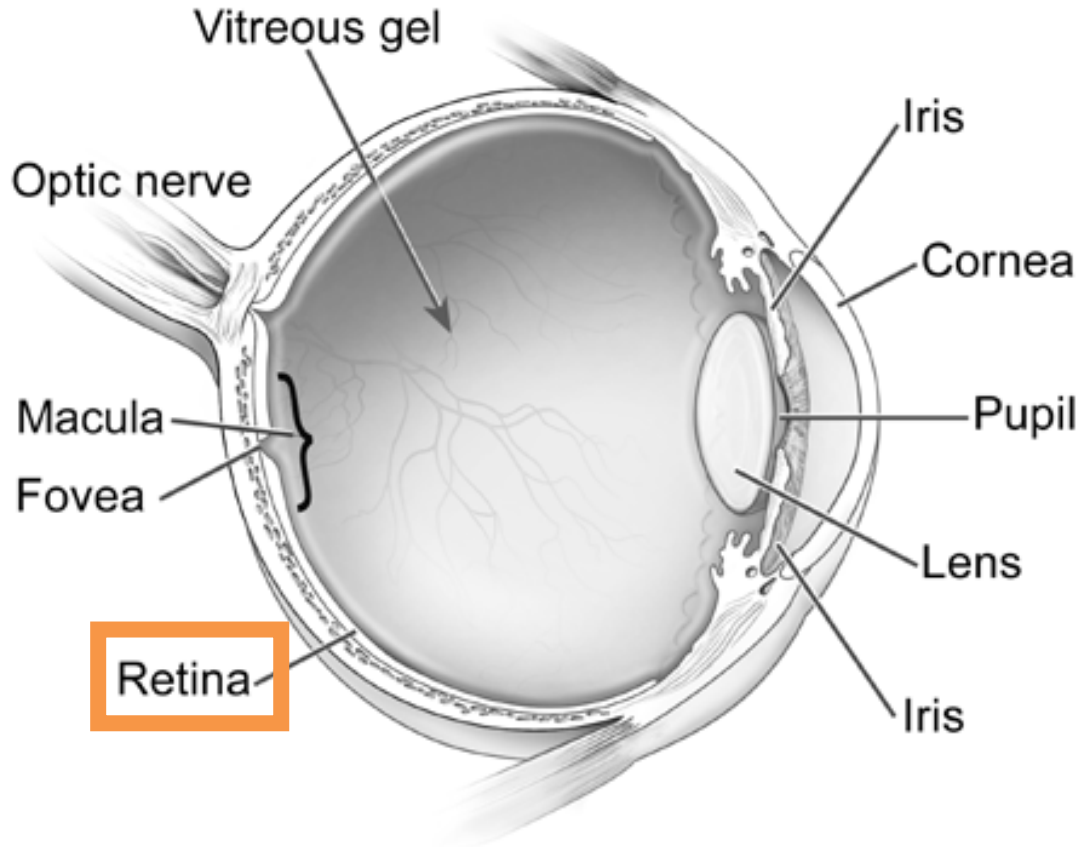
- A little bit about light and how you represent it
- A little bit about lighting and how it works

# Your Very Own Camera



**Where's the film/CCD?**

# Your Very Own Camera

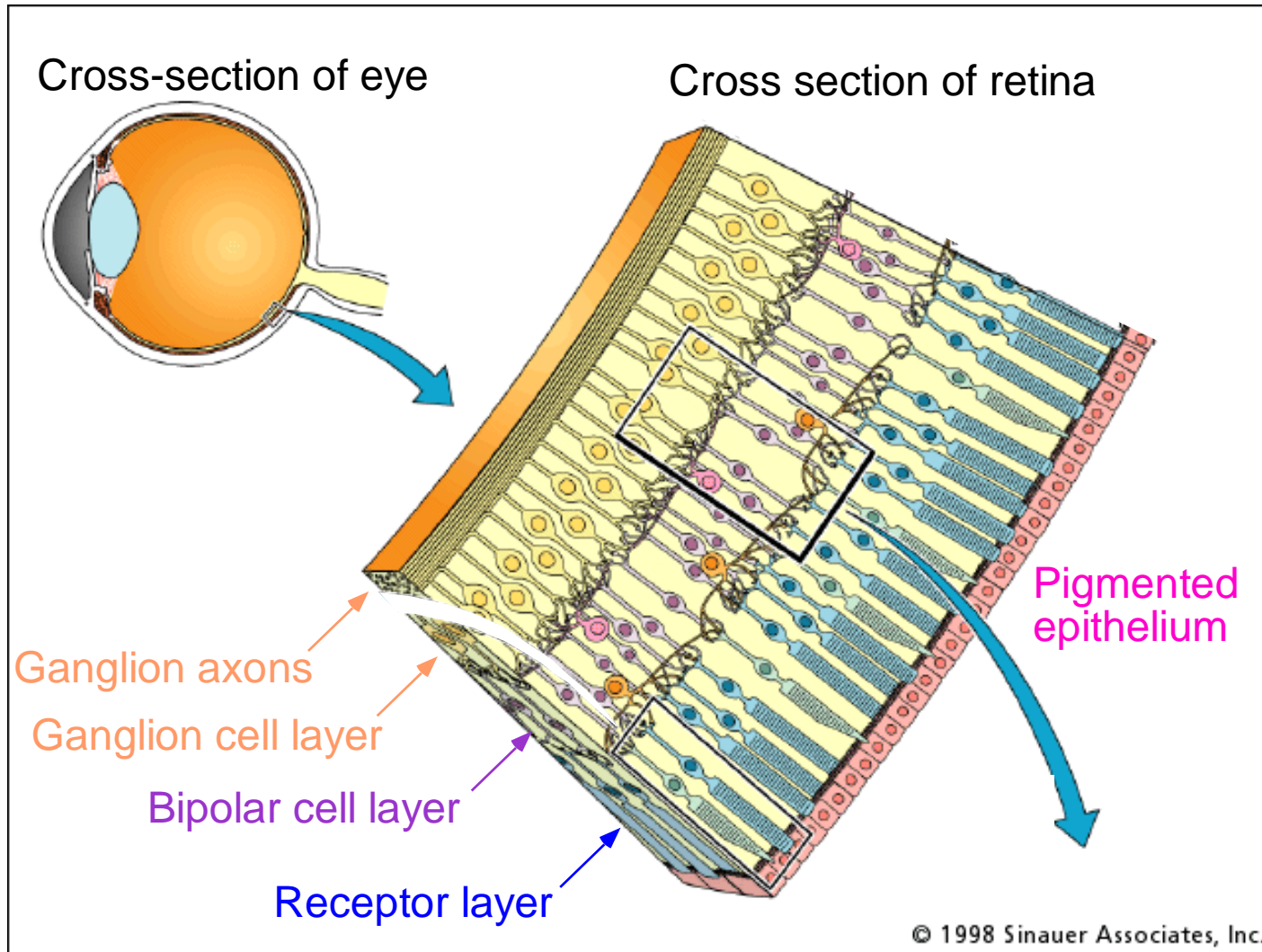


Where's the **film/CCD**?



Demo Time

# What is Retina/Film Made Of?



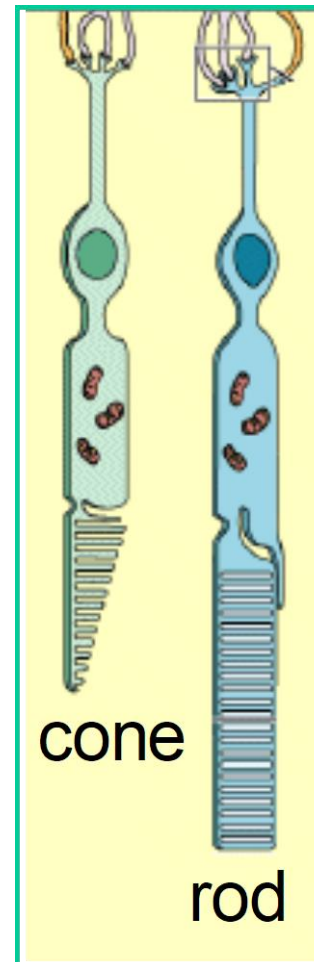
# Two Type of Photo Receptors

## **C**ones

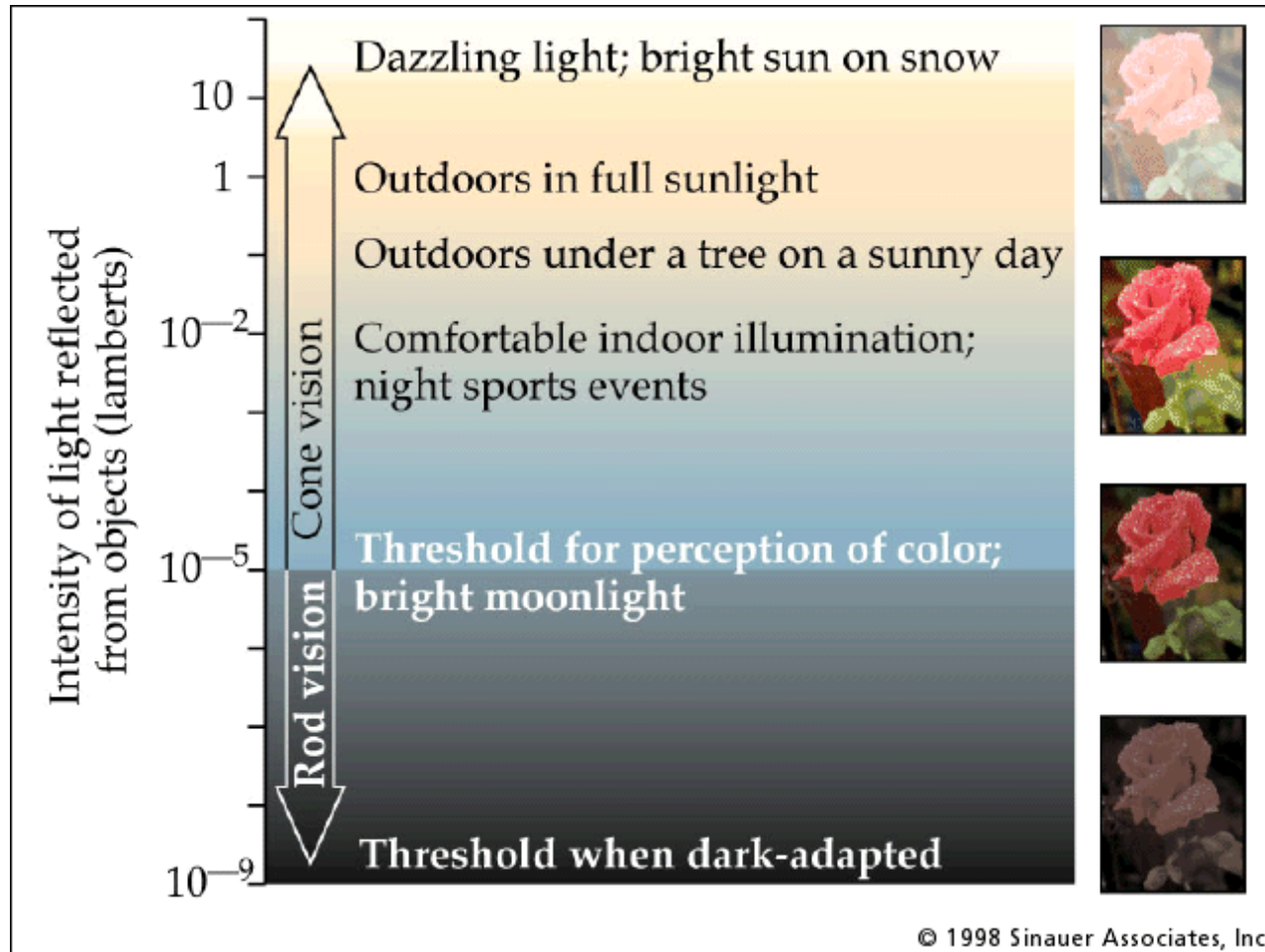
cone-shaped  
less sensitive  
operate in high light  
color vision

## **R**ods

rod-shaped  
highly sensitive  
operate at night  
gray-scale vision

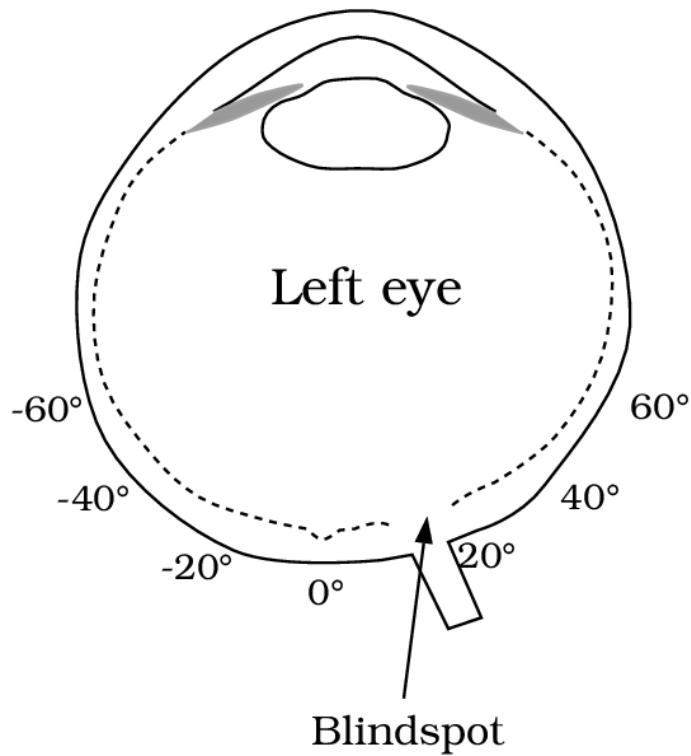


# Rod / Cone Sensitivity

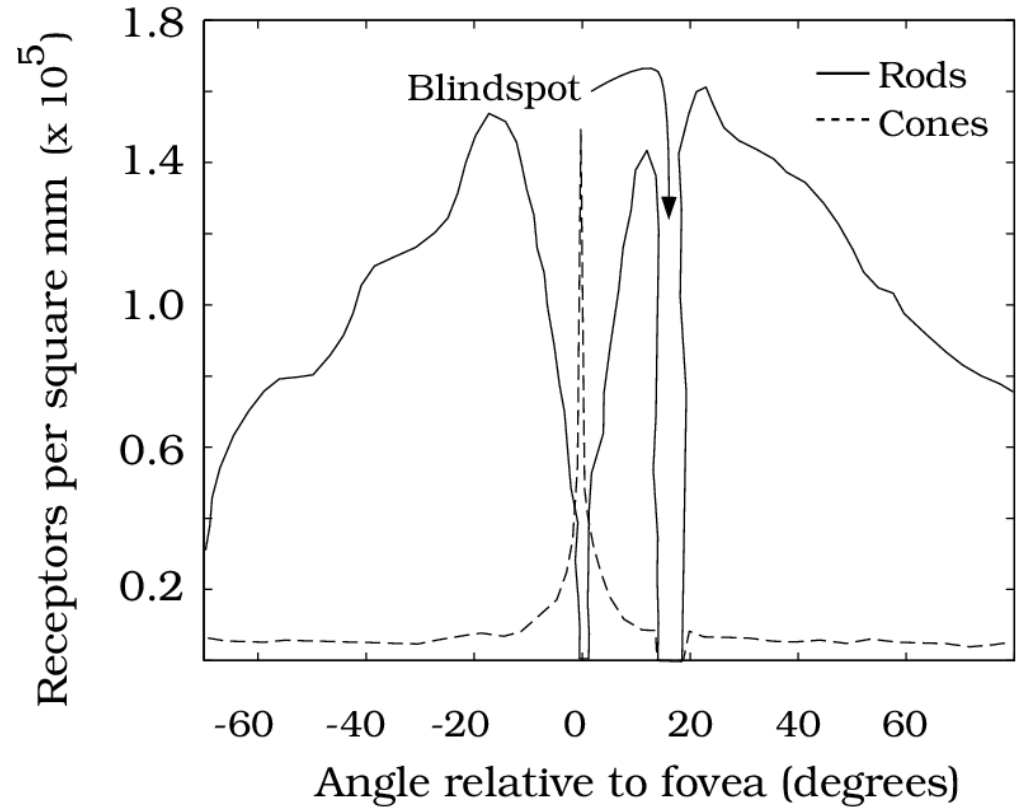


# Rod/Cone Distribution

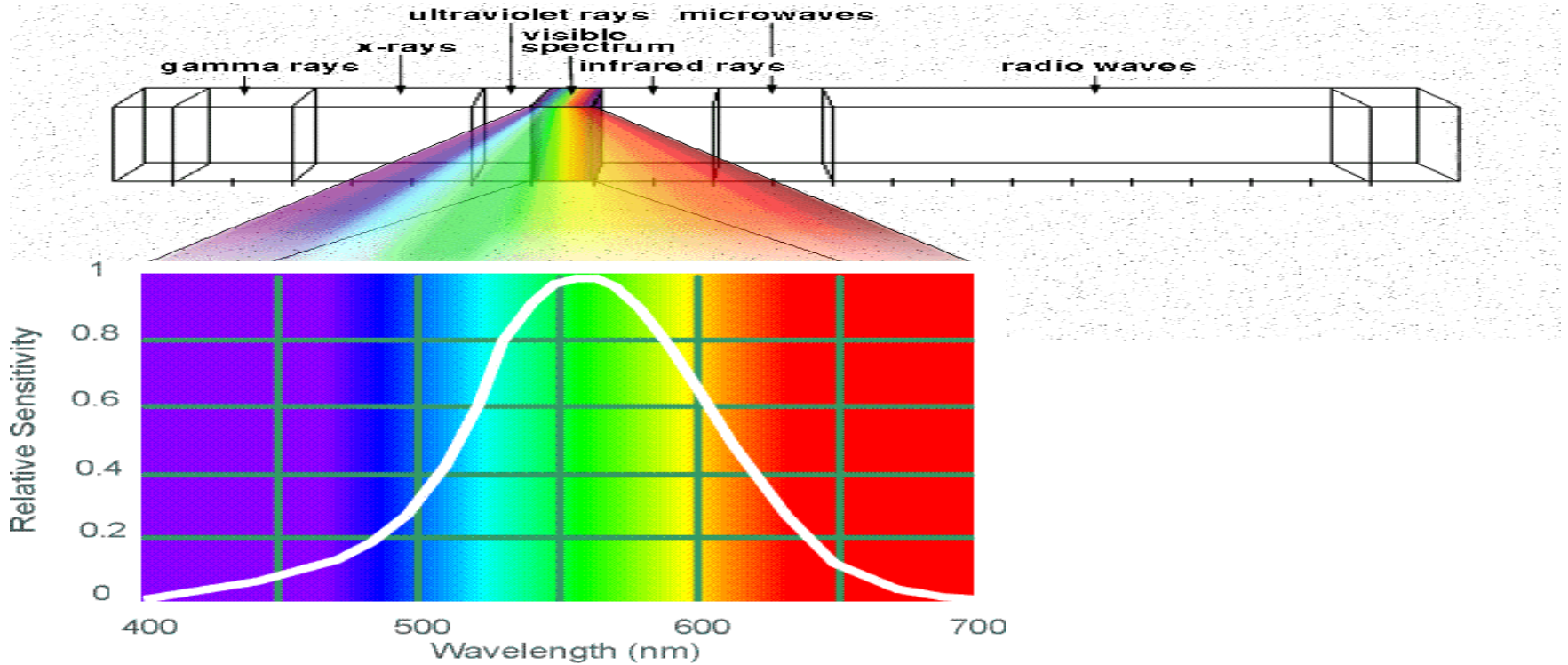
(a)



(b)

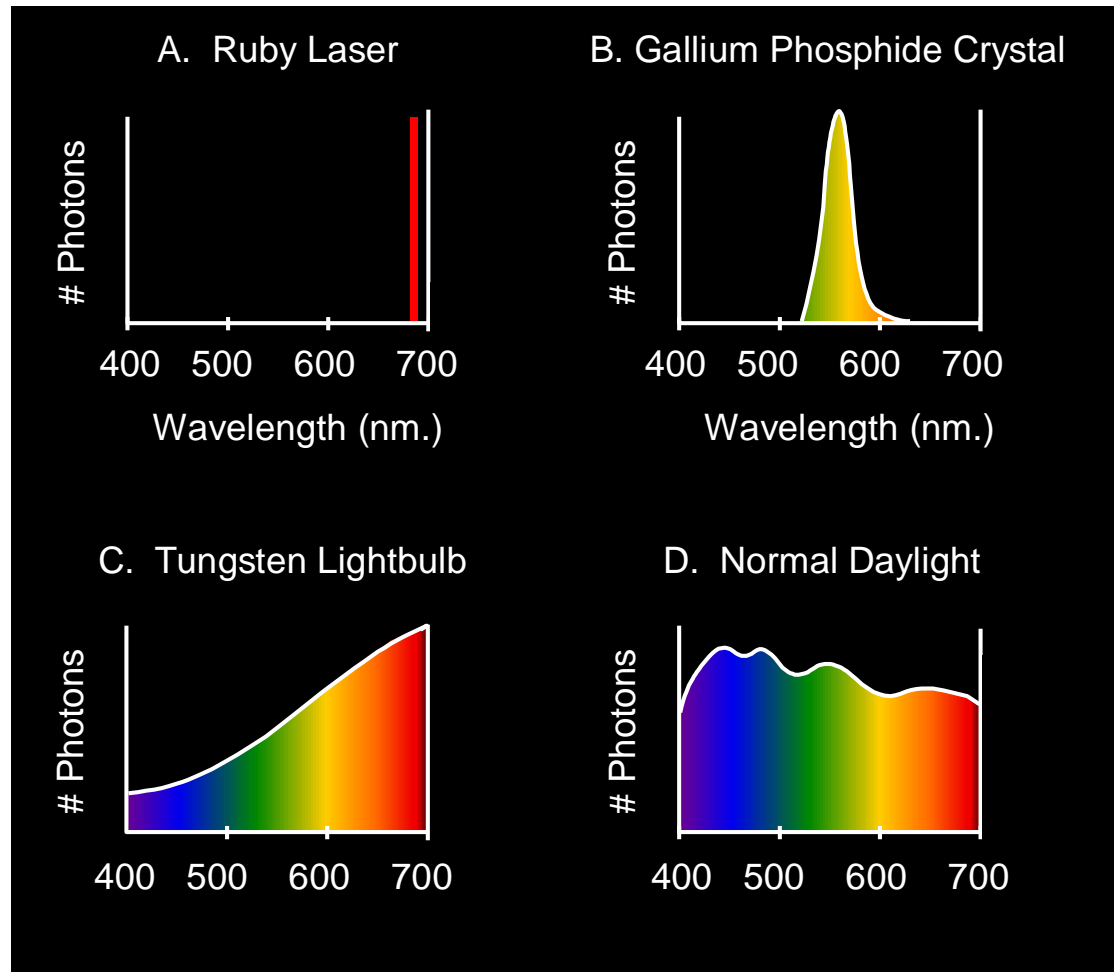


# Electromagnetic Spectrum

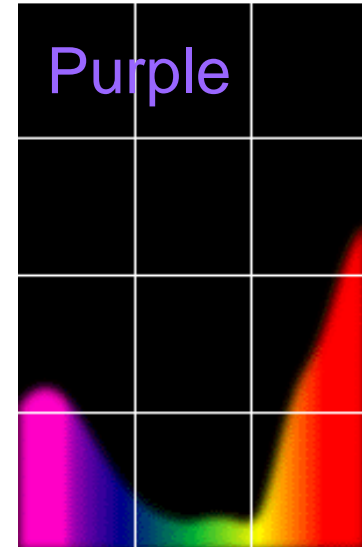
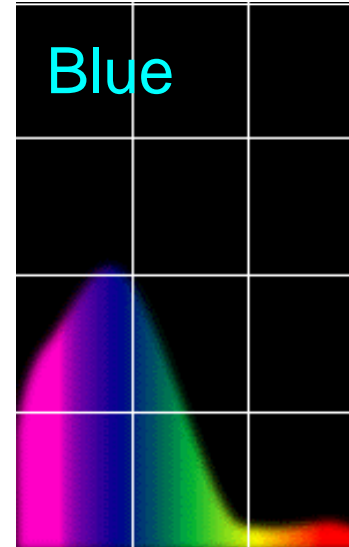
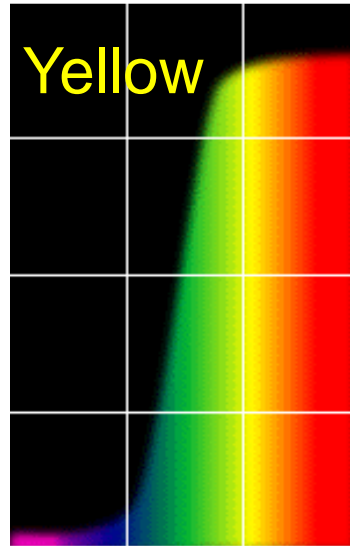
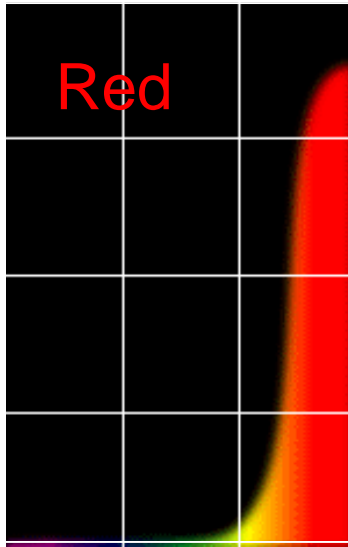


**Why do we see light in these wavelengths?**

# The Physics of Light

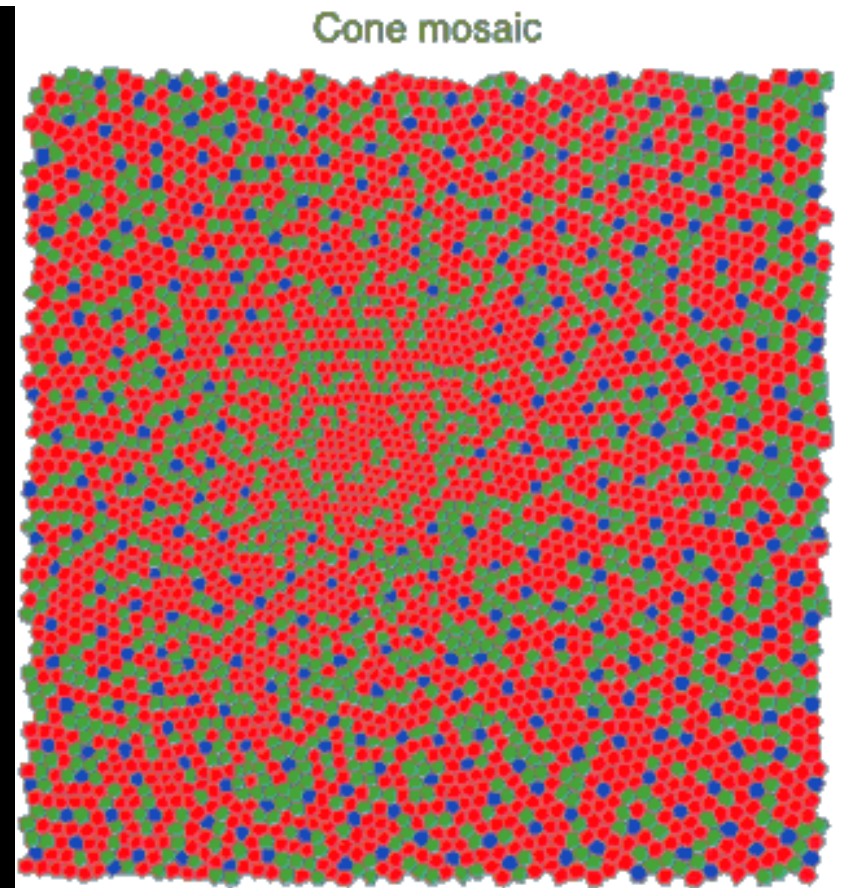
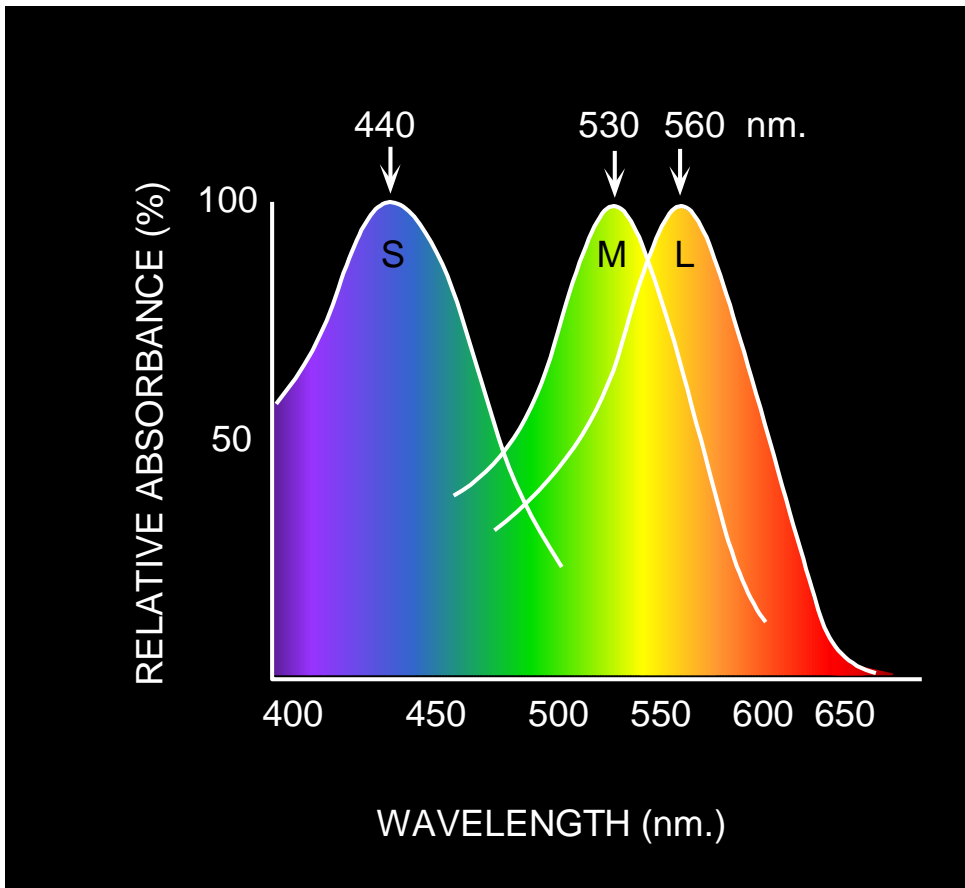


# The Physics of Light



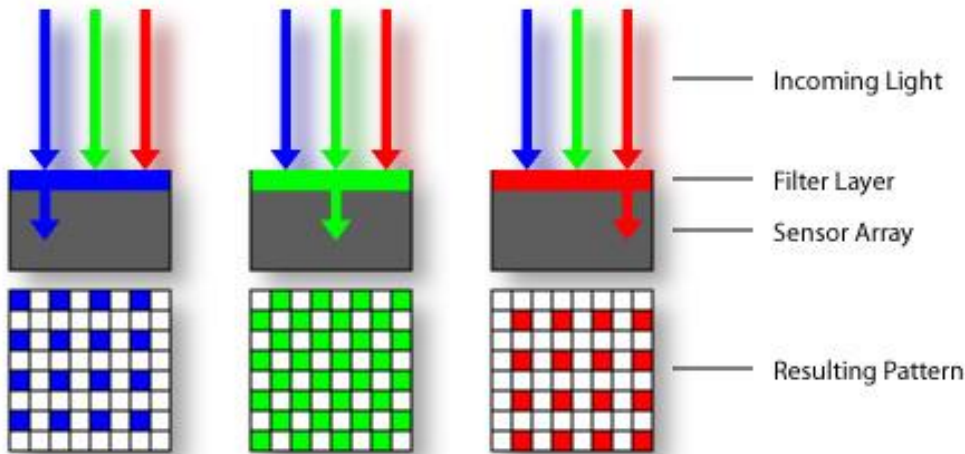
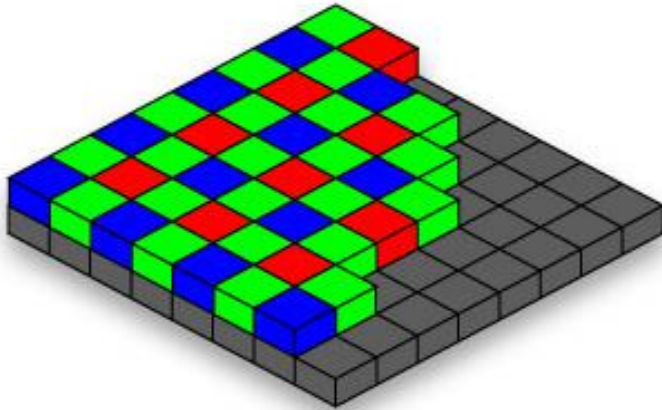


# The Physics of Light



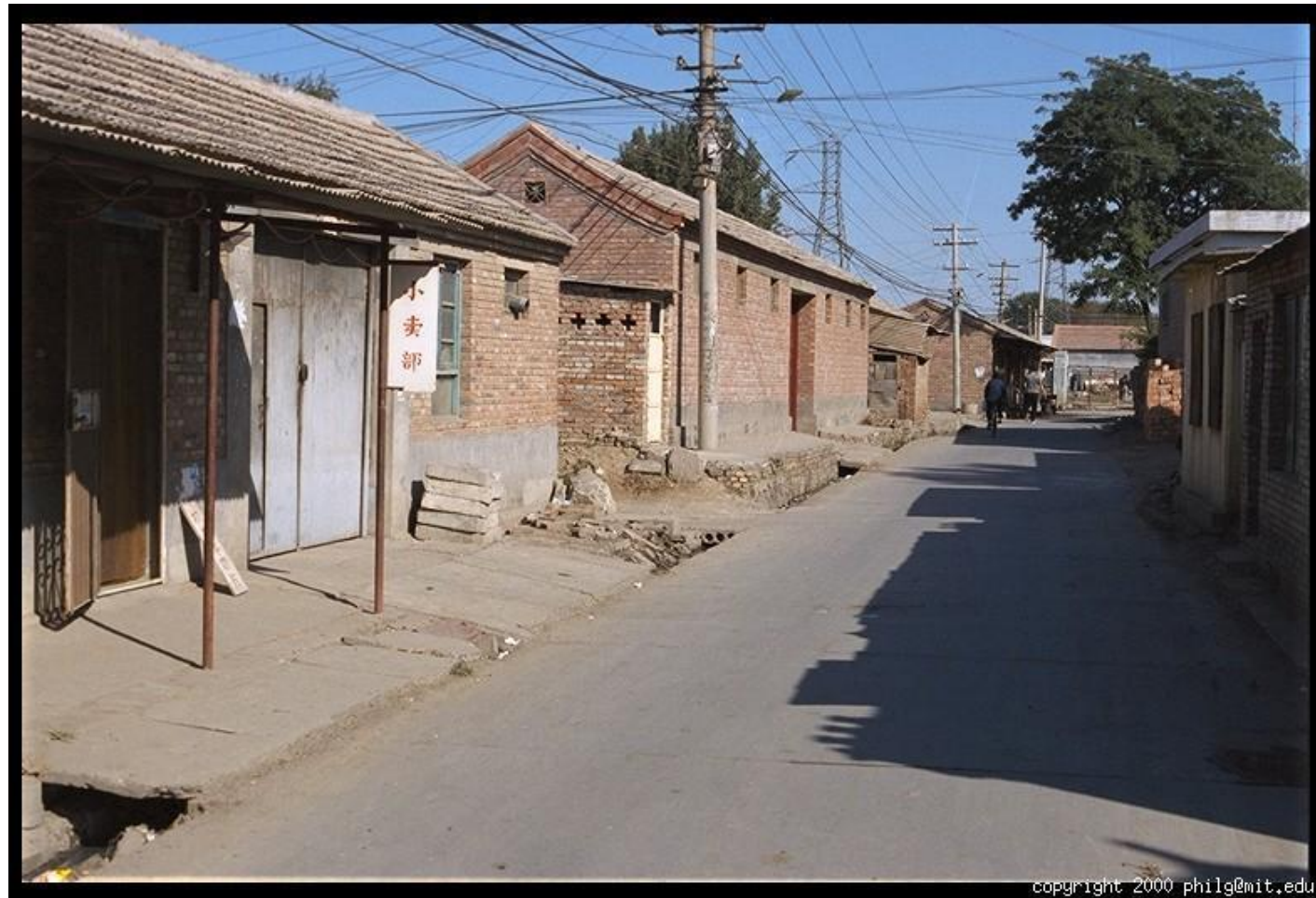
How Do We Get Light?

# Artificial Cones



Estimate RGB  
at 'G' cells from  
neighboring  
values

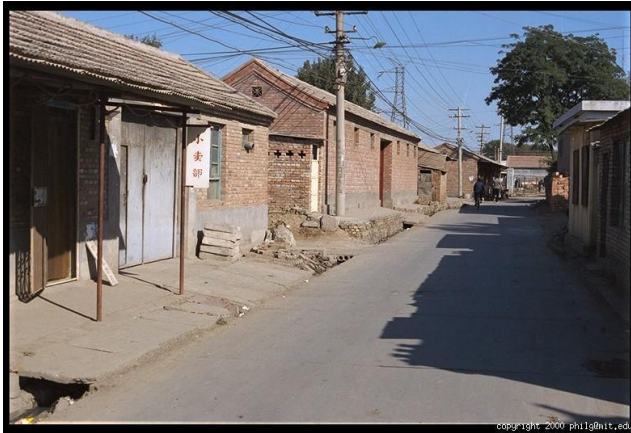
# Color Image



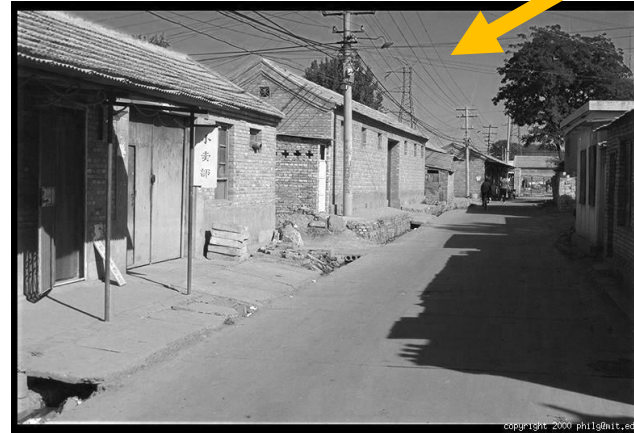


# Color Image

Combined



Red



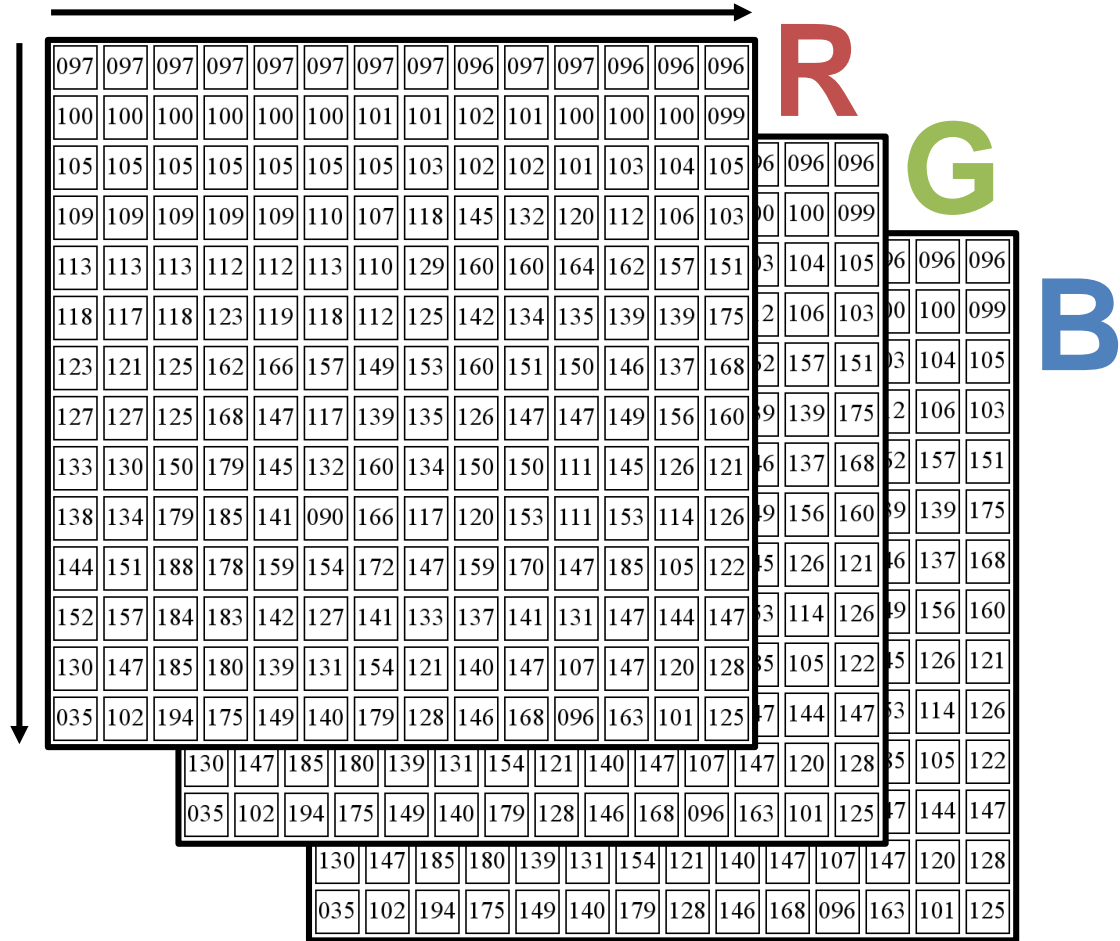
Green



Blue



# Images in Python



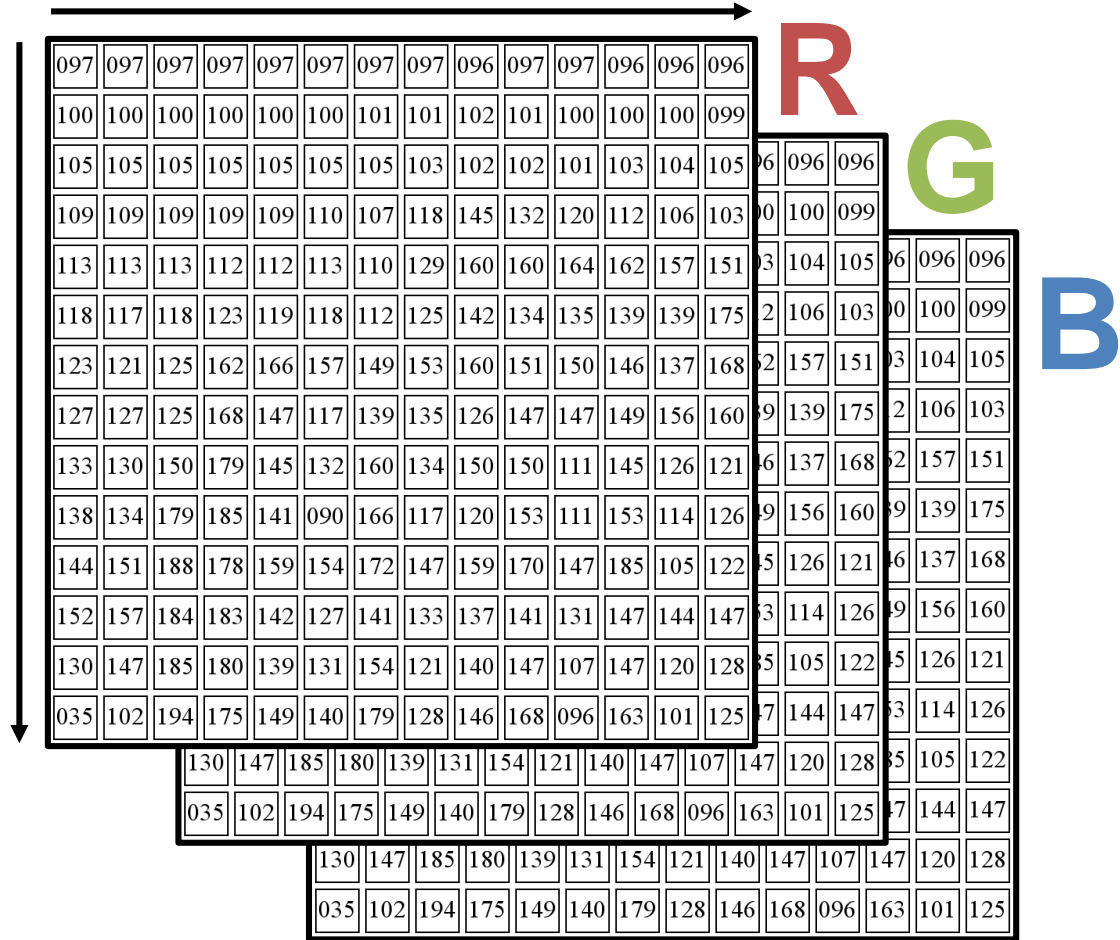
# Images in Python

Images are matrix / tensor `im`

`im[0,0,0]`  
top, left, red

`im[y,x,c]`  
row `y`, column `x`, channel `c`

`im[H-1,W-1,2]`  
bottom right blue

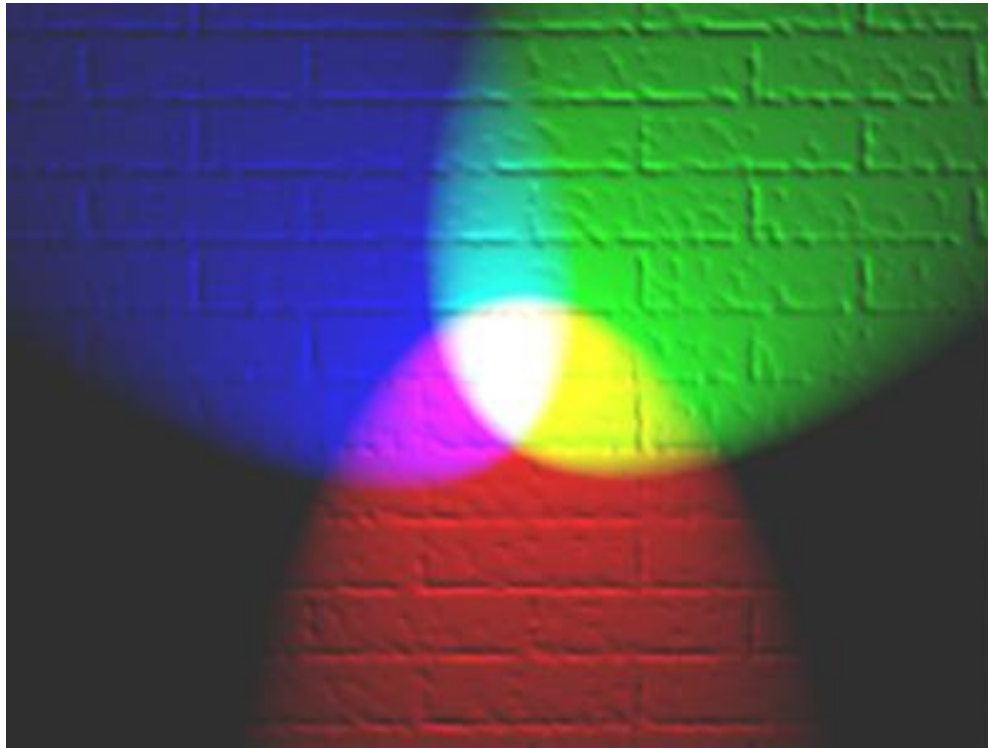


# 5 Things To Always Remember

1. Origin is top left
2. Rows are first index (**what's the fastest direction for accessing?**)
3. Usually referred to as Height x Width
4. Typically stored as uint8 [0,255]
5. for y in range(H): for x in range(W): will run 1 million times for a 1000x1000 image. *A 4GHz processor can do only 4K clock cycles per pixel per second.*



# Representing Colored Light



**Discussion time: how many numbers do you actually need for colored light? Assume all tuples  $(R,G,B)$  are legitimate colors (they are).**

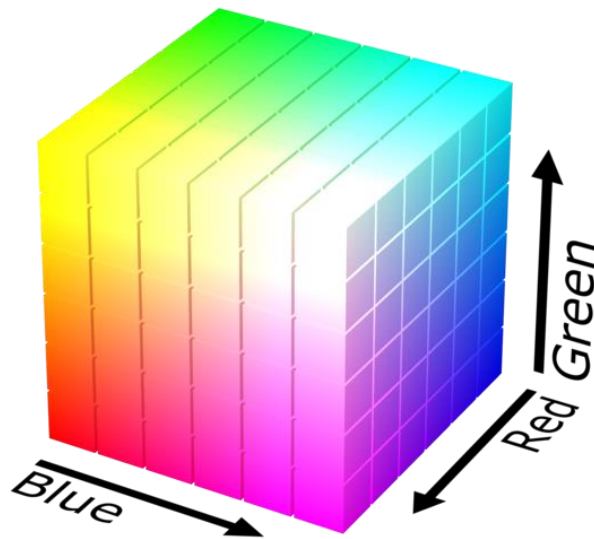
# One Option: RGB

## Pros

1. Simple
2. Common

## Cons

1. Distances don't make sense
2. Correlated



R



G



B

# RGB



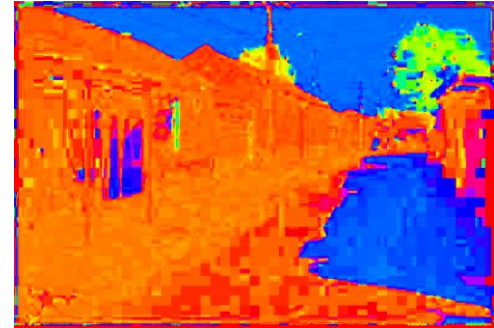
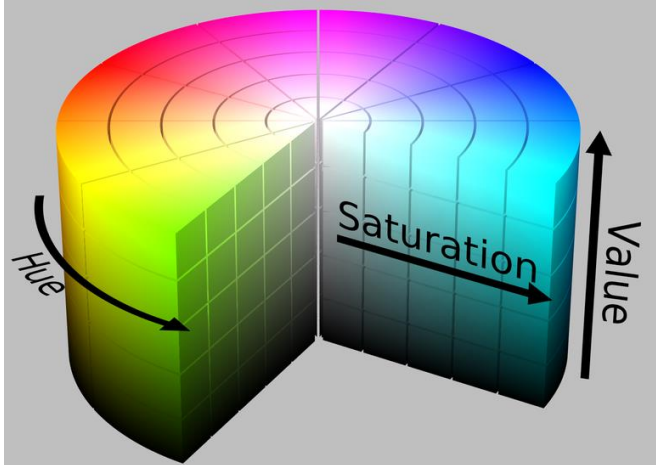
# Another Option: HSV

## Pros

1. Intuitive for picking colors
2. Sort of common
3. Fast to convert

## Cons

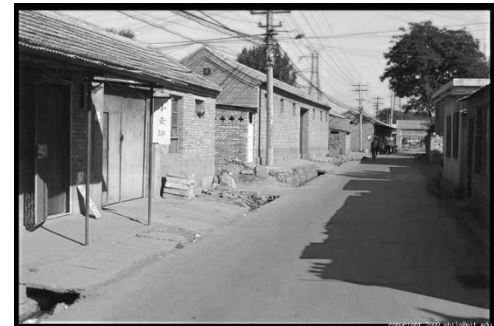
1. Not as good as other better spaces



**H**  
(S=1,V=1)



**S**  
(H=1,V=1)



**V**  
(H=1,S=0)



# HSV

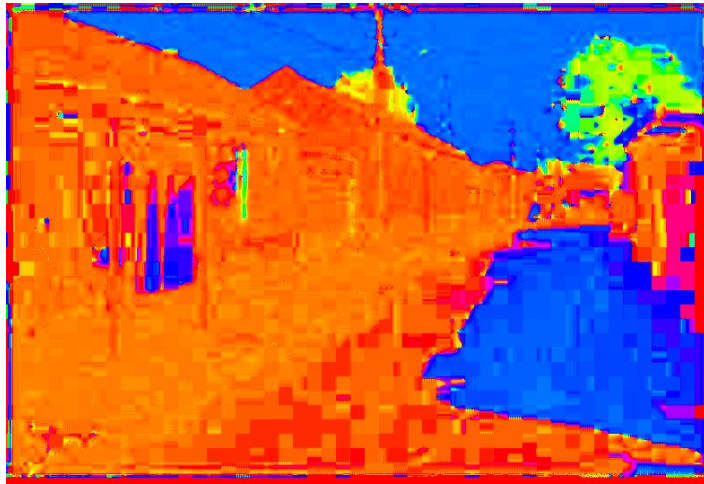


Photo credit: J. Hays

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# Another Option: YCbCr/YUV

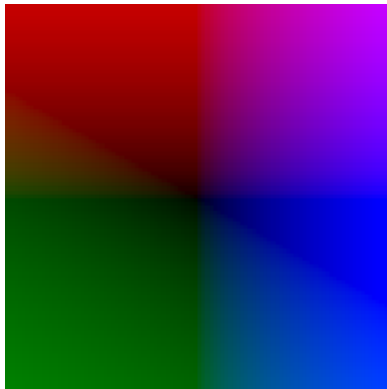
## Pros

1. Great for transmission / compression

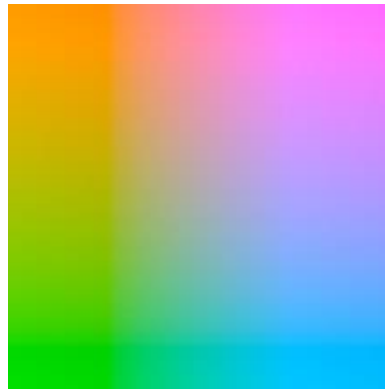
## Cons

1. Not as good as other better smart color spaces

Y = 0



Y = 0.5



**Y**  
(Cb=0.5,  
Cr=0.5)



**Cb**  
(Y=0.5,  
Cr=0.5)



**Cr**  
(Y=0.5,  
Cb=0.5)

# YCbCr



Photo credit: J. Hays

copyright 2009 philip@mit.edu

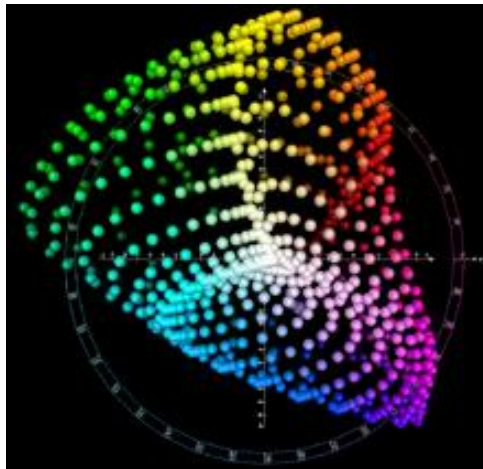
# Another Option: Lab

## Pros

1. Distances correspond with human judgment
2. Safe

## Cons

1. Complex to calculate (don't write it yourself, lots of fp calculations)



**L**  
(a=0,b=0)



**a**  
(L=65,b=0)



**b**  
(L=65,a=0)



# Lab



Photo credit: J. Hays

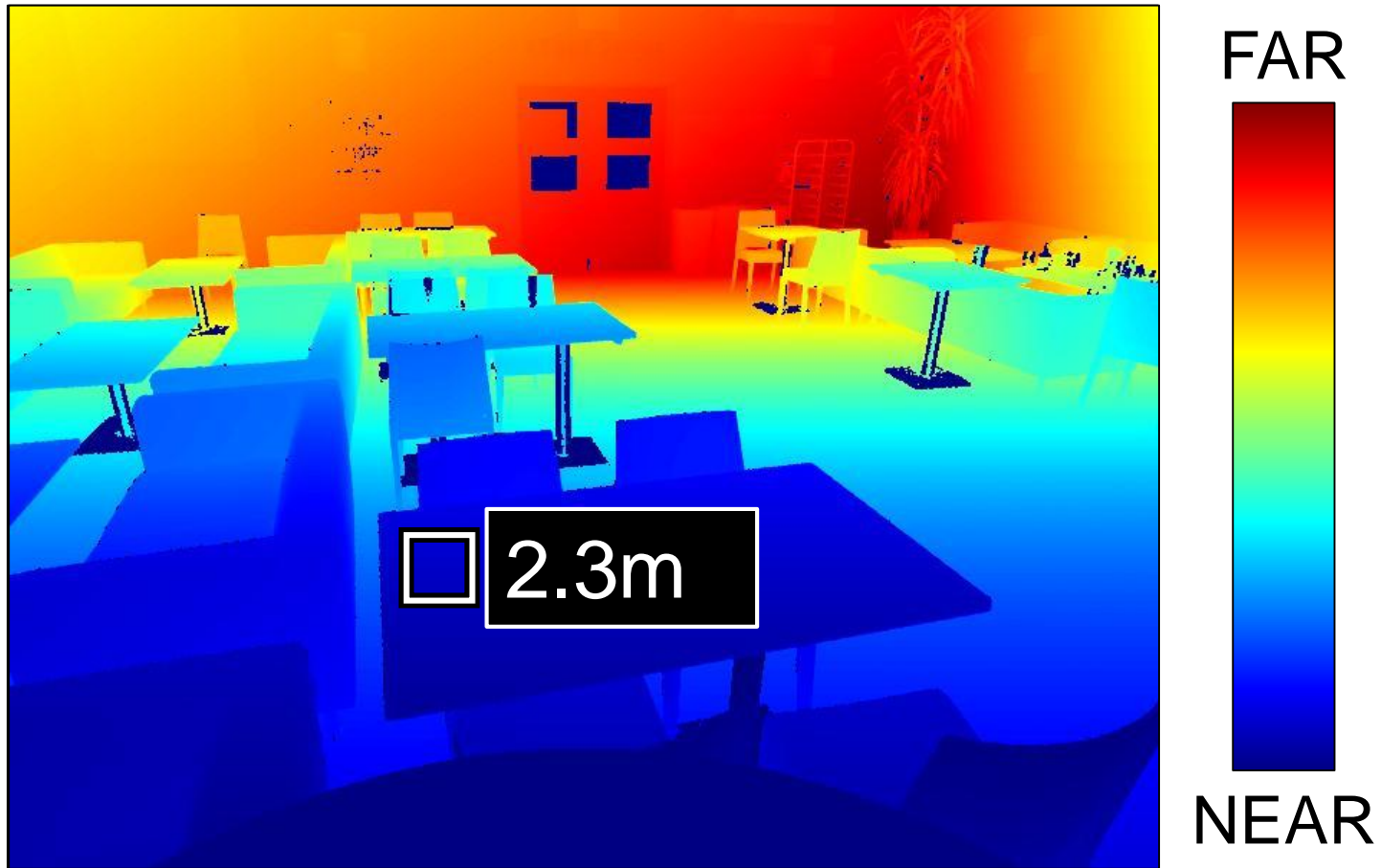
# Why Are There So Many?

- Each serves different functions
  - RGB: sort of intuitive, standard, everywhere
  - HSV: good for picking, fast to compute
  - YCbCr/YUV: fast to compute, compresses well
  - Lab: the right(?) thing to do, but “slow” to compute
- Pick based on what you need and don't sweat it: color really isn't crucial

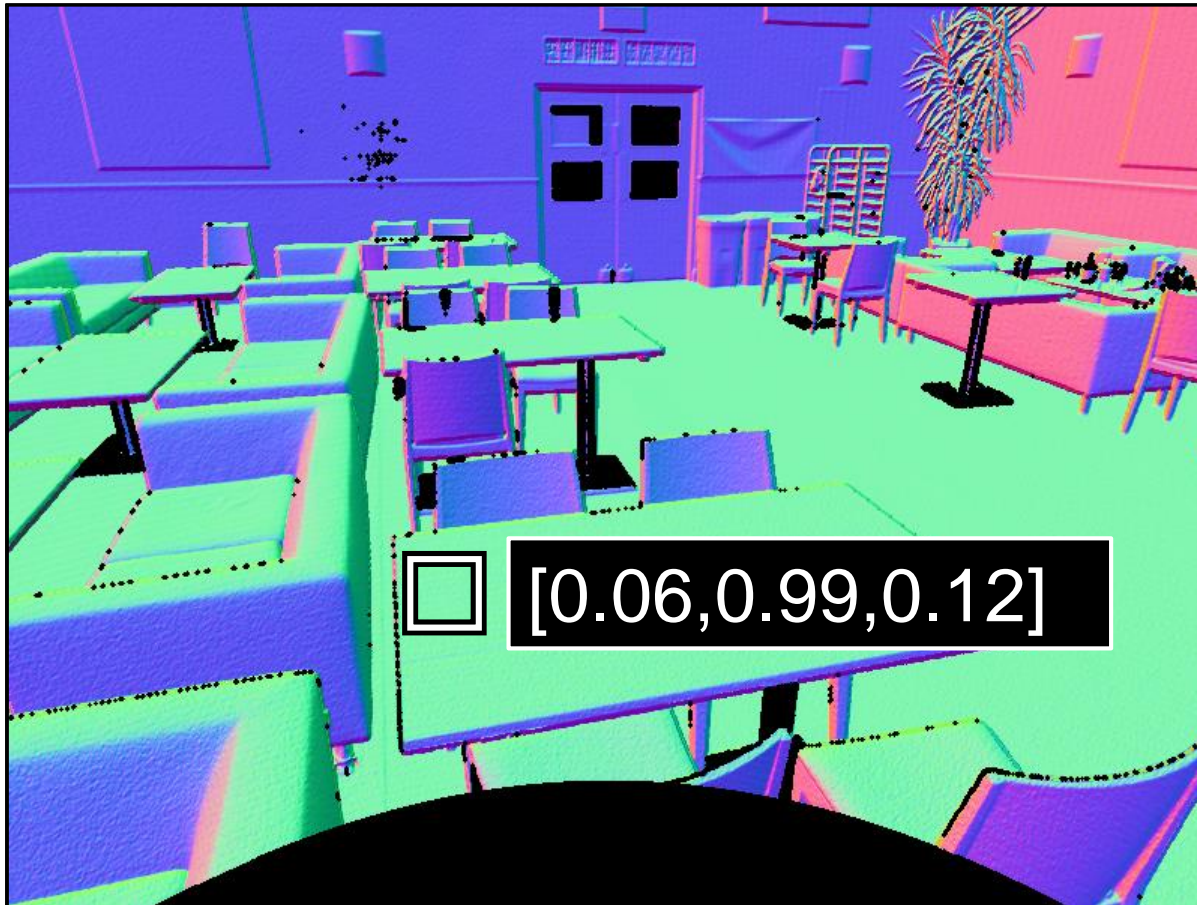
# Only Images

- Almost all of this class is about ordinary RGB images because this has driven a lot of applications
- However, there are lots of other images

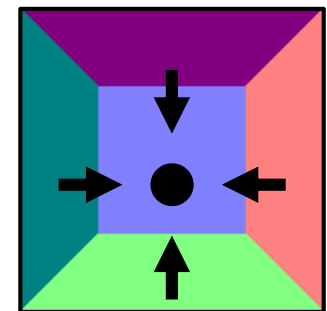
# Depthmap



# Surface Normals



Room



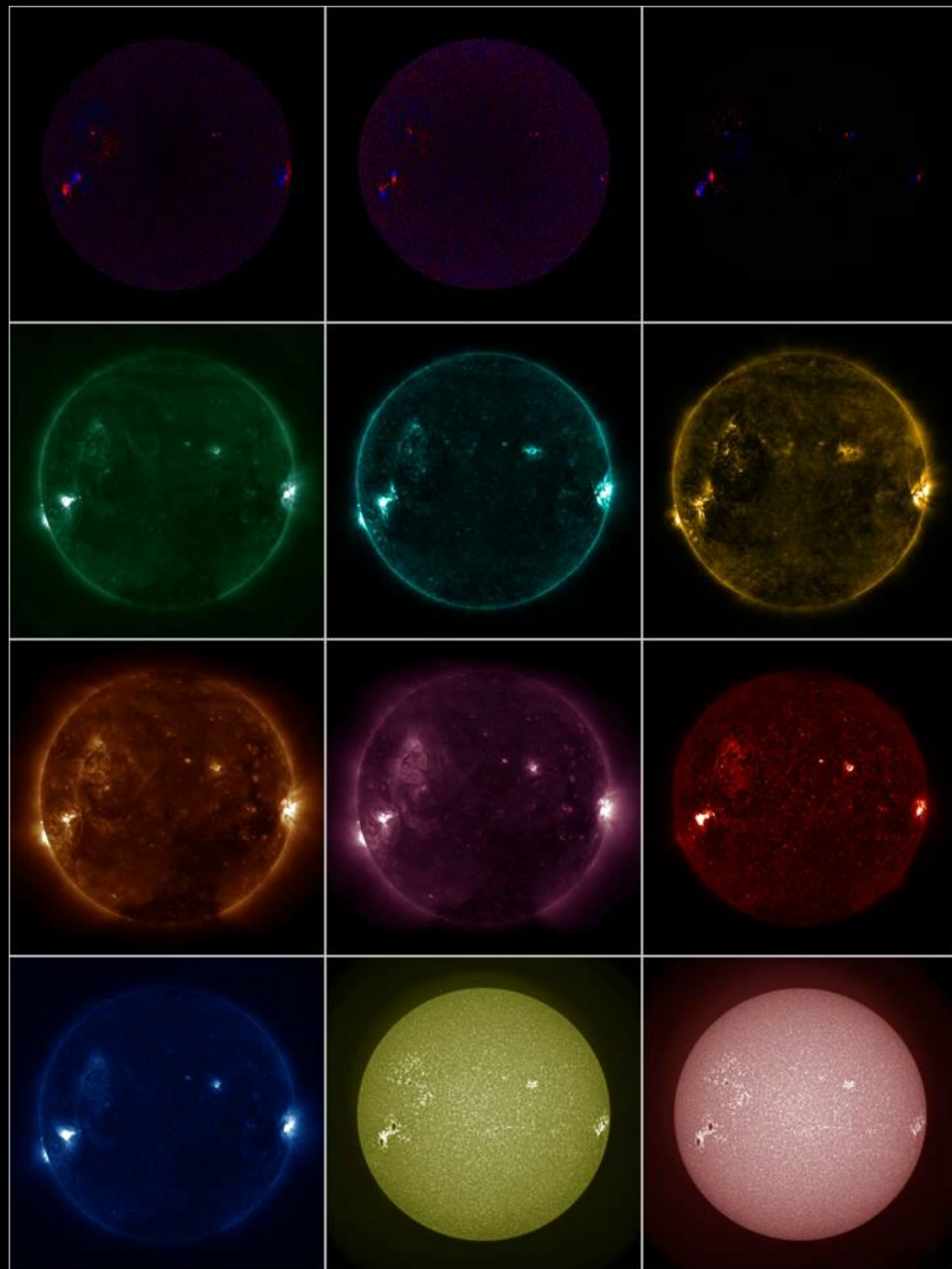
Legend

# Science Data

Magnetic Field in:  
x, y, z

Light at 9 ~wavelenths:  
9.4nm, 13.1nm, 17.1nm  
19.3nm, 21.1nm, 30.4nm  
33.5nm, 160nm, 170nm

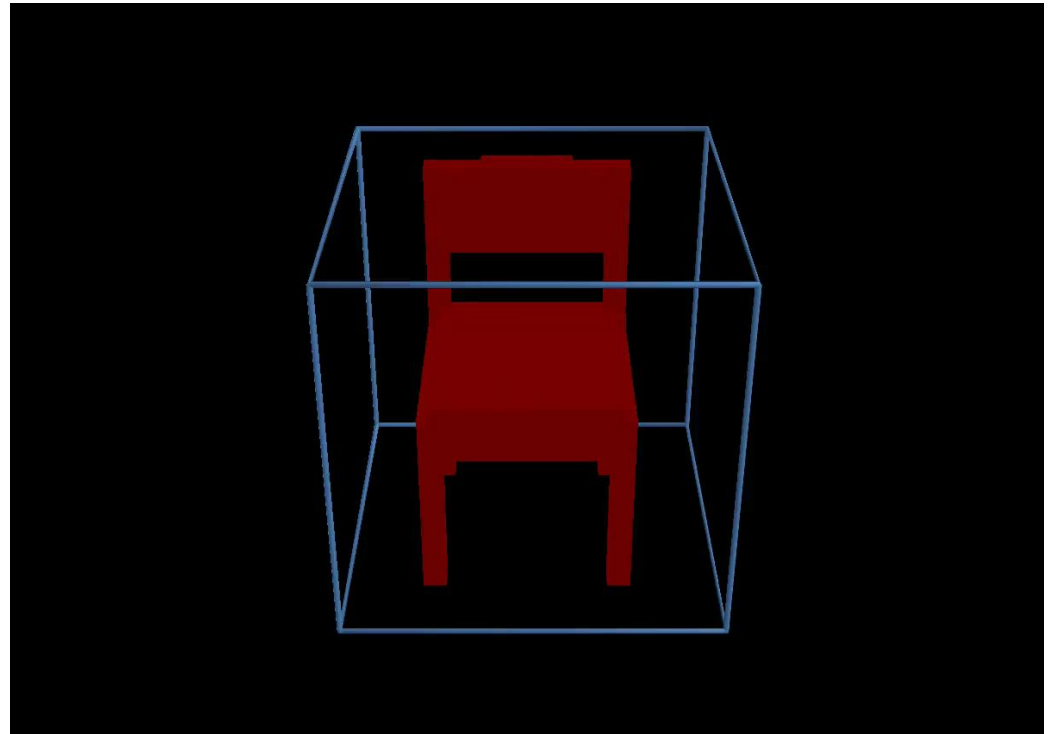
NASA Solar Dynamics  
Observatory observing solar flare



# Volumes

Volumes: images with more dimensions.

Emerge in 3D reconstruction, medical imaging, temporal data



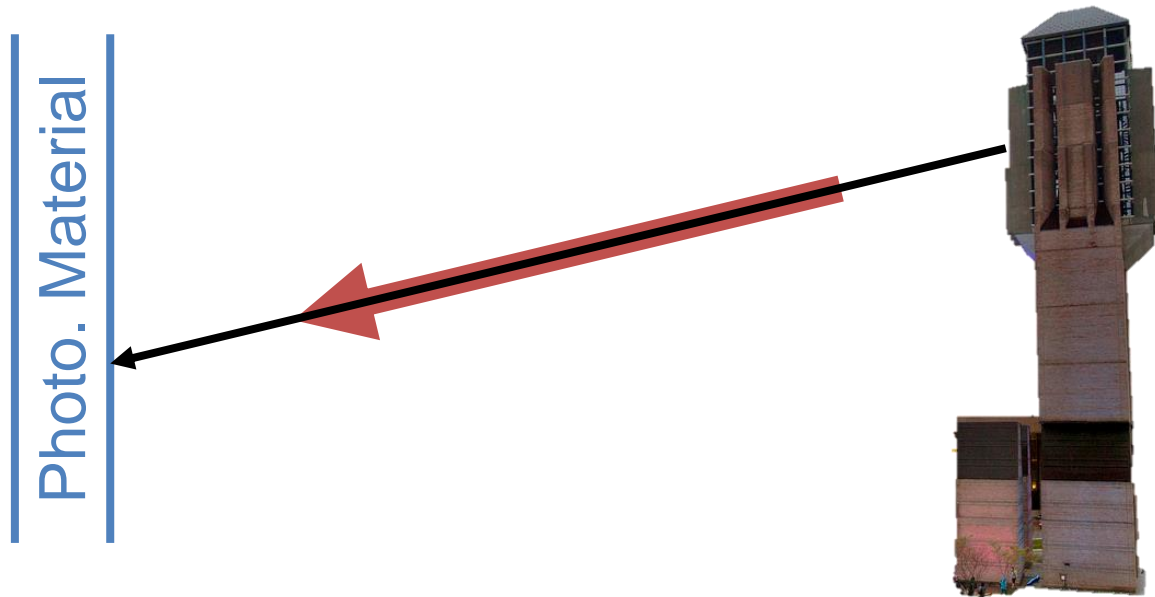
# Other Images

- A small part of computer vision in this class is really only for ordinary images
- The rest is easily generalized to other images
- Really transformative stuff will happen when good vision techniques get traction in other areas

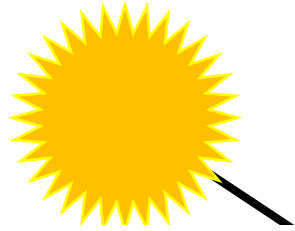


# So Far

How do we represent **light**  
and its storage on **film**?



Now

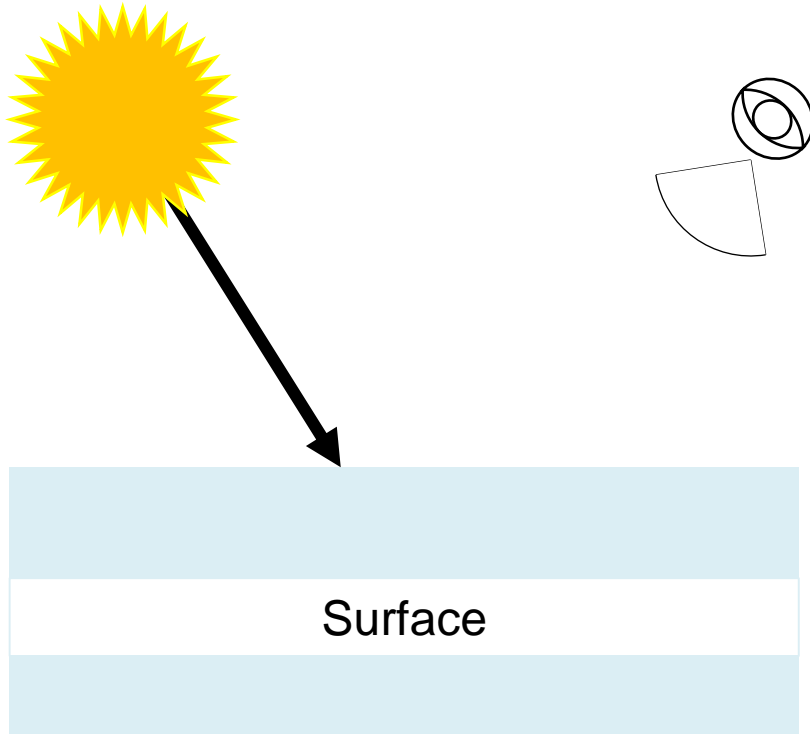


How does the scene  
cause that **light**?

Photo. Material

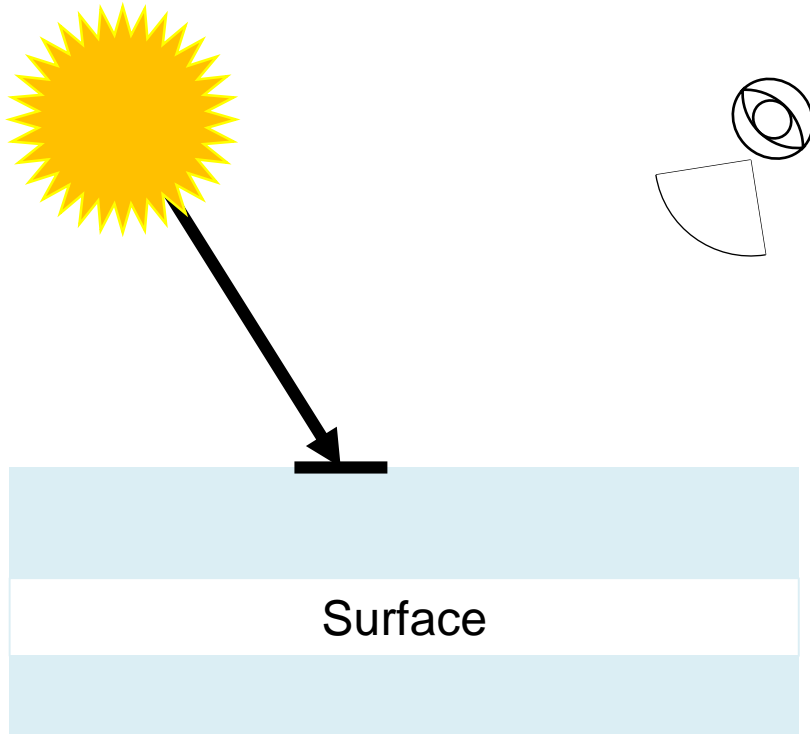


# Light and Surfaces



What happens when  
light hits a surface?

# Light and Surfaces

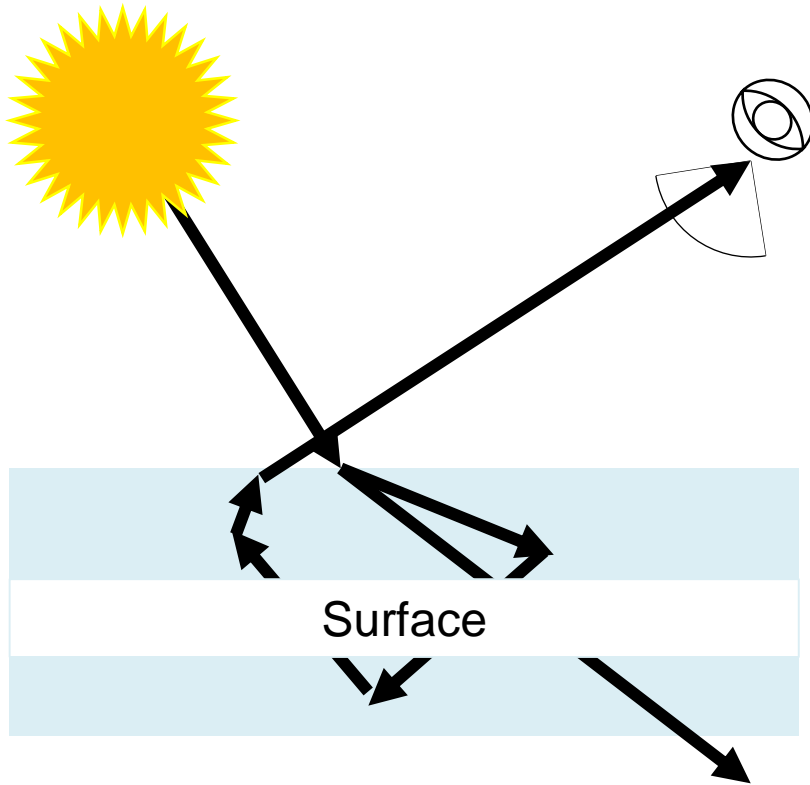


What happens when light hits a surface?

## **1. Absorbed**

It's absorbed and converted into some other form of energy (e.g., a black shirt getting hot in the sun)

# Light and Surfaces

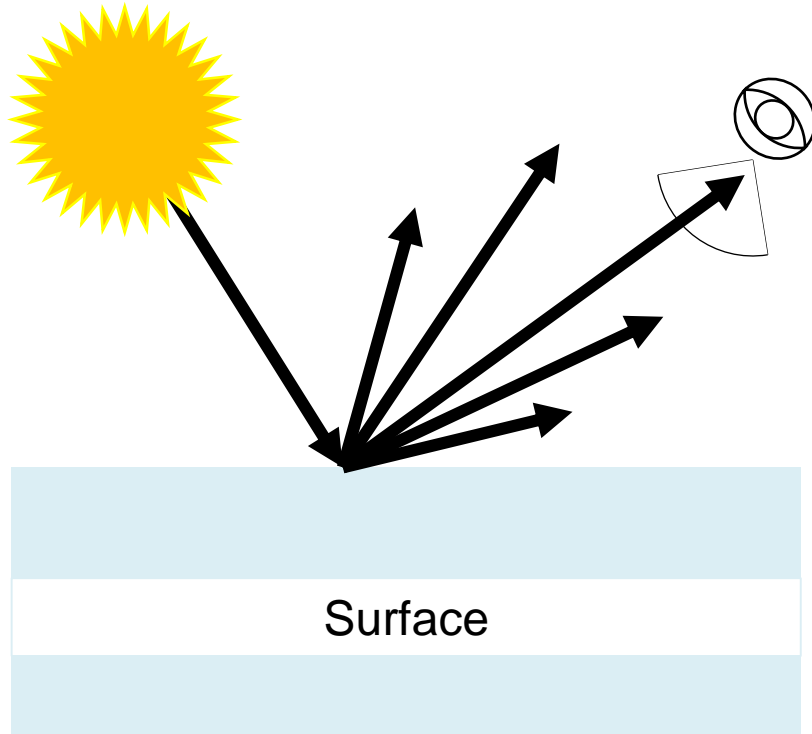


What happens when light hits a surface?

## 2. Transmitted

Possibly bouncing around before going through or out (e.g. lenses bend and go through, milk bounces around)

# Light and Surfaces

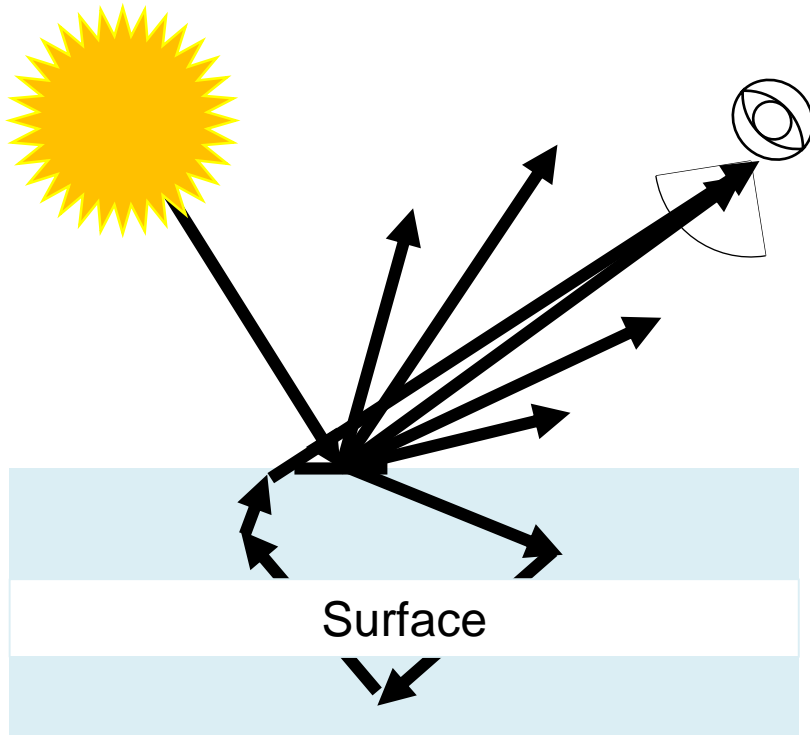


What happens when light hits a surface?

## **3. Reflected**

It's reflected back, in one or more directions with varying amounts (e.g., mirror, or a white surface)

# Light and Surfaces



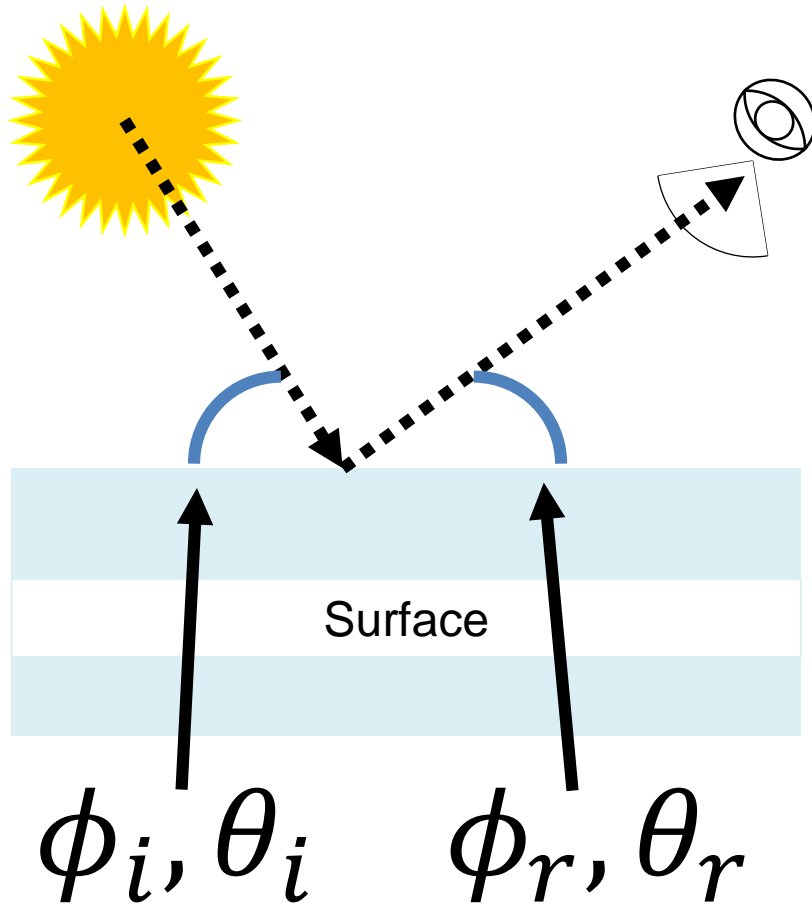
What happens when light hits a surface?

## 4. Everything

All of the above! Real surfaces often have combinations of all of these options.



# Modeling Light and Surfaces



## Opaque Reflections

Bi-directional reflectance function: % reflected given *incident angle* to light *reflected angle* to the viewer.

***Note: have not specified form of function.***

# Specular and Diffuse Reflection

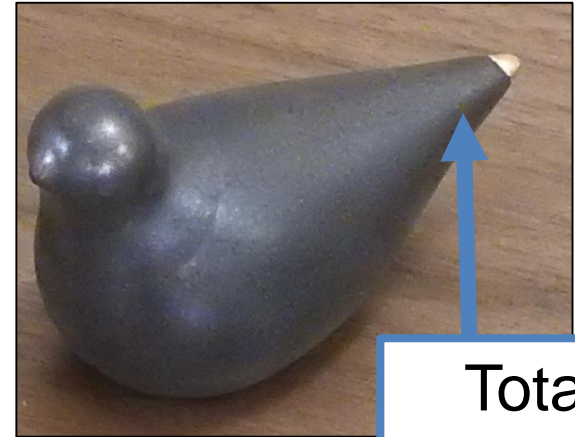
Same lighting, as close as possible camera settings, but different **location**



# Specular and Diffuse Reflection

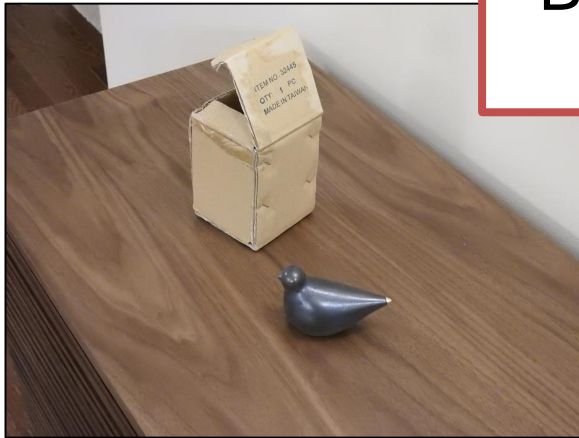
Diffuse

Specular

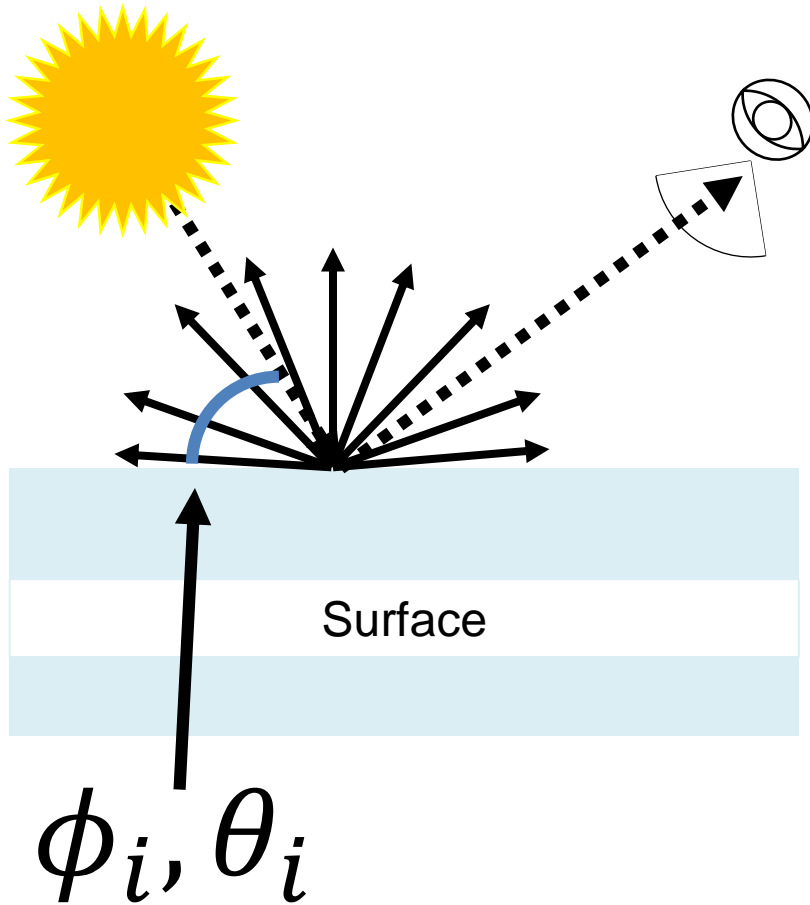


Basically same

Totally different



# Diffuse Reflection



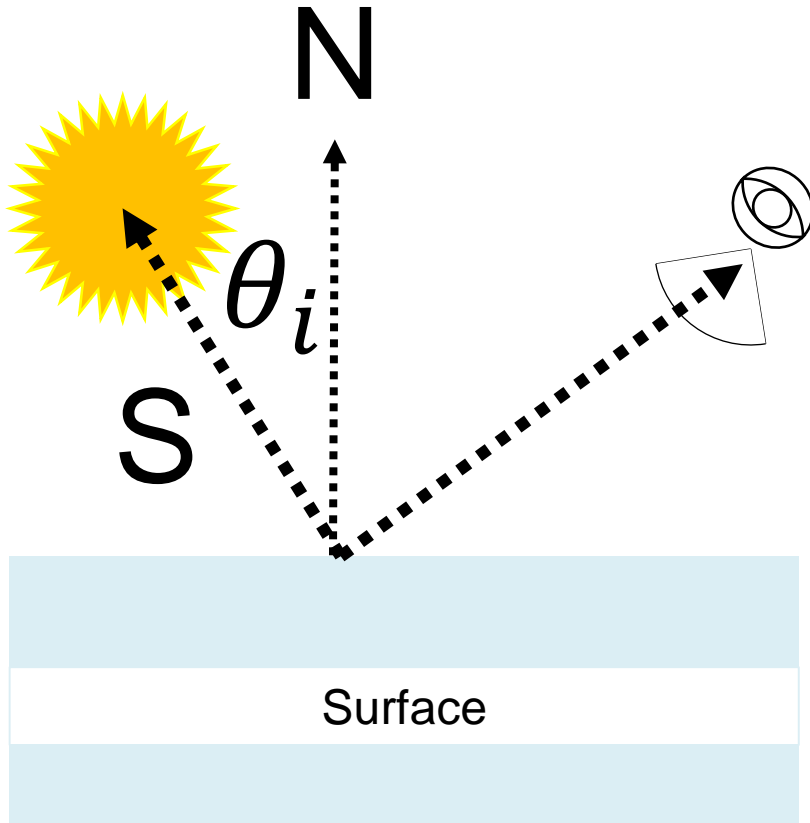
## Lambertian Surface

Light depends **only** on orientation of surface

$$\phi_i, \theta_i$$

to light. Result of random small facets. Looks identical at all views.

# Diffuse Reflection



## Lambert's Law

N: surface normal

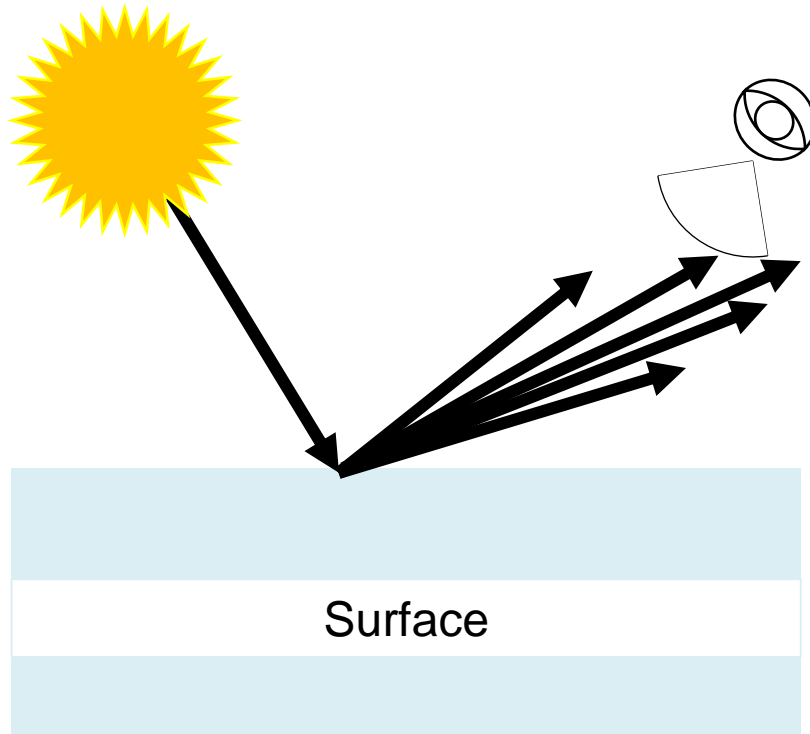
S: source direction **and**  
strength

$\rho$ : how much is reflected

$$B = \rho \mathbf{N} \cdot \mathbf{S}$$

$$B = \rho \|\mathbf{S}\| \cos(\theta)$$

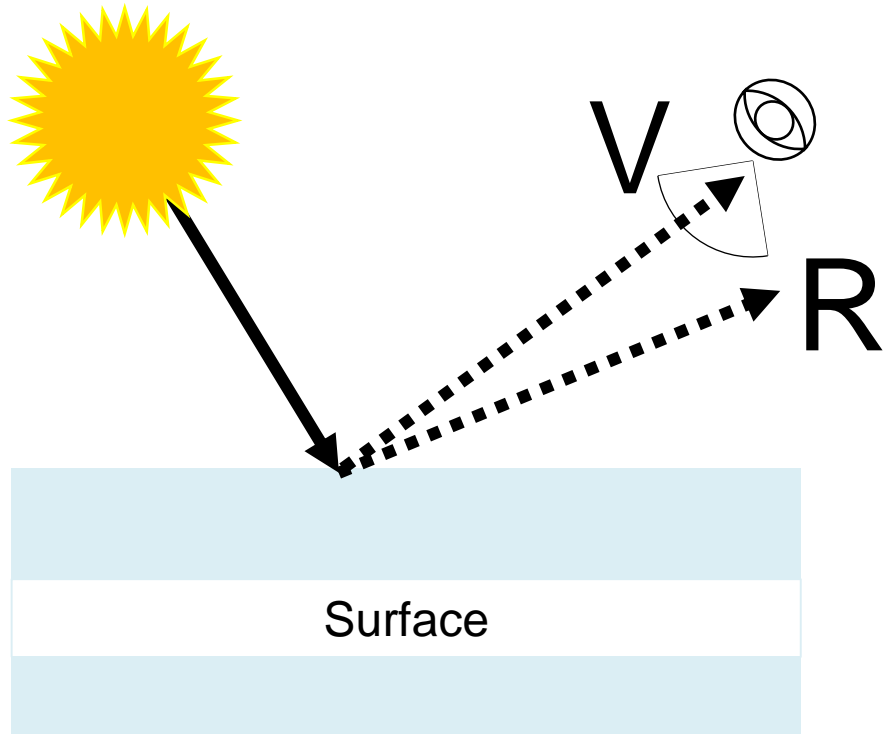
# Specular Reflection



## Specular Surface

Light reflected like a mirror, but spreads out in a “lobe” around the reflection ray

# Specular Reflection



## Phong Model

V: vector to viewer

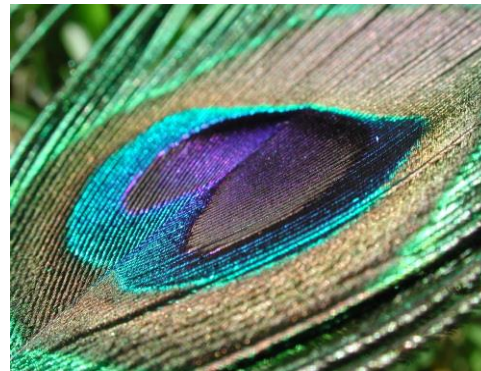
R: reflection ray

$\alpha$ : shininess constant

$$B = (V^T R)^\alpha$$



# BRDFs can be incredibly complicated...





# What Can This Be Used For

## Shape from Shading

Lambert's Law: for every pixel  $i$

$$B_i = \rho N_i \cdot S$$

Reflected  
Light  
(1 dim)

Surface  
Orientation  
(3? dim)

Illumination  
Global,  
(3 dim)

Given: illumination and light, recover normals

**Potential problems?**

# Shape From Shading

$$B_i = \rho N_i \cdot S$$

1D, **fixed**      actually 2D      3D, **fixed**  
**unknown**

- System of equations that's underdetermined (N equations, 2N unknowns, N+3 known)
- **Solution:** Add more equations that enforce smoothness or finding a single surface.

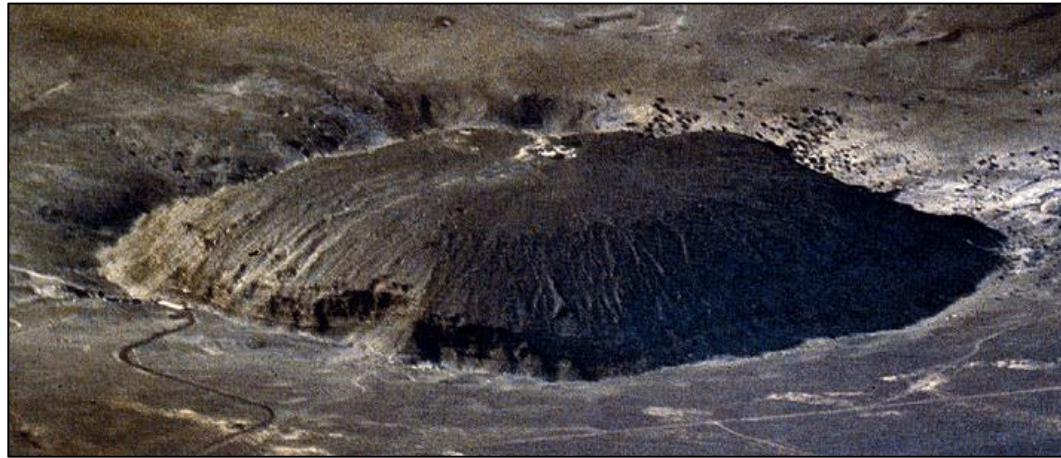
# Realistic Shape From Shading

$$B_i = \rho N_i \cdot S$$

1D, fixed                      2D unknown                      3D, unknown

- System of equations that's underdetermined (N equations, 2N+3 unknowns)
- **Solution:** need prior beliefs to disambiguate.

# Ambiguity



# Ambiguity

Humans assume light from above (and the blueness also tells you distance)



# Shape from Shading in Practice

<https://www.youtube.com/watch?v=4GiLAOtjHNo>