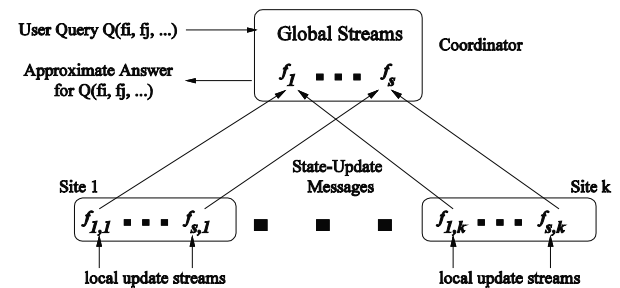
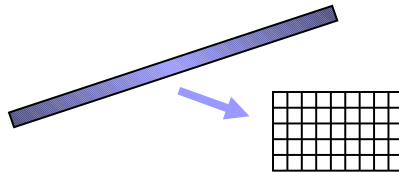


# A Quick Introduction to Data Stream Algorithmics



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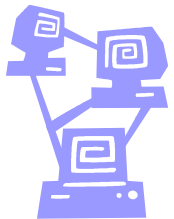
# Streams – A Brave New World

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- **Traditional DBMS:** data stored in *finite, persistent data sets*
- **Data Streams:** distributed, continuous, unbounded, rapid, time varying, noisy, . . .
- **Data-Stream Management:** variety of modern applications
  - Network monitoring and traffic engineering
  - Sensor networks
  - Telecom call-detail records
  - Network security
  - Financial applications
  - Manufacturing processes
  - Web logs and clickstreams
  - Other massive data sets...

# Massive Data Streams

- Data is *continuously growing* faster than our ability to store or index it
- There are 3 Billion **Telephone Calls** in US each day, 30 Billion emails daily, 1 Billion SMS, IMs
- **Scientific data**: NASA's observation satellites generate billions of readings each per day
- **IP Network Traffic**: up to 1 Billion packets per hour per router. Each ISP has many (hundreds) routers!
- Whole **genome sequences** for many species now available: each megabytes to gigabytes in size



# Massive Data Stream Analysis

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Must analyze this massive data:

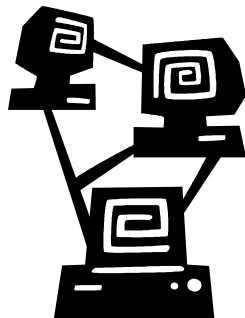
- Scientific research (monitor environment, species)
- System management (spot faults, drops, failures)
- Business intelligence (marketing rules, new offers)
- For revenue protection (phone fraud, service abuse)

Else, why even measure this data?



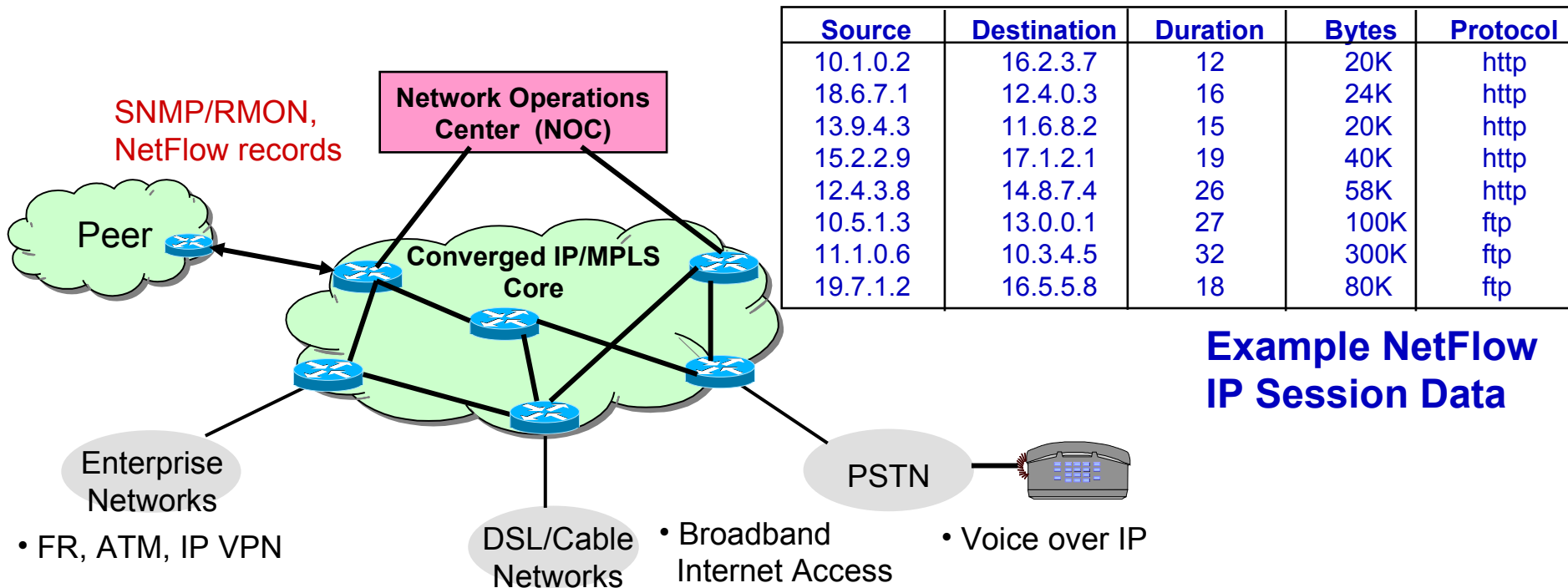
# Example: IP Network Data

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- Networks are sources of massive data: the **metadata** per hour per IP router is gigabytes
- Fundamental problem of data stream analysis:  
*Too much information to **store** or transmit*
- So process data as it arrives – *One pass, small space: the **data stream** approach*
- *Approximate answers* to many questions are OK, if there are guarantees of result quality

# IP Network Monitoring Application



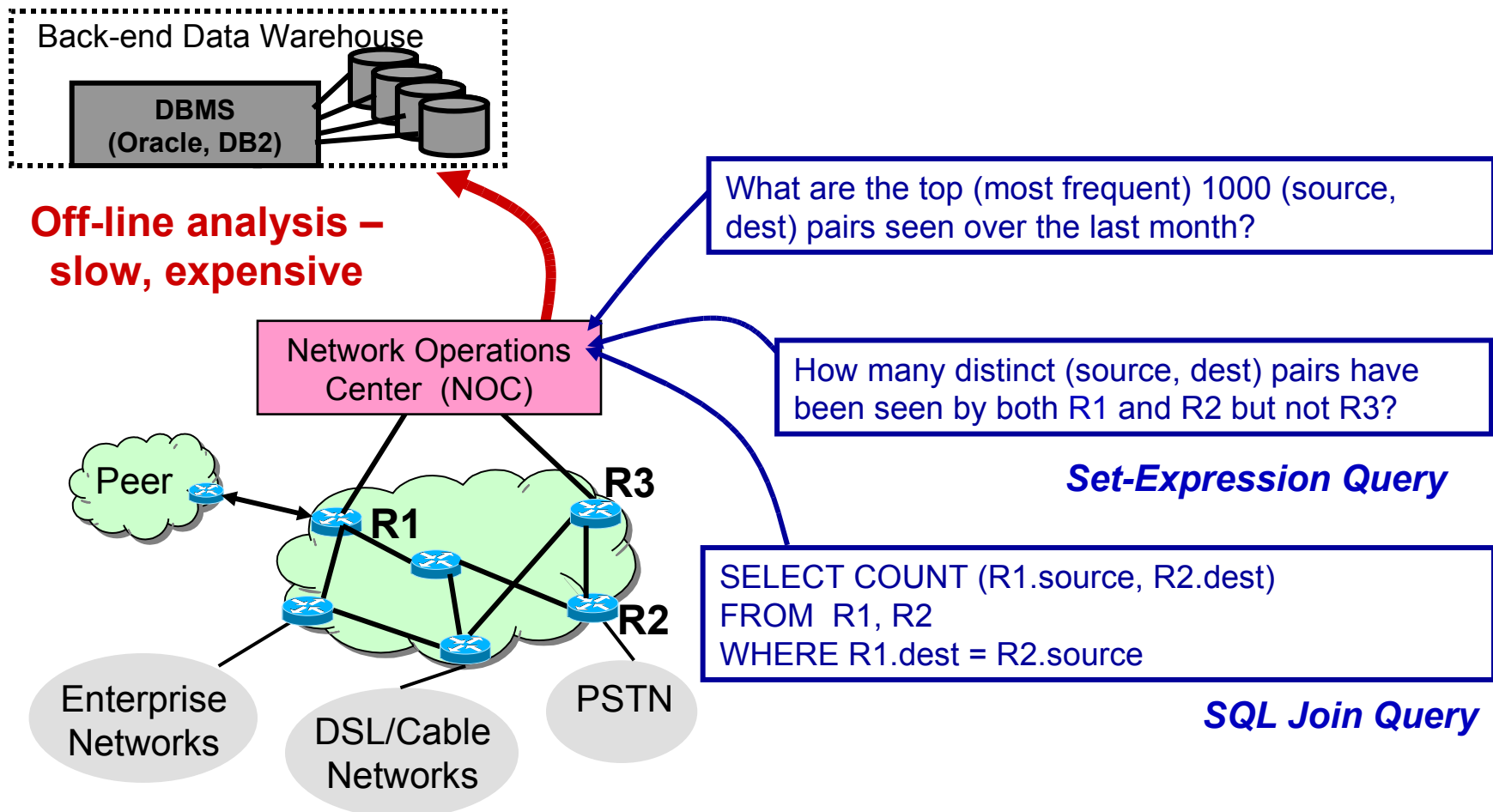
- 24x7 IP packet/flow data-streams at network elements
- Truly massive streams arriving at rapid rates
  - AT&T/Sprint collect *~1 Terabyte* of NetFlow data *each day*
- Often shipped off-site to data warehouse for off-line analysis

# Packet-Level Data Streams

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- Single 2Gb/sec link; say avg packet size is 50bytes
- Number of packets/sec = 5 million
- Time per packet = 0.2 microsec
- If we only capture **header information** per packet: src/dest IP, time, no. of bytes, etc. – at least 10bytes.
  - Space per second is 50Mb
  - Space per day is 4.5Tb per link
  - ISPs typically have hundreds of links!
- Analyzing **packet content streams** – whole different ballgame!!

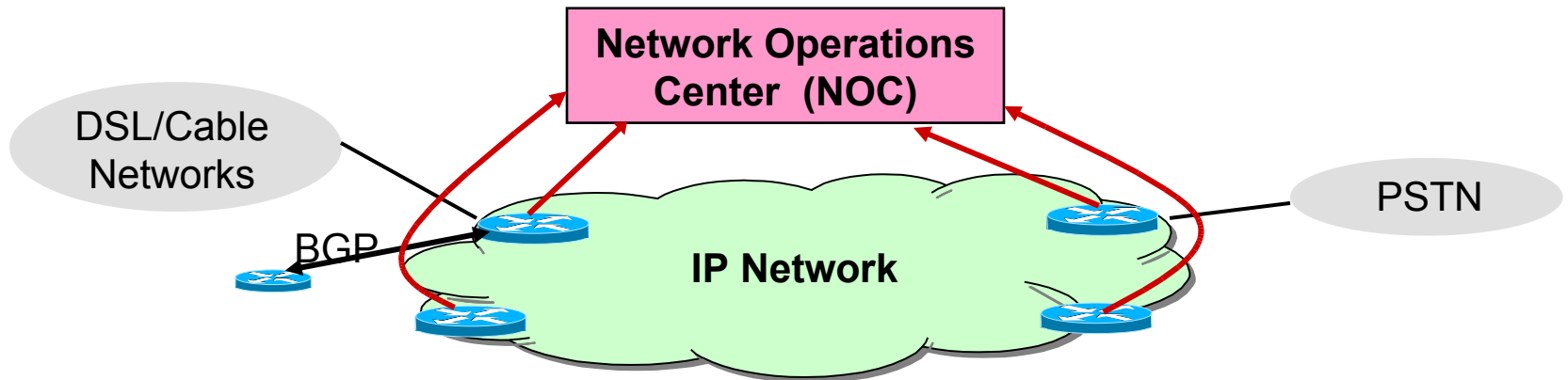
# Network Monitoring Queries



- Extra complexity comes from *limited space and time*
- Solutions exist for these and other problems



# Real-Time Data-Stream Analysis

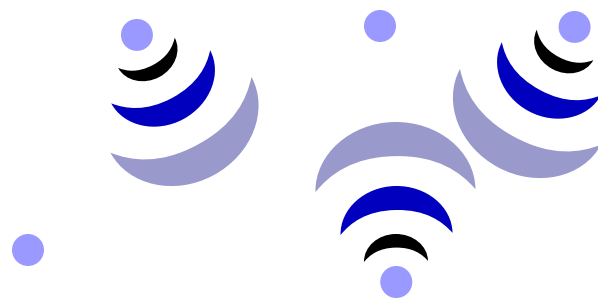


- Must process network streams in *real-time* and *one pass*
- Critical NM tasks: fraud, DoS attacks, SLA violations
  - Real-time traffic engineering to improve utilization
- *Tradeoff result accuracy vs. space/time/communication*
  - Fast responses, small space/time
  - Minimize use of communication resources

# Sensor Networks

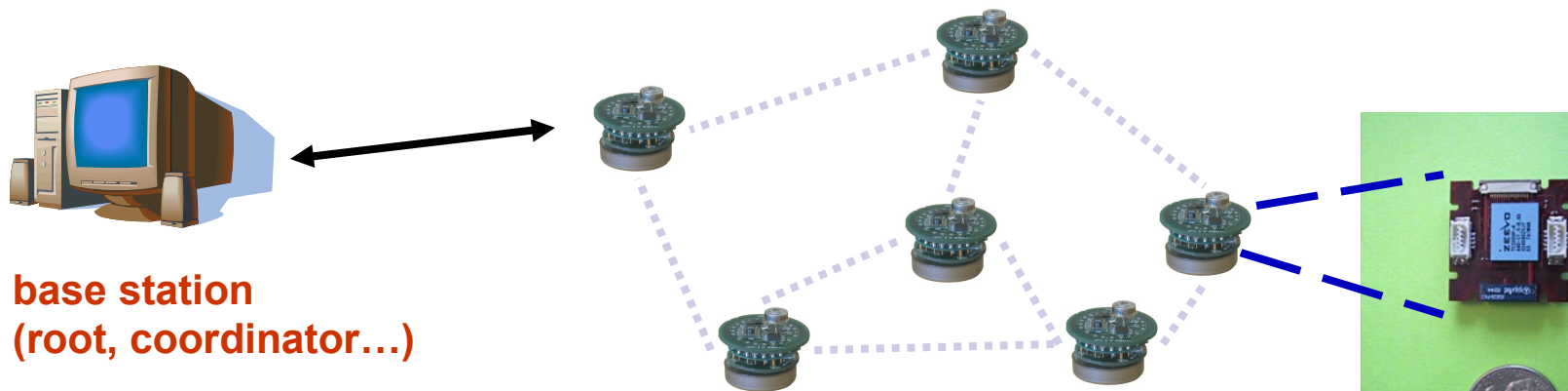
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- Wireless sensor networks becoming ubiquitous in environmental monitoring, military applications, ...
- Many (100s,  $10^3$ ,  $10^6$ ?) sensors scattered over terrain
- Sensors observe and process a local stream of readings:
  - Measure light, temperature, pressure...
  - Detect signals, movement, radiation...
  - Record audio, images, motion...



# Sensornet Querying Application

- Query sensornet through a (remote) *base station*
- Sensor nodes have **severe resource constraints**
  - Limited battery power, memory, processor, radio range...
  - *Communication* is the major source of battery drain
  - “transmitting a single bit of data is equivalent to 800 instructions” [Madden et al.'02]



# Lecture Outline

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- Motivation & Streaming Applications
- Centralized Stream Processing
  - Basic streaming models and tools
  - Stream synopses and applications
    - Sampling, sketches
- Conclusions

# Data Streaming Model

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- **Underlying signal:** One-dimensional array  $A[1\dots N]$  with values  $A[i]$  all initially zero
  - Multi-dimensional arrays as well (e.g., row-major)
- Signal is implicitly represented via a ***stream of update tuples***
  - $j$ -th update is  $\langle x, c[j] \rangle$  implying
    - $A[x] := A[x] + c[j]$  ( $c[j]$  can be  $>0$ ,  $<0$ )
- **Goal: Compute functions on  $A[]$**  subject to
  - Small space
  - Fast processing of updates
  - Fast function computation
  - ...
- Complexity arises from massive length and domain size ( $N$ ) of streams

# Example IP Network Signals

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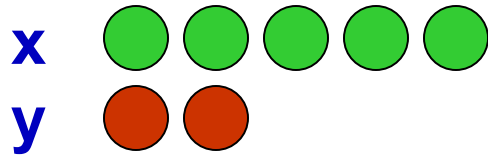
- Number of bytes (packets) sent by a source IP address during the day
  - $2^{32}$  sized one-d array; increment only
- Number of flows between a source-IP, destination-IP address pair during the day
  - $2^{64}$  sized two-d array; increment only, aggregate packets into flows
- Number of **active** flows per source-IP address
  - $2^{32}$  sized one-d array; increment and decrement

# Streaming Model: Special Cases

## ■ Time-Series Model

- Only  $x$ -th update updates  $A[x]$  (i.e.,  $A[x] := c[x]$ )

## ■ Cash-Register Model: Arrivals-Only Streams

- $c[x]$  is always  $> 0$
- Typically,  $c[x]=1$ , so we see a multi-set of items in one pass
- Example:  $\langle x, 3 \rangle, \langle y, 2 \rangle, \langle x, 2 \rangle$  encodes the arrival of 3 copies of item  $x$ , 2 copies of  $y$ , then 2 copies of  $x$ .  
The diagram shows two rows of colored circles. The top row is labeled with a blue 'x' and contains five green circles. The bottom row is labeled with a blue 'y' and contains two red circles.
- Could represent, e.g., packets on a network; power usage

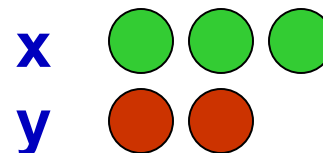
# Streaming Model: Special Cases

## ■ Turnstile Model: Arrivals and Departures

- Most general streaming model
- $c[x]$  can be  $>0$  or  $<0$

## ■ Arrivals and departures:

- Example:  $\langle x, 3 \rangle, \langle y, 2 \rangle, \langle x, -2 \rangle$  encodes final state of  $\langle x, 1 \rangle, \langle y, 2 \rangle$ .



- Can represent fluctuating quantities, or measure differences between two distributions

## ■ *Problem difficulty varies depending on the model*

- E.g., MIN/MAX in Time-Series vs. Turnstile!



# Approximation and Randomization

---

- Many things are hard to compute exactly over a stream
  - Is the count of all items the same in two different streams?
  - Requires linear space to compute exactly
- **Approximation**: find an answer correct within some factor
  - Find an answer that is within **10%** of correct result
  - More generally, a  $(1 \pm \epsilon)$  factor approximation
- **Randomization**: allow a small probability of failure
  - Answer is correct, except with probability 1 in 10,000
  - More generally, success probability  $(1 - \delta)$
- **Approximation and Randomization**:  $(\epsilon, \delta)$ -approximations

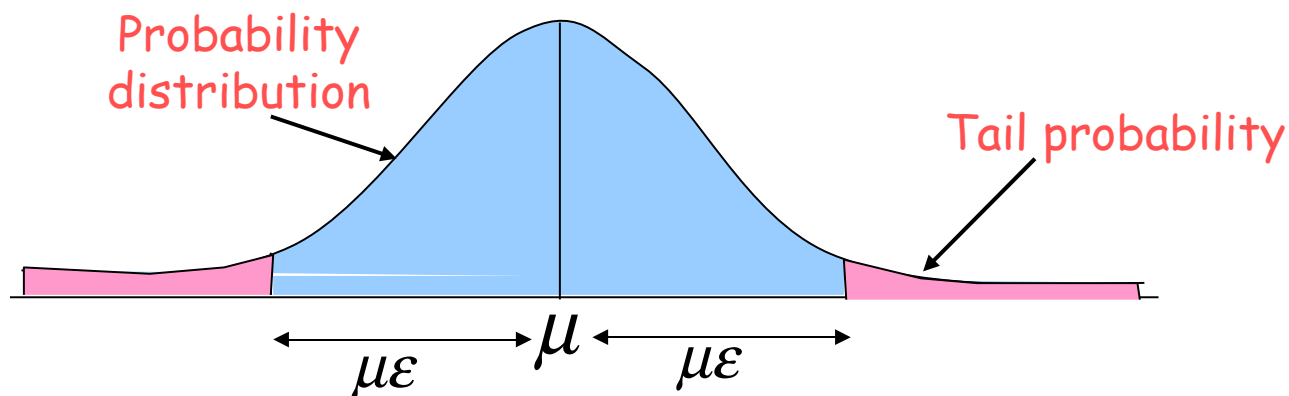
# Probabilistic Guarantees

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- User-tunable  $(\epsilon, \delta)$ -approximations
  - Example: Actual answer is within  $5 \pm 1$  with prob  $\geq 0.9$
- Randomized algorithms: Answer returned is a specially-built *random variable*
  - *Unbiased* (correct on expectation)
  - Combine several *Independent Identically Distributed (iid)* instantiations (average/median)
- Use *Tail Inequalities* to give probabilistic bounds on returned answer
  - *Markov Inequality*
  - *Chebyshev Inequality*
  - *Chernoff Bound*
  - *Hoeffding Bound*

# Basic Tools: Tail Inequalities

- General bounds on *tail probability* of a random variable (that is, probability that a random variable deviates far from its expectation)



- Basic Inequalities: Let  $X$  be a random variable with expectation  $\mu$  and variance  $\text{Var}[X]$ . Then, for any  $\epsilon > 0$

**Markov:**

$$\Pr(X \geq (1 + \epsilon)\mu) \leq \frac{1}{1 + \epsilon}$$

**Chebyshev:**

$$\Pr(|X - \mu| \geq \mu\epsilon) \leq \frac{\text{Var}[X]}{\mu^2 \epsilon^2}$$

# Tail Inequalities for Sums

- Possible to derive stronger bounds on tail probabilities for the **sum of independent random variables**
- Hoeffding Bound: Let  $X_1, \dots, X_m$  be independent random variables with  $0 \leq X_i \leq r$ . Let  $\bar{X} = \frac{1}{m} \sum_i X_i$  and  $\mu$  be the expectation of  $\bar{X}$ . Then, for any  $\varepsilon > 0$ ,

$$\Pr(|\bar{X} - \mu| \geq \varepsilon) \leq 2 \exp \frac{-2m\varepsilon^2}{r^2}$$

- *Application*: Sample average  $\approx$  population average
  - See below...

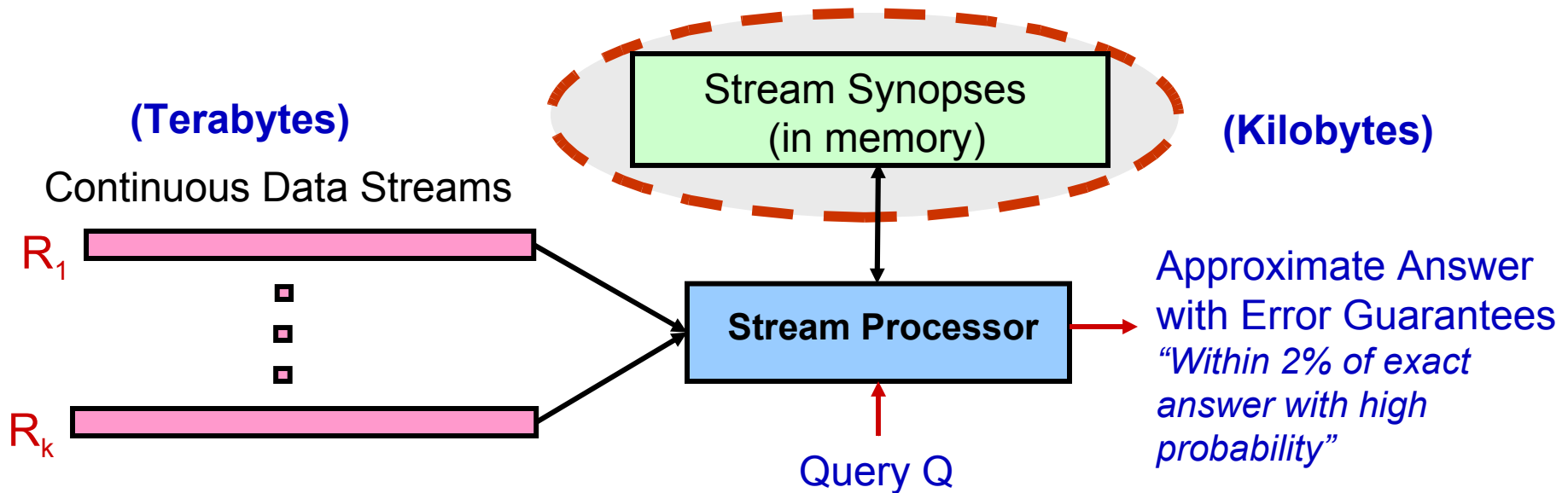
# Tail Inequalities for Sums

- Possible to derive even stronger bounds on tail probabilities for the sum of *independent Bernoulli trials*
- Chernoff Bound: Let  $X_1, \dots, X_m$  be independent Bernoulli trials such that  $\Pr[X_i=1] = p$  ( $\Pr[X_i=0] = 1-p$ ). Let  $X = \sum_i X_i$  and  $\mu = mp$  be the expectation of  $X$ . Then, for any  $\varepsilon > 0$ ,

$$\Pr(|X - \mu| \geq \mu\varepsilon) \leq 2 \exp \frac{-\mu\varepsilon^2}{2}$$

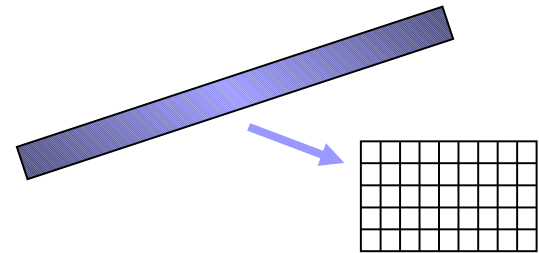
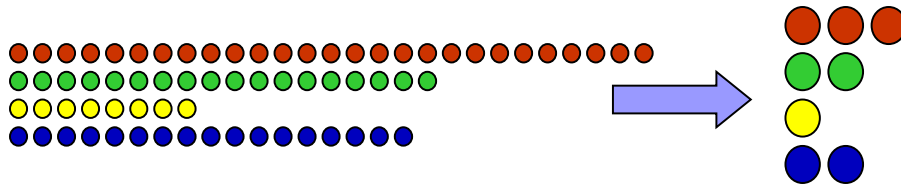
- *Application*: Sample selectivity  $\approx$  population selectivity
  - See below...
- *Remark*: Chernoff bound results in tighter bounds for *count queries* compared to Hoeffding bound

# Data-Stream Algorithmics Model



- *Approximate answers*– e.g. trend analysis, anomaly detection
- Requirements for stream synopses
  - *Single Pass*: Each record is examined at most once
  - *Small Space*: Log or polylog in data stream size
  - *Small-time*: Low per-record processing time (maintain synopses)
  - Also: *delete-proof*, *composable*, ...

# Sampling & Sketches



# Sampling: Basics

- Idea: A small random sample  $S$  of the data often well-represents all the data
  - For a fast approx answer, apply “modified” query to  $S$
  - Example: select agg from  $R$  where  $R.e$  is odd

( $n=12$ ) Data stream: 9 3 5 2 7 1 6 5 8 4 9 1

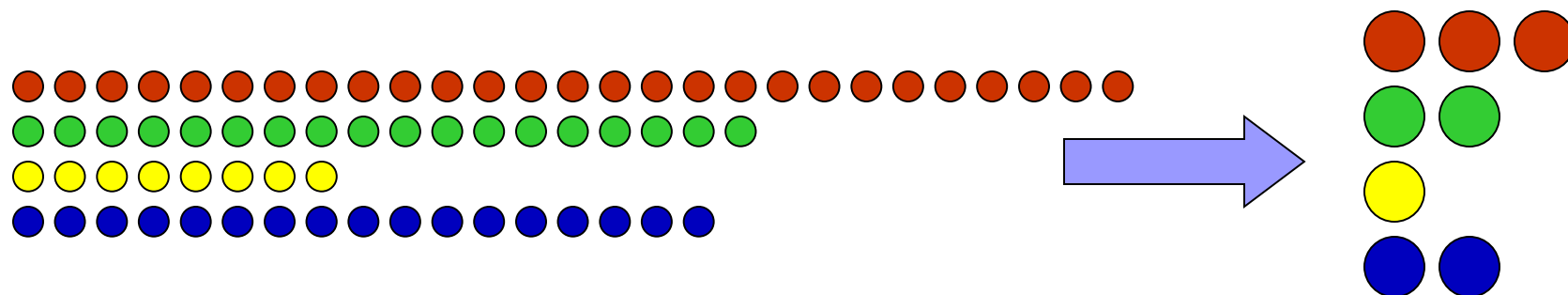
Sample  $S$ : 9 5 1 8

- If agg is avg, return average of odd elements in  $S$  answer: 5
- If agg is count, return average over all elements  $e$  in  $S$  of
  - $n$  if  $e$  is odd
  - $0$  if  $e$  is evenanswer:  $12 * 3/4 = 9$

- Unbiased Estimator (for count, avg, sum, etc.)
  - Bound error using *Hoeffding* (sum, avg) or *Chernoff* (count)



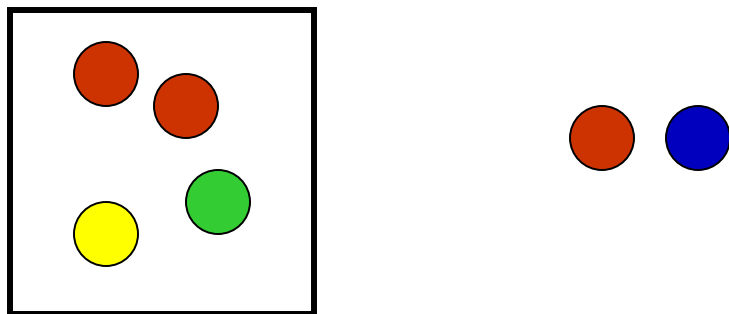
# Sampling from a Data Stream



- Fundamental problem: sample  $m$  items uniformly from stream
  - Useful: approximate costly computation on small sample
- **Challenge**: don't know how long stream is
  - So when/how often to sample?
- Two solutions, apply to different situations:
  - Reservoir sampling (dates from 1980s?)
  - Min-wise sampling (dates from 1990s?)

# Reservoir Sampling

---



- Sample first  $m$  items
- Choose to sample the  $i$ 'th item ( $i > m$ ) with probability  $m/i$
- If sampled, randomly replace a previously sampled item
- **Optimization:** when  $i$  gets large, compute which item will be sampled next, skip over intervening items [Vitter'85]

# Reservoir Sampling - Analysis

- Analyze simple case: sample size  $m = 1$
- Probability  $i$ 'th item is the sample from stream length  $n$ :
  - Prob.  $i$  is sampled on arrival  $\times$  prob.  $i$  survives to end

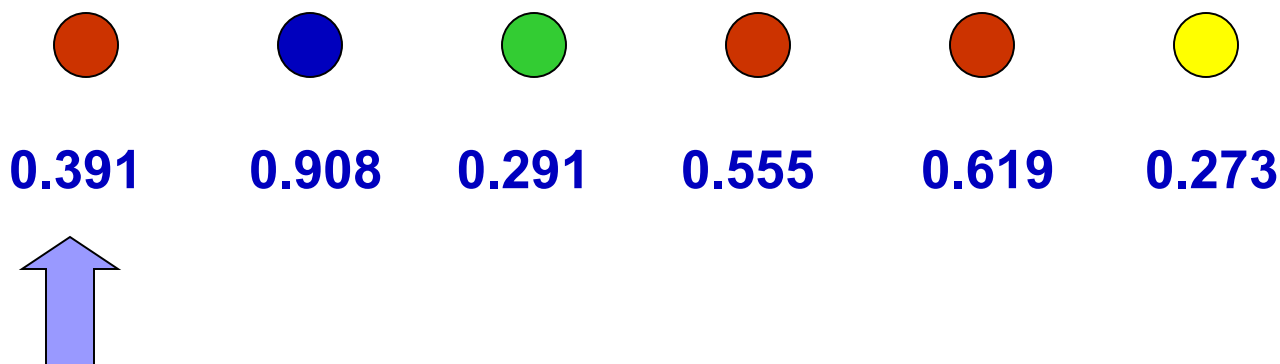
$$\frac{1}{i} \times \frac{\cancel{i}}{\cancel{i+1}} \times \frac{\cancel{i+1}}{\cancel{i+2}} \cdots \frac{\cancel{n-2}}{\cancel{n-1}} \times \frac{\cancel{n-1}}{n}$$

$= 1/n$

- Case for  $m > 1$  is similar, easy to show uniform probability
- Drawbacks of reservoir sampling: hard to parallelize

# Min-wise Sampling

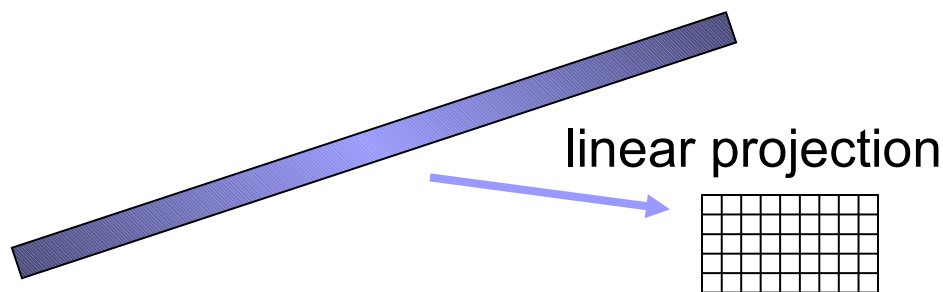
- For each item, pick a random fraction between 0 and 1
- Store item(s) with the smallest random tag [Nath et al.'04]



- Each item has same chance of least tag, so uniform
- Can run on multiple streams separately, then merge

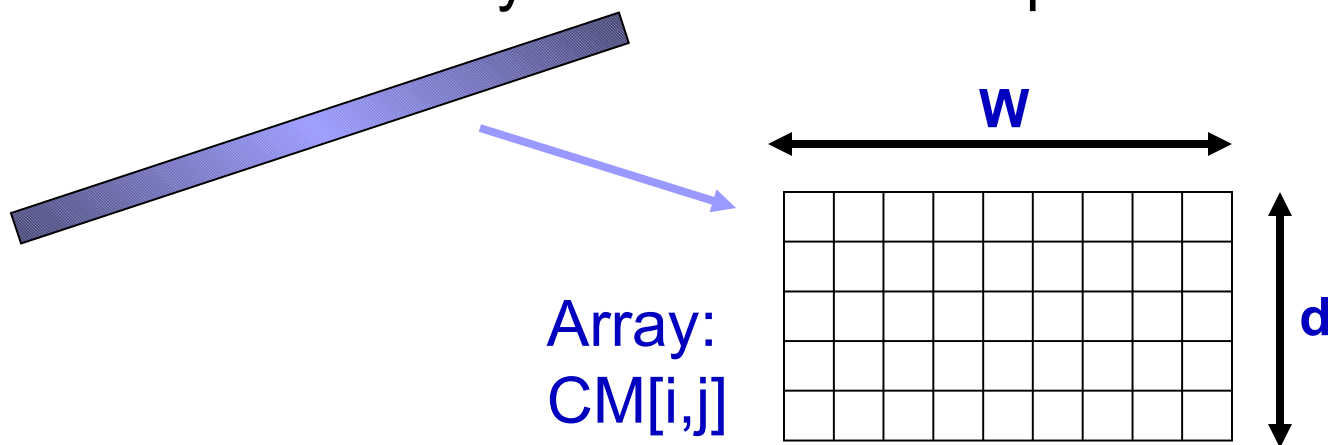
# Sketches

- Not every problem can be solved with sampling
  - **Example**: counting how many distinct items in the stream
  - If a large fraction of items aren't sampled, don't know if they are all same or all different
- Other techniques take advantage that the algorithm can “see” all the data even if it can't “remember” it all
- **“Sketch”**: essentially, a linear transform of the input
  - Model stream as defining a vector, sketch is result of multiplying stream vector by an (implicit) matrix

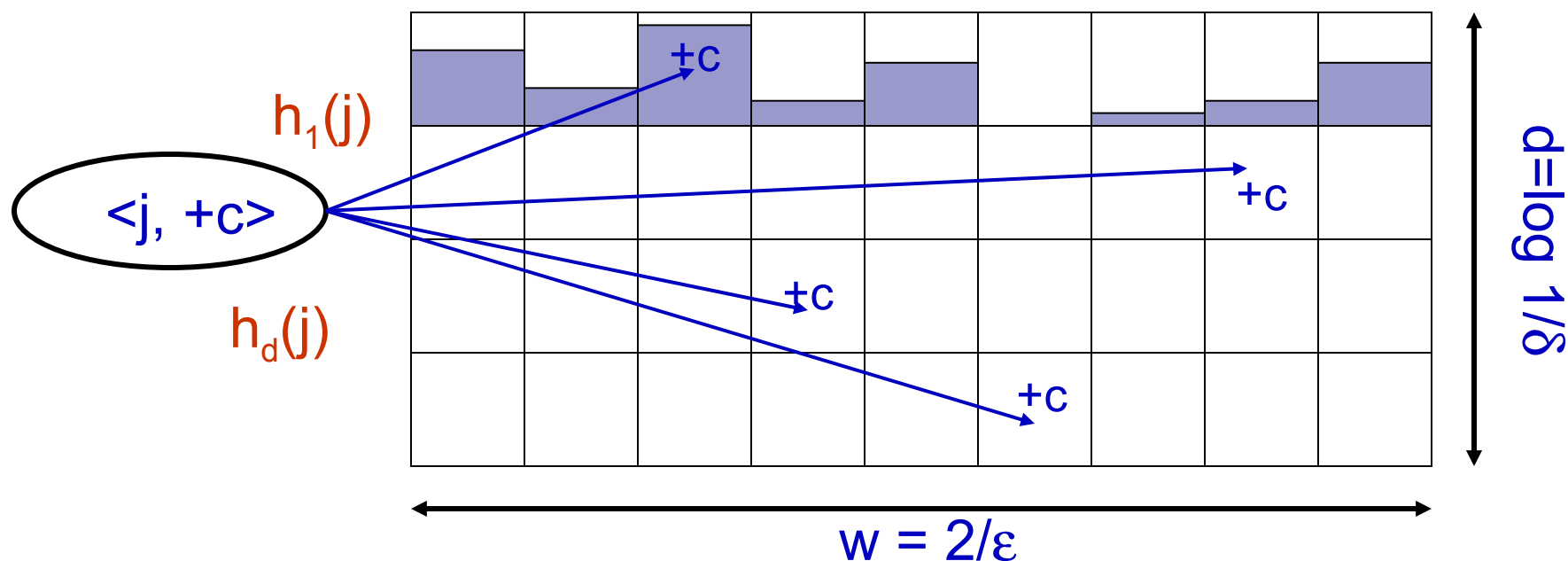


# Count-Min Sketch [Cormode, Muthukrishnan'04]

- Simple sketch idea, can be used for as the basis of many different stream mining tasks
  - Join aggregates, range queries, moments, ...
- Model input stream as a vector  $A$  of dimension  $N$
- Creates a small summary as an array of  $w \times d$  in size
- Use  $d$  hash functions to map vector entries to  $[1..w]$
- Works on arrivals only and arrivals & departures streams



# CM Sketch Structure



- Each entry in input vector  $A[]$  is mapped to one bucket per row
  - $h()$ 's are *pairwise independent*
- Merge two sketches by entry-wise summation
- Estimate  $A[j]$  by taking  $\min_k \{ CM[k, h_k(j)] \}$

# CM Sketch Guarantees

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- [Cormode, Muthukrishnan'04] CM sketch guarantees approximation error on point queries less than  $\epsilon \|A\|_1$  in space  $O(1/\epsilon \log 1/\delta)$ 
  - Probability of more error is less than  $1-\delta$
  - Similar guarantees for range queries, quantiles, join size,...
- Hints
  - Counts are *biased (overestimates)* due to collisions
    - Limit the expected amount of extra “mass” at each bucket?
  - **Use independence across rows** to boost the confidence for the `min{}` estimate
    - Based on independence of row hashes



# CM Sketch Analysis

Estimate  $A'[j] = \min_k \{ \text{CM}[k, h_k(j)] \}$

- Analysis: In  $k$ 'th row,  $\text{CM}[k, h_k(j)] = A[j] + X_{k,j}$ 
  - $X_{k,j} = \sum A[i] \mid h_k(i) = h_k(j)$
  - $E[X_{k,j}] = \sum A[i] \cdot \Pr[h_k(i) = h_k(j)]$   
 $\leq (\epsilon/2) * \sum A[i] = \epsilon \|A\|_1 / 2$  (pairwise independence of  $h$ )
  - $\Pr[X_{k,j} \geq \epsilon \|A\|_1] = \Pr[X_{k,j} \geq 2E[X_{k,j}]] \leq 1/2$  by **Markov inequality**
- So,  $\Pr[A'[j] \geq A[j] + \epsilon \|A\|_1] = \Pr[\forall k. X_{k,j} > \epsilon \|A\|_1] \leq 1/2^{\log 1/\delta} = \delta$
- Final result: with certainty  $A[j] \leq A'[j]$  and with probability at least  $1-\delta$ ,  $A'[j] < A[j] + \epsilon \|A\|_1$

# Distinct Value Estimation

- **Problem:** Find the *number of distinct values* in a stream of values with domain  $[1, \dots, N]$ 
  - Zeroth frequency moment  $F_0$ , L0 (Hamming) stream norm
  - Statistics: number of *species or classes* in a population
  - Important for query optimizers
  - *Network monitoring*: distinct destination IP addresses, source/destination pairs, requested URLs, etc.

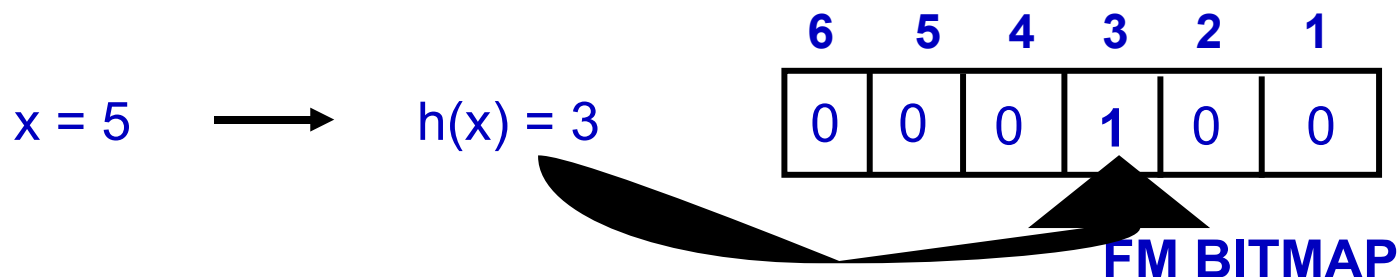
■ Example (N=64) Data stream: 3 2 5 3 2 1 7 5 1 2 3 7

*Number of distinct values: 5*

- Hard problem for random sampling! [Charikar et al.'00]
  - Must sample almost the entire table to guarantee the estimate is within a factor of 10 with probability  $> 1/2$ , regardless of the estimator used!
- AMS and CM only good for *multiset semantics*

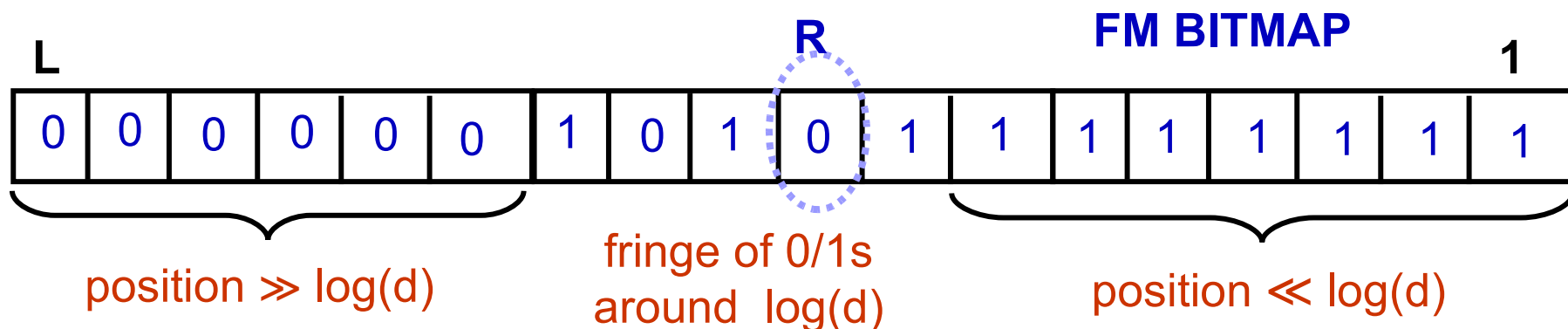
# FM Sketch [Flajolet, Martin'85]

- Estimates number of distinct inputs (**count distinct**)
- Uses hash function mapping input items to  $i$  with prob  $2^{-i}$ 
  - i.e.  $\Pr[h(x) = 1] = 1/2$ ,  $\Pr[h(x) = 2] = 1/4$ ,  $\Pr[h(x)=3] = 1/8$  ...
  - Easy to construct  $h()$  from a uniform hash function by counting trailing zeros
- Maintain FM Sketch = bitmap array of  $L = \log N$  bits
  - Initialize bitmap to all 0s
  - For each incoming value  $x$ , set  $FM[h(x)] = 1$



# FM Sketch Analysis

- If  $d$  distinct values, expect  $d/2$  map to  $FM[1]$ ,  $d/4$  to  $FM[2]$ ...



- Let  $R$  = position of rightmost zero in FM, indicator of  $\log(d)$
- Basic estimate  $d = c2^R$  for scaling constant  $c \approx 1.3$
- Average many copies (different hash fns) improves accuracy

# FM Sketch Properties

- With  $O(1/\epsilon^2 \log 1/\delta)$  copies, get  $(1 \pm \epsilon)$  accuracy with probability at least  $1 - \delta$  [Bar-Yossef et al.'02], [Ganguly et al.'04]
  - 10 copies gets  $\approx 30\%$  error, 100 copies  $< 10\%$  error
- *Delete-Proof*: Use counters instead of bits in sketch locations
  - +1 for inserts, -1 for deletes
- *Composable*: Component-wise OR/add distributed sketches together

$$\begin{array}{cccccc} 6 & 5 & 4 & 3 & 2 & 1 \\ \hline 0 & 0 & 1 & 0 & 1 & 1 \end{array} + \begin{array}{cccccc} 6 & 5 & 4 & 3 & 2 & 1 \\ \hline 0 & 1 & 1 & 0 & 0 & 1 \end{array} = \begin{array}{cccccc} 6 & 5 & 4 & 3 & 2 & 1 \\ \hline 0 & 1 & 1 & 0 & 1 & 1 \end{array}$$

- Estimate  $|S_1 \cup \dots \cup S_k| = \text{set union cardinality}$

# Sketching and Sampling Summary

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- Sampling and sketching ideas are at the heart of many stream mining algorithms
  - Moments/join aggregates, histograms, wavelets, top-k, frequent items, other mining problems, ...
- A sample is a quite **general representative** of the data set; sketches tend to be *specific to a particular purpose*
  - FM sketch for count distinct, CM/AMS sketch for joins / moment estimation, ...
- Traditional sampling does not work in the **turnstile (arrivals & departures) model**
  - **BUT...** see recent generalizations of distinct sampling [Ganguly et al.'04], [Cormode et al.'05]; as well as [Gemulla et al.'08]

# Practicality

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- Algorithms discussed here are quite simple and very fast
  - Sketches can easily process millions of updates per second on standard hardware
  - Limiting factor in practice is often I/O related
- Implemented in several practical systems:
  - AT&T's Gigascope system on live network streams
  - Sprint's CMON system on live streams
  - Google's log analysis
- Sample implementations available on the web
  - <http://www.cs.rutgers.edu/~muthu/massdal-code-index.html>
  - or web search for 'massdal'

# Conclusions

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- **Data Streaming:** Major departure from traditional persistent database paradigm
  - Fundamental re-thinking of models, assumptions, algorithms, system architectures, ...
- Many new streaming problems posed by developing technologies
- Simple tools from **approximation and/or randomization** play a critical role in effective solutions
  - Sampling, sketches (CM, FM, ...), ...
  - Simple, yet powerful, ideas with **great reach**
  - Can often “**mix & match**” for specific scenarios





<http://www.cs.berkeley.edu/~minos/>

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