# PLL On-Chip Jitter Measurement: Analysis and Design

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#### **Abstract**

Analysis of on-chip jitter measurements based on the dead-zone method reveals potentially large errors in the jitter variance estimate, when the jitter distribution is changing or not known a priori. To overcome this, a more accurate variance estimation method is proposed and experimentally verified. The residual error, caused by the correlated noise between the PLL and the measurement circuit, is fully characterized and circuit topologies are proposed to mitigate this type of error.

## Introduction

On-chip jitter measurement has been proposed to adaptively optimize the PLL performance [1,2]. This paper studies the limitations of on-chip jitter measurement based on the dead-zone method and improves on it by proposing a new jitter metric.

Fig. 1a shows the jitter measurement circuit based on the dead-zone method [3]. The phase of the PLL output clock is compared to that of the delayed reference clock  $\phi_{REF}$ . The control voltage of the delay line (VCDL) is adjusted so that the  $\phi_{REF}$  phase converges to the specified tails of the jitter distribution. The dead zone width is assumed to be a measure of the RMS jitter, Fig. 1b. The tunable PLL uses a dual-charge-pump, self-biased architecture [4] with charge pump currents that are controlled by 4-bit DACs. The damping factor is proportional to the current  $I_{CP2}$ . For low values of  $I_{CP2}$ , the damping factor decreases causing peaking of the noise transfer function and increase of the PLL jitter. For high values of  $I_{CP2}$ , the PLL jitter increases again due to increased phase detector frequency spurs and/or lower phase margin. The minimum jitter corresponds to intermediate values of  $I_{CP2}$ .

### **Error Sources of On-Chip Jitter Measurement**

The RMS jitter estimate based on the dead-zone measurement method may be inaccurate, if the jitter distribution shape varies at different operating points. Furthermore, various noise sources induce jitter both in the PLL and the measurement circuit, and this noise correlation may affect the measurements.

To study the performance of the jitter measurement procedure, the PLL and the jitter measurement circuit were implemented in a 0.13  $\mu$ m CMOS process, Fig. 2. At 1 GHz, the PLL and measurement circuits consume 17mW and 10mW, respectively. Power consumption of the measurement circuit is less important, as it can be powered down after it determines the optimal PLL operating point. A delay line is used to align the PLL output clock with the reference phase  $\phi_{REF}$  at the beginning of each experiment, in order to increase the dynamic range of the measurements. The same effect is achieved by increasing the length of the VCDL in the measurement circuit. The jitter estimation algorithm was implemented in software for

added flexibility. A digital oscilloscope is used to verify the accuracy of the on-chip measurements.

Fig. 3 shows the measured variance of the PLL jitter at various damping factors while operating at 1GHz along with jitter histograms from scope measurements. At high damping factors the jitter distribution changes to bimodal Gaussian due to the periodic jitter from the phase detector spur. As the distribution deviates from Gaussian, the error due to the deadzone method increases. This indicates that the minimum jitter could be correctly identified from on-chip jitter estimates, if the variance could be calculated more accurately from arbitrary jitter histograms.

#### **Jitter Variance Metric**

To combat the dead-zone errors, a new jitter variance metric (*VM*) is proposed, which makes no assumption about the shape of the jitter distribution:

$$VM = \sum_{k=-K+1}^{K-1} [(K-k) \cdot H_k + (k+K) \cdot (N-H_k)]$$
 (1),

where  $H_k$  is the cumulative number of hits at position k, N is the number of edges compared during a measurement, and 2K-1 is the number of histogram partitions, Fig. 4a. Fig. 4b shows the VM calculations for the histograms of Fig. 3. If the histogram partition width  $\Delta x$  is small enough, the shape of the VM curve follows that of the measured jitter curve. The proposed algorithm utilizes the simple hardware of Fig. 1a, and its implementation does not require multiplication, as shown in the simplified schematic of Fig. 5. The histogram partition counter controls the DAC, which determines the phase  $\phi_{REF}$ . The control logic ensures that the term  $H_k$  (N- $H_k$ ) is added K-k (k+K) times during the VM calculation, see Eq. (1), where k is the histogram partition index.

## **Residual Error**

After compensating for the dead-zone error, the residual error is due to correlated noise between the PLL and the measurement circuit. The on-chip measurement estimates the jitter of the phase difference between the two clocks at the input of the phase arbiter:

Var $[\phi_{PLL} - \phi_{REF}]$  = Var $[\phi_{PLL}]$  + Var $[\phi_{REF}]$  - 2 · Cov $[\phi_{PLL}, \phi_{REF}]$  (2). The correlation term  $-2 \cdot \text{Cov}[\phi_{PLL}, \phi_{REF}]$ , caused both by supply/substrate noise and reference clock jitter, depends on the PLL operating point, and may affect the jitter estimates.

The variation of the correlation errors across the PLL operating points is relatively small, Fig. 6. The correlation errors due to supply noise affect the relative jitter values more than the ones due to refclk jitter. Almost all of the supply correlation error is produced by the interaction of the supply noise spectrum spur at the refclk frequency, Fig. 7a, with the component of the PLL phase detector spur due to supply noise,

Fig. 7b. It can be shown that this main component of the supply correlation error can be removed by eliminating the alignment delay line.

Thus, with adequate jitter metric and appropriate circuit topology, very accurate on-chip jitter measurements can be performed and used for PLL adaptation.

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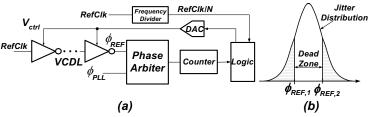


Fig. 1: (a) Jitter measurement circuit, (b) Dead-zone method.

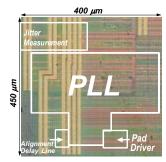


Fig. 2: Die photo.

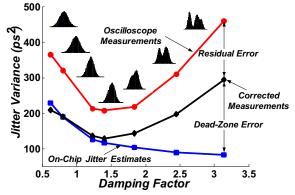


Fig. 3: Jitter measurement results.

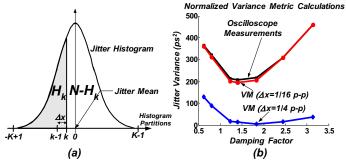


Fig. 4: (a) Definition of variables for variance metric calculation, (b) Normalized variance metric calculations for different histogram partition widths  $\Delta x$  (defined as fractions of p-p jitter).

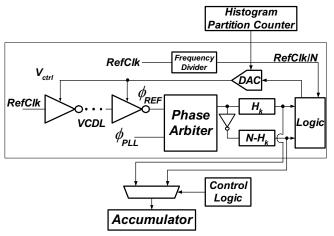


Fig. 5: Simplified block schematic for variance metric calculation.

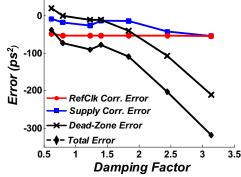


Fig. 6: Components of measurement error.

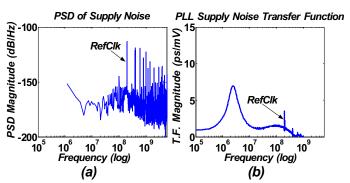


Fig. 7: (a) Supply noise spectrum, (b) PLL supply noise transfer function.