Inferring and Assisting with Constraints in Shared Autonomy

Negar Mehr, Roberto Horowitz, Anca D. Dragan

Abstract—Our goal is to enable robots to better assist people with motor impairments in day-to-day tasks. Currently, such robots are teleoperated, which is tedious. It requires carefully maneuvering the robot by providing input through some interface. This is further complicated because most tasks are filled with constraints, e.g., on how much the end effector can tilt before the glass that the robot is carrying spills. Satisfying these constraints can be difficult or even impossible with the latency, bandwidth, and resolution of the input interface. We seek to make operating these robots more efficient and reduce cognitive load on the operator. Given that manipulation research is not advanced enough to make these robots autonomous in the near term, achieving this goal requires finding aspects of these tasks that are difficult for human operators to achieve, but easy to automate with current capabilities. We propose constraints are the key: maintaining task constraints is the most difficult part of the task for operators, yet it is easy to do autonomously. We introduce a method for inferring constraints from operator input, along with a confidence-based way of assisting the user in maintaining them, and evaluate in a user study.

I. INTRODUCTION

Decades ago, industrial robots were developed to automate dirty, dull, and dangerous tasks, and they purposely eschewed human involvement for reasons of speed and safety. In stark contrast, a new generation of medical and health care robots is designed for direct interaction with human users in environments such as the surgical theater, the rehabilitation center, and the family room. Teleoperated robots such as the da Vinci Surgical System are used to perform minimally invasive surgery around the world, resulting in shorter recovery times and more reliable outcomes in select procedures [1]–[3]. Physically assistive systems are being developed for in-home use to help limited mobility users with Activities of Daily Living (ADLs) [4]–[7].

These robots have the potential to help doctors and patients alike with performing tasks that are difficult for them to accomplish with their own body: robots have access to quantitative data about tasks and environments, and can move accurately without tiring. Despite this, integrating them with human users still presents significant challenges in performance and user acceptance, for two reasons. On the one hand, teleoperating and controlling these robots is tedious and does not take advantage of many of the potential advantages of artificial intelligence and robot mechanisms. On the other hand, current manipulation research is not advanced enough to make these robots autonomous in medical and health care environments in the near term.

Our insight is that there are important aspects of manipulation tasks that are difficult for human operators to achieve, but relatively easy to automate with current capabilities.

Rather than attempting full automation, we propose to automate these aspects. We focus on task constraints as the key, because maintaining task constraints is the most difficult part of many tasks for human operators, yet autonomous systems can easily keep track of and satisfy multiple constraints. Figure 4 shows examples of constraints encountered in ADLs, including orientation and position constraints: in order to place a book in the bookshelf, its orientation needs to be aligned with the other books; to wipe a board, the end-effector is constrained to move along the plane of the board; or the end-effector has to traverse an arc when opening the door of a refrigerator.

Two challenges make assisting human operators with maintaining tasks constraints difficult: 1) inferring which constraint the operator is trying to enforce, and 2) deciding how to provide assistance once a constraint is inferred. Our contributions are in line with these challenges:

Constraint Inference: Typically, constraint inference is done from multiple demonstrations of the same task [8]–[11]. In shared autonomy, however, the robot needs to infer the constraint from a single ongoing execution of the task. We introduce a constraint inference algorithm, capable of online inference of task constraints from the ongoing stream of user’s control inputs and trajectory of the robot in the task space. Our approach is based on the Moving Window KPCA [12], a variant of Kernel Principle Component Analysis (KPCA) [13]. This enables the robot to handle non-linear constraints online, inferring the constraint solely based on the most recent control inputs in order to make the computation real-time.

Moving Window KPCA identifies a constraint in feature space. To enforce the constraint, the robot has to first map the user input into feature space, and then project it onto the constraint. This gives the robot a direction in feature space, but does not identify the constraint in task space. We contribute a preimage learning technique that learns to approximately project a feature space direction back in the robot’s task space, which the robot can then follow (e.g., via Jacobian-based or IK-based controllers).

Assisting with (Changing) Constraints: Given a predicted constraint, the robot has to decide how and how much to assist the user. One option is to enforce the
predicted constraint, but this can be catastrophic if the robot has the wrong prediction. Building on [14], we propose to mediate assistance by the robot’s confidence in the constraint. We introduce a confidence measure capable of dealing with the fact that constraints may be changing over time, or that the user might be going from no constraint to a constraint and vice-versa.

**User Study Evaluation:** We conduct two user studies with novice users in which we measure the effectiveness of our algorithm in assisting users with maintaining task constraints. When dealing with a single constraint, our results support that users prefer to be assisted by the robot, and their objective measure of performance improves significantly by means of assistance. When dealing with switching constraints, our measure of confidence enables the robot to stop assisting and make it easier for the user to perform the switch, improving subjective and objective measures.

**II. Related Work**

**Shared Autonomy.** The very first instance of shared autonomy (or shared control) was in manipulators utilized for transporting radioactive material, where the low accuracy of user control input can lead to violating safety criteria [15]. Since then, various methods have been introduced [16]–[21].

[14] characterized the problem of shared control in tasks where there is continuous user input as arbitrating between the user input and a robot predicted policy, showing how many algorithms instantiate this characterization by using different predictors and different arbitration functions. This is the paradigm we adopt as well. However, instead of predicting the operator’s desired goal and assuming that the robot can achieve it as in [14], we predict desired *constraints*. This requires more limited robot capability, yet still captures a difficult aspect of the task for the operator.

**Virtual Fixtures.** Virtual fixtures [22] are the most related type of shared autonomy to the topic of this work. Virtual fixtures assist the operator with maintaining constraints by constraining or guiding either the user’s input or the robot itself [23], [24]. Implementations in abstract and surgical environments have demonstrated the effectiveness of static virtual fixtures, as well as the role of haptic feedback in two-degree-of-freedom guidance [25]–[27].

Thus far, the assumption has been that the robot *knows* the constraint (fixture) to maintain. In this work, we enable the robot to *infer* it from operator data and control inputs. This is not only an inference challenge, but also an assistance challenge because the robot is no longer certain of what fixture or constraint the user wants.

**Constraint Inference.** Although inferring constraints has not been actively studied in teleoperation, it has been a focus in Learning from Demonstration [28]. There, constraints are identified as the invariants among a set of demonstrated trajectories for the same task [8]–[11].

Unlike Learning from Demonstration, our robot does not get access to multiple training trajectories for the same task. Instead, in teleoperation, the robot needs to infer the constraint being maintained along a trajectory online, as the trajectory is being observed.

**III. Problem Statement**

In this section, we formulate the problems of constraint inference and assistance.

**A. Online Constraint Inference**

Let $s \in S$ denote the state, here the end-effector task space in $\text{SE}(3)$ and $u_t \in U$ be the control input that the user provides (via some interface, e.g. a joystick) at time $t$. We represent a constraint that a user might attempt to satisfy, e.g. keeping a bottle of water upright, as the zero set of some function $h$ of the state $s$. The set of states satisfying a constraint $c$ denoted by $S_c \in S$ is:

$$S_c = \{s | h(s) = 0\}, \quad h : S \to \mathbb{R}^+$$  (1)

Given the operator’s control input from the starting time to the current time step $t$, $u_0, \cdots, u_t$, and the robot trajectory so far, $s_0, \cdots, s_t$, the constraint inference problem requires finding the function $h_t$ that characterizes the constraint the operator currently wants to maintain.

Fig. 1: Example constraints for ADL-assistive robotics with a Kinova arm that will be mounted to a wheelchair.
B. Assistance with Maintaining Constraints

Once the robot has an inference of the constraint, the question is how to deploy this prediction in assisting the user. Particularly, given the current state $s_t$, the user input $u_t$, and the current prediction $h_t$, the robot needs to decide whether and how to modify $u_t$ to assist the user.

IV. INFERRING AND ASSISTING WITH CONSTRAINTS

A. Online Constraint Inference

Given the states, $L_t = \{s_0, \cdots, s_t\}$, that noisily satisfy a constraint $h_t$, along with the user input vector $\{u_0, \cdots, u_t\}$ the goal is to infer $h_t$. Because the zero set of $h_t$ is a manifold in $S$, manifold learning is a natural choice for identifying the constraint.

Manifold learning algorithms attempt to find a lower dimensional representation of given points such that a certain proximity criteria is met in a lower dimensional subset of data points. There exists a large number of manifold learning algorithms [29]–[33] that could possibly be utilized in inferring $h_t$. The distinction between the existing manifold learning algorithms arises from the type of proximity criteria that they try to optimize, or the class of functions they can learn for $h_t$.

Constraint inference raises some requirements for manifold learning that narrow down which algorithms are applicable. First, manifolds might be non-linear. Second, manifolds need to be learned online, in real time, as the operator’s input data is coming in.

Kernel PCA

The requirements above point to Kernel Principle Component Analysis [13] (KPCA) as the basis of our work. In this method, principle components can be found in a non-linear feature space defined by the choice of a kernel function. KPCA maps the data points to a non-linear, possibly infinite dimensional feature space $F$, through a non-linear feature mapping $\phi$:

$$s \mapsto \phi(s) \in F,$$

and computes principle components of the mapped data points, $\{\phi(s_0), \cdots, \phi(s_t)\}$, in the obtained feature space.

Nominally, this would be achieved by computing the eigenvectors of the covariance matrix $C$ of mapped data points in $F$:

$$C_t = \frac{1}{t} \sum_{i=1}^{t} \phi(s_i)\phi(s_i)^T \quad (2)$$

The main idea behind KPCA is to compute the principal components without ever mapping the data to feature space, or even explicitly defining $\phi$. Instead, KPCA operates by introducing a kernel function $k$ and implicitly defining $\phi$ such that $k(s_i, s_j) = \langle \phi(s_i), \phi(s_j) \rangle$. It constructs a $t \times t$ kernel matrix $K$ via $K_{ij} = k(s_i, s_j)$. Each principle component, $v_l$, can be written as a linear combination of $\phi(s_i)$’s:

$$v_l = \sum_{i=1}^{t} a_i^l \phi(s_i). \quad (3)$$

The vector of coefficients $a_i^l$, denoted by $a^l$, can be computed solely from $K$ by solving:

$$t \lambda a = Ka, \quad (4)$$

where $\lambda$ is an eigenvalue of $K$, and $a$ is its corresponding eigenvector.

Note that in the above, for the sake of simplicity, we have assumed that the data is centered in the feature space, i.e. $\sum_{i=1}^{t} \phi(s_i) = 0$. In general, this does not need to hold. In that case, we need the eigendecomposition of the Gram matrix $G$ instead of $K$:

$$G = K - \frac{1}{t} K E_t - \frac{1}{t} E_t K + \frac{1}{t^2} E_t K E_t, \quad (5)$$

where $E_t$ is the $t \times t$ matrix with all entries equal to 1. See [12] for more details.

Note that the output of KPCA is the set of vectors $a$. As a result, the projection of a state $s$ on the $i^{th}$ kernel principle component of data points can be computed from $a_i$ using the kernel function, without explicitly computing $\phi(s)$:

$$\langle v_l, \phi(s) \rangle = \sum_{i=1}^{t} a_i^l \langle \phi(s_i), \phi(s) \rangle = \sum_{i=1}^{t} a_i^l k(s_i, s), \quad (6)$$

where $a_i^l$ is the $i^{th}$ entry in the vector of $a$ corresponding to the $i^{th}$ kernel principle component.

Projecting $s$ on $h_t$ in feature space means projecting $\phi(s)$ onto the first $D$ principle components according to the largest $D$ eigenvalues:

$$P_S = \sum_{l=1}^{D} \frac{\langle v_l, \phi(s) \rangle}{\langle v_l, v_l \rangle} v_l \quad (8)$$

We discuss raising $P_S$ back into task space in “Enforcing an Inferred Constraint” below.

Online KPCA

Running KPCA over the entire set of user-provided states and control inputs is computationally prohibitive. We make KPCA online by using a finite time horizon: a moving window where the newest user input point replaces the oldest one, and we reuse computation from the previous step whenever the window moves.

We perform KPCA for a rolling constant-length horizon of $M$ data points, $L_t = \{s_{t-M+1}, \cdots, s_t\}$. This implies that at time $t + 1$, a new data point, $s_{t+1}$ is received and the very first element of the horizon of data, $s_{t-M+1}$, is removed from the history of data points. This updates the matrix $K$.

Running KPCA over a time horizon of $M$ still requires the eigendecomposition of $K$ at each step, which
is in \(O(M^3)\). To overcome this computational hindrance of KPCA, we need to reuse the computation performed in the previous time steps. Liu et al. [12] show that updating the eigendecomposition of the Gram matrix
\[
G = K - \frac{1}{M}KE_M - \frac{1}{M}E_MK + \frac{1}{M^2}E_ME_MK,
\]
at every step can be done in \(O(M^2)\). Here, \(E_M = 1_M \times 1_M^T\) and \(1_M\) is the \(M\) dimensional vector of 1’s.

**Enforcing an Inferred Constraint** KPCA learns the constraint as a manifold in its Reproducing Kernel Hilbert Space \(F\). The output of KPCA is the set of vectors \(\alpha_i\), which enable projecting the user inputted next state \(s_t\) onto each principle component, and in turn that enables computing the projection of \(s_t\) onto \(h_t\) in \(F\), denoted by \(Ps_t\), via (8). To enforce the constraint, the robot needs to compute the state corresponding to \(Ps_t\), i.e. the preimage of the projection.

In general, finding preimages is computationally expensive. The approach we take for finding preimages is an approximation based on [34]: we learn a function \(\Gamma : F \rightarrow \mathbb{R}^d\) such that \(\Gamma(\phi(s)) \approx s\) locally.

Our insight for learning a \(\Gamma\) is to use the robot’s trajectory so far, along with the projections \(Ps\) on the currently learned manifold, as training data: \(\mathcal{D} = \{(s_i, Ps_i)|i = \{t - M + 1, \ldots, t - 1\}\}\). A few aspects combine to make this work well: 1) \(\Gamma\) only needs to work well locally, in the space of interest, i.e. along the robot’s trajectory, where the training data is; 2) the states visited so far, \(s_t\), lie approximately on the manifold: even though \(\phi(s_{t}) \neq Ps_{t}\) in general, this is approximately true along the trajectory so far (in the current time horizon); and 3) we use a simple function class for \(\Gamma\) to prevent overfitting to the noise in \(s_t\), and construct a function that maps points in feature space closer to the actual manifold in task space.

We thus use a linear model for each output dimension of \(\Gamma\):
\[
\Gamma_j(\psi) = w_j^T \psi, \quad j = 1, \ldots, d
\]
for \(\psi \in F\). We learn the weights \(w_j\) by solving the following optimization problem:
\[
w_j = \arg\min_{w_j} \sum_{i=t-M+1}^{t-1} \mathcal{L}(s_i, w_j^TP\phi(s_i)) + \lambda \Omega(\Gamma),
\]
where \(\mathcal{L}\) is loss function penalizing distance in task space, \(\Omega\) is a a regularizer, and \(\lambda\) is a pre–selected non–negative weight.

Applying the learned function \(\Gamma\) to the projected state \(s_t\) in feature space, \(Ps_t\), yields the projection of the user’s desired next state in task space onto the constraint:
\[
\text{projection of } s_t: \Gamma(Ps_t)\quad (12)
\]

**B. Assistance**

**Assistance for One Constraint** If the robot were assisting with a known constraint, then it is sufficient to go to \(\Gamma(Ps_t)\). However, the robot does not actually know the constraint, and its inference might be wrong. Key to successful assistance is knowing when to (or not to) assist.

Therefore, besides inferring the constraint manifold, the robot should also compute its confidence in the inference. In the case that the user is always following the same constraint, how far away the trajectory so far is from the manifold is a good indicator of how accurate the manifold is. We thus measure the confidence in the inference as inversely proportional to the average distance between previous states and the preimages of their projects onto the manifold:
\[
d_t = \sum_{i=t-M+1}^{t} |s_i - \Gamma(Ps_i)|,\quad (13)
\]
The bigger \(d_t\) is, the less confident the robot must be in its prediction. Let \(c_t^1\) denote the confidence in the inferred constraint at time \(t\):
\[
c_t^1 = e^{-\gamma_1 d_t},\quad (14)
\]
where \(\gamma_1\) is a positive selected scalar. Equation (14) ensures that \(c_t^1 \in [0, 1]\), and \(c_t^1\) decreases as \(d_t\) increases.

We propose to blend between the user–provided \(s_t\) and its projection on the inferred constraint, \(\Gamma(Ps_t)\), using:
\[
s_t^R = (1 - c_t^1)s_t + c_t^1 \Gamma(Ps_t)\quad (15)
\]
with \(s_t^R\) being the blended state to which the robot moves at time \(t\). Once \(s_t^R\) is reached, the user provides the next input \(u_{t+1}\), leading to the inputted state \(s_{t+1}\), and the process repeats for \(L_{t+1} = s_{t-M+2} \cdots s_{t+1}\).

**Assistance for Switching Constraints** The confidence measure \(c_t^1\) is designed for when there is a single constraint that the user is always trying to maintain. But executing a real task may require either maintaining a sequence of dissimilar constraints, or switching from maintaining a constraint to being unconstrained. The confidence measure \(c_t^1\) does not capture such cases well: once the robot becomes confident, it starts assisting a lot and biasing the state sequence. Confidence could also be computed based solely on the user inputs; however, we found that once people realize that the robot is intelligent enough to guide them through the constraint, they stop providing informative inputs. For instance, they constantly move the joystick along a single Cartesian direction even they need the robot...
to move along a direction different from their input, making input–based confidence impractical.

Thus, while \( c^1 \) works well in the one constraint case (as we will see in the first user study), we need to augment it to detect changing constraints. We leverage the natural difference in operator input when following a constraint versus switching constraints.

When the operator is controlling the robot on an ongoing constraint, once a deviation from the underlying constraints is observed, the operator provides control inputs that correct and cancel out the observed deviation. In other words, moving along a constraint is formed by a set of deviations and corrections that are on average in the direction of the constraint. On the other hand, while leaving a constraint, the states ensuing from the user’s raw (un–arbitrated) inputs are constantly along a direction different from \( h_1 \). We can detect this.

This suggests that augmenting our measure of confidence requires computing the alignment between the direction suggested by the average user input, and the direction of the constraint. We denote the direction of average user input by \( \delta_t^u \), and compute it as

\[
\delta_t^u = \frac{1}{M-1} \sum_{i=-M+1}^{t-1} f(s_i, u_i) - s_i
\]

where \( f \) is the task space dynamics model – this computes the average difference between the user inputted state and the current state.

The constraint manifold is feature space, so we approximate it via \( \delta_t^c \), the average direction of the robot’s trajectory:

\[
\delta_t^c = \frac{1}{M-1} \sum_{i=-M+1}^{t-1} s_{i+1} - s_i
\]

Let \( \theta_t \) be the alignment between these two measures:

\[
\theta_t = \cos^{-1} \left( \frac{\delta_t^u \cdot \delta_t^c}{\| \delta_t^u \| \| \delta_t^c \|} \right)
\]

We compute \( c_t^2 \) by:

\[
c_t^2 = e^{-\gamma_2 \theta_t};
\]

We measure the overall confidence in robot’s inference, \( c_t^3 \), by combining the two measures:

\[
c_t^3 = c_t^1 c_t^2
\]

\( c^3 \) replaces \( c^1 \) in 15.

V. Experiments

Our experiments are two-fold: we are interested in the performance of the constraint inference algorithm, as well as its impact on real user teleoperation scenarios.

A. Constraint Inference Analysis

In order to evaluate the accuracy of our inference algorithm, we collected direct teleoperation data (without assistance).

We asked participants to teleoperate the 7-DOF arm from Figure 4 through a joystick interface for moving a grasped object along a predefined path, demonstrated to the users in a simulation environment. We asked participants to traverse the path in the shortest possible time while keeping the grasped object as close as possible to the path. We designed three different scenarios: tracking a line, an arc with a large radius and low curvature as a result and finally moving the grasped object along a semicircle of low radius and high curvature.

Analysis A key element in the performance of any kernel-based algorithm is the choice of kernel made for the algorithm. In our problem in particular, the kernel function restricts the inferred constraints, \( h_t \), to a subset of all possible constraints, i.e. it implicitly makes assumptions about real-world tasks.

We tested our method’s performance across different kernel parameter choices, manipulating kernel type
(polynomial of different degrees \(d\)) and kernel parameters (coefficients \(\gamma\) and the free coefficient \(a\)). Across our tasks, we found the 3\(^{rd}\) order to perform the best and be more robust to parameters (Fig. 3(a)).

We also analyzed the effect of the time horizon on performance. Unsurprisingly, short time horizons produce inferred constraints that overfit to the user’s noisy input (Fig. 3(b)), while longer horizons more easily recover a constraint close to the ground truth (Fig. 3(c)), canceling out the deviations in user input.

**B. User Study 1: Assistance with A Single Constraint**

In this first study, we assess the effectiveness of online assistance in maintaining a single constraint.

**Manipulated Variables** We asked participants to control an arm in the three scenarios described previously: tracking a line, an arc, and a semicircle. In each scenario, the operator controls the robot in two conditions: direct teleoperation (no assistance is provided), or the user is assisted with the inferred task constraint via our (15). We thus manipulate two factors in a factorial design:

1) Assistance: Whether or not the robot provides assistance.
2) Task Difficulty: the constraint the user needs to maintain.

This setup leads to 6 different conditions experienced by each participant. Task difficulty ranges from simple, in the line case, to hard, in the semicircle scenario. We used the confidence measure \(c^1\) in this study.

**Dependent Measures** We have both objective and subjective measures:

1) Task Execution Time.
2) Average deviations from the underlying constraint. Any component of motion normal to the instantaneous direction of constraint is defined as deviation.
3) User’s subjective measure of robot’s intelligence for assistance vs. no-assistance in each scenario (on a 7-point Likert scale)

**Hypothesis:**

**H1.** Assistance improves the performance of the human–robot team, both objectively and subjectively.

**Subject Allocation:** We chose a within-subject design for 9 participants (4 females and 5 males, 27 years old on average) to enable them to compare the assistance vs. no-assistance conditions in each scenario. We counterbalanced the order of the conditions to avoid any biases resulting from ordering effects.

In order to control for the prior skill in playing with joysticks, we asked each participant to take part in a training phase to teleoperate the arm through joystick with no assistance.

**Analysis:** Figure 4 shows the results. We ran a factorial repeated measures ANOVA with assistance and task as factors for each of our dependent measures.

For time, we found both factors had significant effects and there was a significant interaction effect \(F(2, 56) = 6.1, p < .01\). The post-hoc analysis with Tukey HSD corrections showed that assistance improved the timing performance for the line task, \(p < .01\). As the graph shows, the timing for the other two tasks were almost identical.

The results for deviations supported our hypothesis: there was a significant effect for assistance, \(F(1, 57) = 13.56, p < .01\). There was no significant effect for task and no interaction effect: assistance improved deviations across the board.

The results for rating also support our hypothesis: there was a significant effect for assistance, \(F(1, 57) = 17.29, p < .001\), and no other effects were significant. Ratings for the assistance robot were higher across the board.

Overall, the results suggest that assistance does improve subjective and objective performance. Even for
simple tasks in 2D, assistance can significantly improve user’s comfort. We expect that common ADL’s will include 3D constraints which are much harder to satisfy through teleoperation. Furthermore, maintaining task constraints becomes much harder for people with physical impairments.

C. User Study 2: Assistance with Changing Constraints

Our first study indicated that assistance is good when dealing with a single constraint. Next, we investigated what happens when the user needs to switch from a constraint. We conducted a second study to evaluate the effect of our proposed confidence measure, $c_3$, on the performance of assistance.

Manipulated Variables We considered two scenarios: switching from one constraint to a new constraint, or leaving a constraint and entering free space, thus requiring no assistance for the rest of the task execution.

1) Whether or not the confidence measure $c_1^c$ is taken into account ($c_1^c = c_1^e c_2^e$ vs. $c_3^e = c_1^e$).
2) Whether to switch to a new constraint, or to a no-constraint scenario.

We mimicked the scenario of switching to a new constraint by designing the tracking path to be two line segments perpendicular to each other (called line-to-line scenario). We imitated requiring no-assistance from the switching point onward, by designing the path to be a line segment followed by a sequence of high curvature semicircles depicting a sinewave-like shape (line-to-sine scenario).

Dependent Measures: We used the same objective and subjective measures as before: time, deviations, and rating.

Hypothesis:
H2: Incorporating the $c_1^c$ measure of confidence improves the performance both subjectively and objectively.

Subject Allocation: Analogous to user study 1.

Analysis: Figure 5 shows the results. We ran a factorial repeated measures ANOVA with confidence measure and task as factors for each of our dependent measures.

For time, supporting our hypothesis, we found a significant effect for confidence measure, $F(1,27) = 6.39, p = .0210$: using the augmented confidence meant to handle changing constraints lead to lower task time. The task factor was also significant, with changing from one constraint to the other taking longer than changing from a constraint to no constraint. There was no significant interaction effect.

For deviations, also supporting the hypothesis, we found a significant improvement for the augmented confidence $F(1,27) = 19.01, p < .001$. Task again had a significant effect.

For rating, also supporting our hypothesis, we found that users rated the robot using the augmented confidence more highly, $F(1,27) = 10.47, p < .01$. There was no other significant effect.

Overall, the results support that our confidence metric that augments manifold-based confidence with user input direction-based confidence leads to better assistance when dealing with changing constraints.

VI. Discussion

Summary. We introduced and evaluated a method for inferring and assisting with task constraints. Constraint inference happens online, in real-time, and assistance is mediated by confidence and capable of handling changing constraints. This improved teleoperation both objectively and subjectively.

Limitations and Future Work. Albeit useful, constraints are complex and difficult to identify, and much work remains in this area: being able to restrict the space of possible constraints based on possible real-world tasks, incorporating prior knowledge about...
a particular task, identifying the dimensionality of the constraint manifold automatically, handling force-based constraints, as well as testing in real-world assistive robotics scenarios, and with users with motor impairments. We are excited to tackle these challenges in future work.

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References


