# Model Generation from Execution Traces

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Acknowledgments: Avrim Blum

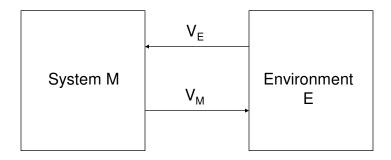
# Today's Lecture

- Generating models of finite-state systems by observing execution traces
  - Based on a machine learning algorithm first proposed by D. Angluin in '87 and improved upon by Rivest & Schapire in '93
- Apr 4: Guest lecture by Anubhav Gupta on using learning in model checking

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State variables  $V = V_E \cup V_M$ ,  $V_E \cap V_M = \phi$ 



Want to observe E and generate a good model of it Usually easy to get a model of M

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# Why Learn Environment Models?

- · As a middle ground between
  - Traditional, pessimistic (worst-case) verification
  - Optimistic verification ("does there exist an environment that makes my system work?")
- To generate environment assumptions for use in assume-guarantee reasoning
- To deal with incorrect models (of system modules or environment)
  - May miss behaviors and also include spurious behaviors

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#### A Quote

- "Assumptions are the things you don't know you're making"
  - Douglas Adams, Mark Cawardine, "Last Chance to See"

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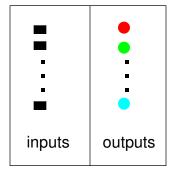
# Learning Env. Model

- Model: (Deterministic) Finite Automaton
  - As a representation of the set of traces of env.
- What we can do:
  - Provide inputs to the environment
  - Observe (finite) prefixes of environment's output trace
- Note:
  - Env. is a reactive system too, has infinitely long traces but we can only observe finite prefixes
  - So we are learning a finite automaton (not a Buchi automaton)

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#### **Another View**

- Environment is a box, with input buttons and output lights
  - Outputs capture observable part of env state
- We can press some subset of input buttons at any time step
- Observe what lights turn on



Assumption for this lecture: We can "reset" the environment at any time

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# Angluin's DFA Learning Algo.

(adapted to our setting)

- Input: A box as in the previous picture
  - inputs from an alphabet  $\boldsymbol{\Sigma}$
- Outputs: a DFA that accurately represents all (finite) output traces seen so far
- What it can do:
  - Generate environment traces by supplying inputs
  - Ask an oracle whether a candidate DFA is indeed correct (if not, get a counterexample)
  - Reset environment model to initial state

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# Angluin's DFA Learning Algo. (adapted to our setting)

- Input: A box as in the previous picture
  - inputs from an alphabet Σ
- Outputs: a DFA that accurately represents all (finite) output traces seen so far
  - · Given an oracle that precisely knows the environment, it learns the DFA representing exactly the output traces of the env.
- What it can do:
  - Generate environment traces by supplying inputs
  - Ask an oracle whether a candidate DFA is indeed correct (if not, get a counterexample)

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## Formal Setup

- Want to learn (synthesize) a DFA (Q, Σ, δ,
  - Q : set of states
  - $-\Sigma$ : input alphabet
  - $-\delta$ : transition function: Q x  $\Sigma \rightarrow$  Q
  - L: labeling/output function
- What does it mean for two states of the DFA to be different?

(In terms of the labels we observe)

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## Formal Setup

- Want to learn a DFA (Q, Σ, δ, L)
  - Q : set of states
  - $-\Sigma$ : input alphabet
  - $-\delta$ : transition function: Q x  $\Sigma \rightarrow$  Q
  - L: labeling/output function
- What does it mean for two states of the DFA to be different?
  - q and q' are different if there is a input sequence s.t. the states reachable on that sequence from q and q' respectively have different labels

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#### What defines a state

- Its label (observable part)
- What input sequence gets us to that state
  - Could be many, pick a representative
- What output sequence we see from that state
  - Perform "experiments" from that state to see this
- Angluin's algorithm "names" a state by the latter two things
  - A prefix and a suffix

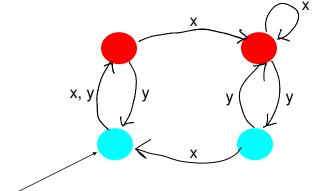
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# Algorithm Sketch

- 1. Start with only the DFA's initial state q<sub>0</sub>
- 2. Generate a "new" state by supplying inputs
- 3. Check if its next states are observationally different from those of existing states
  - If yes, add it in
  - If not, ask the oracle if we have the correct DFA
    - If yes, we're done
    - If not, use the counterexample to figure out what new state(s) to add until that counterex goes away
  - Go back to step 2

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# An Example



This is the DFA we want to learn (the correct environment model)

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How the algorithm works on the previous example – worked out on board

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# Complexity

- Polynomial in size of environment model
- · Good if environment model is small
  - This is why it is especially good for learning assumptions or concise env specifications

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# Some Refs. to Applications

- "Adaptive Model Checking" -- Groce, Peled, Yannakakis, TACAS'02
- "Learning Assumptions for Compositional Verification" -- Cobleigh et al., TACAS'03

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#### Next: Part III of the course

- Next week: Decision procedures for fragments of first-order logic
  - Equivalent of Part I lectures on "SAT solving"
- · After spring break:
  - -Guest lecture
  - Your presentations

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